

ESI

Theoretical Investigation of various aspects of Two Dimensional holey Boroxine, B₃O₃

Computational Details:

SIESTA code has the capability of making a cocktail of various functionals to be employed in the calculations^{1, 2}. In this regard, we combine GGA with the LDA to make a hybrid functional, though it is not in the true spirit of the hybrid since the exact Hartree-Fock exchange is absent^{3, 4}. The exchange energy is built by taking 50% of each functional, whereas, 25-75% GGA-LDA is used to define the correlation part. For AIMD simulations, we use both the hybrid and vdW-DF level by employing a 2x2 supercell. The heat treatment is performed at 300K and 600 K where the heat-bath is controlled by the Nosé–Hoover thermostat with NVT ensemble. The VASP calculations were carried out with a kinetic energy cutoff of 500 eV⁵⁻⁷. The forces and energy convergence criteria are set as 0.01 eV/Å and 10⁻⁶ eV, respectively. We use Methfessel-Paxton smearing with 0.05-0.001 eV smearing width since we also report various properties of graphene/graphite for the comparison⁸. Spin polarization is turned on in each and every case.

We also calculate the formation energy of B₃O₃ monolayer by taking the energy of one O from O₂ molecule as a chemical potential using the equation given in the main text. At PBE-D3 level, the formation energy of B₃O₃ monolayer is -5.03 eV/atom. With the same definition, the formation energy at PBE-D2 and hybrid levels are -5.023 and -5.38 eV/atom, respectively. For completeness, the cohesive energy of O₂ molecule is -3.377, -3.374, and -3.385 eV/atom at PBE-D3, PBE-D2, and hybrid level, respectively. The vulnerability of SIESTA's results to BSSE is a known fact, therefore, the energetics from SIESTA cannot be trusted. Yet we see a reasonable agreement between hybrid and PBE-D2/PBE-D3 values.

Table 1: Structural parameters (in Å), charge transfer, band gaps and cohesive strengths at various levels of study. On an average, charge accumulation on O atoms is equal to the charge depletion on B atoms.

	Lattice parameter a (Å)	d_{BB} (Å)	d_{BO} (Å)	d_{OO} (Å)	*Charge $ e $	Band-gap (eV)	Cohesive energy (eV/atom)
GGA	7.83	1.73	1.39	6.28	0.15	3.66	
vdW-DF	7.89	1.74	1.39	6.33	0.15	3.80	
Hybrid	7.81	1.72	1.38	6.27	0.15	3.66	-7.08
PBE-D2	7.83	1.72	1.39	6.28	1.96	3.57	-6.71
PBE-D3	7.82	1.72	1.39	6.27	1.96	3.57	-6.72
M06-L	7.78	1.71	1.38	6.21	0.4	3.90	-6.3
HSEH1PBE	7.80	1.72	1.38	6.24	0.4	5.30	

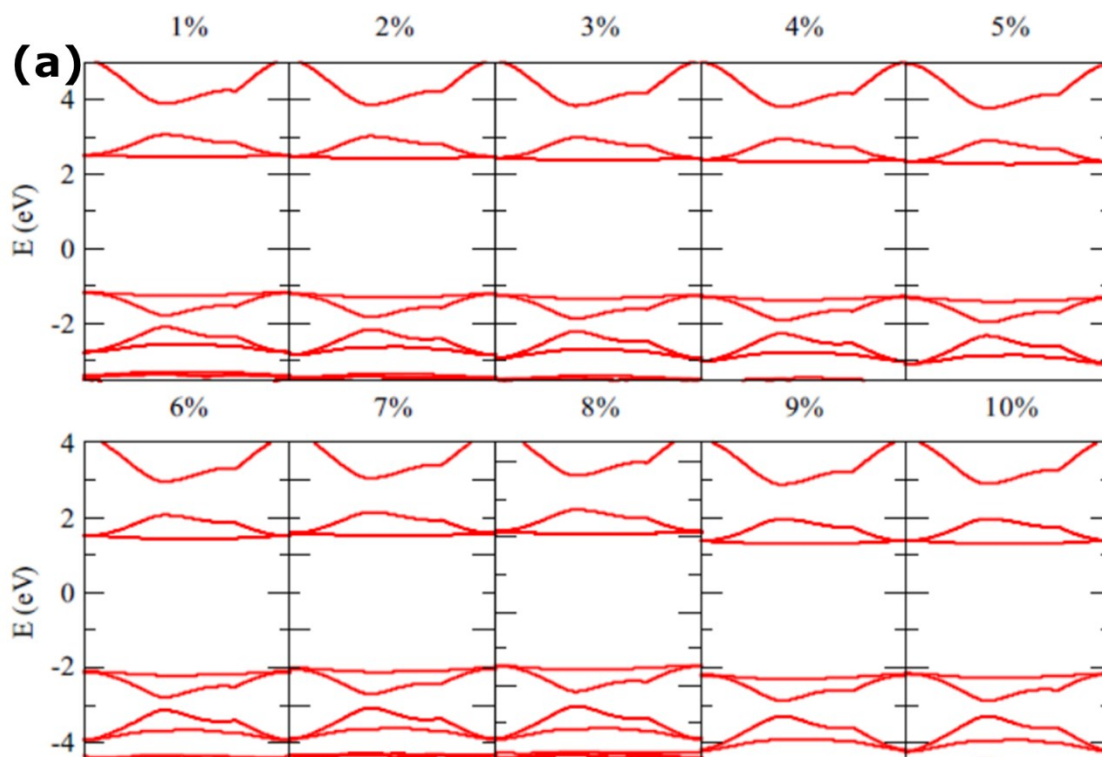
*Hirshfeld and Voronoi analyses in SIESTA, Bader in VASP, and Mulliken in Gaussian

Table S2 : Structural and energetics data at various levels of theory

	Relative energy (meV)	IIE (meV/atom)	E_{exf} (meV/Å ²)	Interlayer separation, $h, h1/h2$ (Å)
PBE-D2				
B₃O₃	1100			
AA-bilayer	870	9.6		3.55
AB-bilayer	650	18.73		3.138/3.25
AB2-bilayer	570	22.13		2.97/3.2

AA-bulk	550	22.83	5.1	3.11
AB-bulk	85	42.34	9.5	3.0/3.0
AB2-bulk	0	45.88	10.37	2.97/3.0
Graphene-bilayer		25		3.33
Graphite		55.9	21	3.21
vdW-DF				
B₃O₃	1732			
AA-bilayer	1082	27		3.56
AB-bilayer	984	31		3.33/3.52
AB2-bilayer	856	36.5		3.03/3.33
AA-bulk	456	53	11.8	3.6
AB-bulk	103	68	15	3.27/3.27
AB2-bulk	0	72	16	3.16/3.16
Hybrid				
B₃O₃	798			
AA-bilayer	565	9.7		3.5
AB-bilayer	460	14.1		3.32/3.45
AB2-bilayer	358	18.3		3.04/3.3
AA-bulk	375	17	4	3.6
AB-bulk	88	29	6.7	3.21/3.21
AB2-bulk	0	33	7.5	3.09/3.14
Graphene-		17.5		3.35

bilayer				
Graphite		35	13	3.35



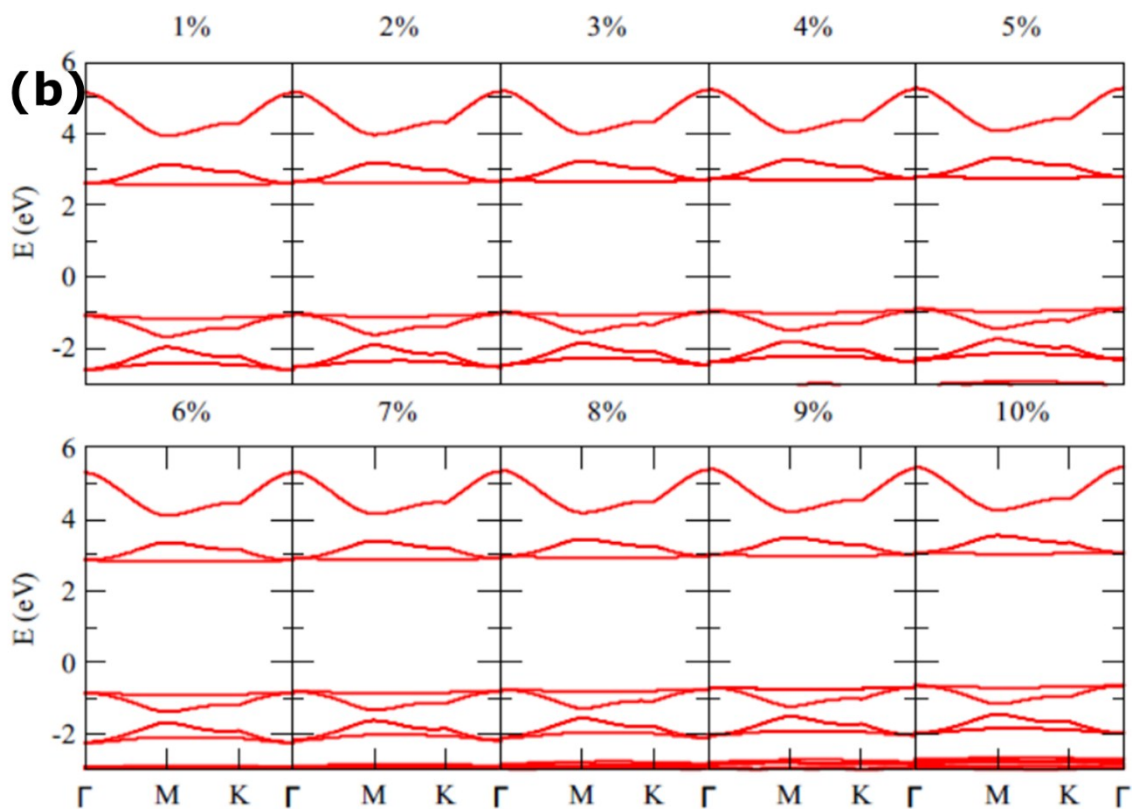


Figure S1: Electronic band structure of B3O3 monolayer with biaxial strain, (a) compression and (b) expansion

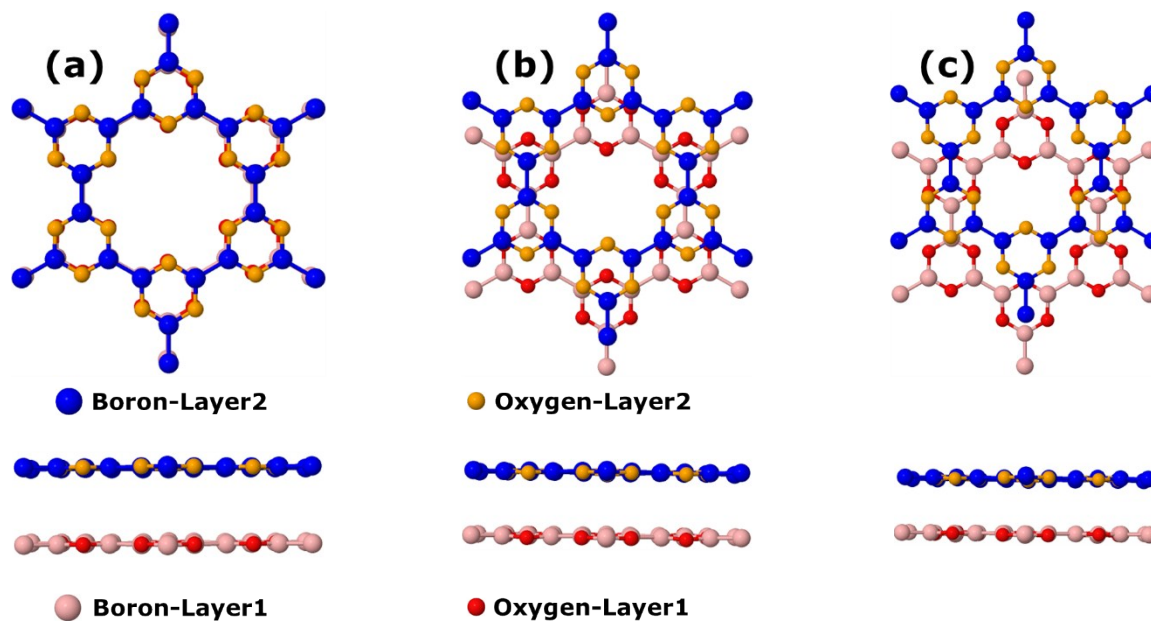


Figure S2: Geometric structures of bilayer B3O3 in (a) AA, (b) AB, and (c) AB2 stacking.

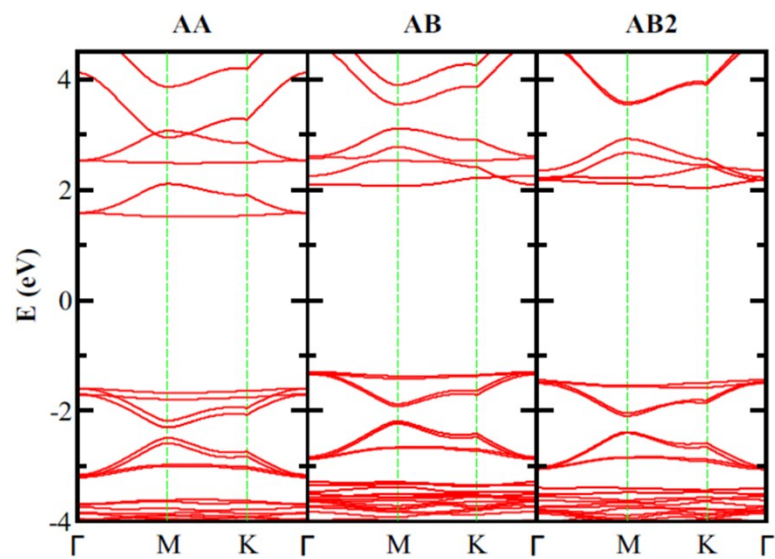
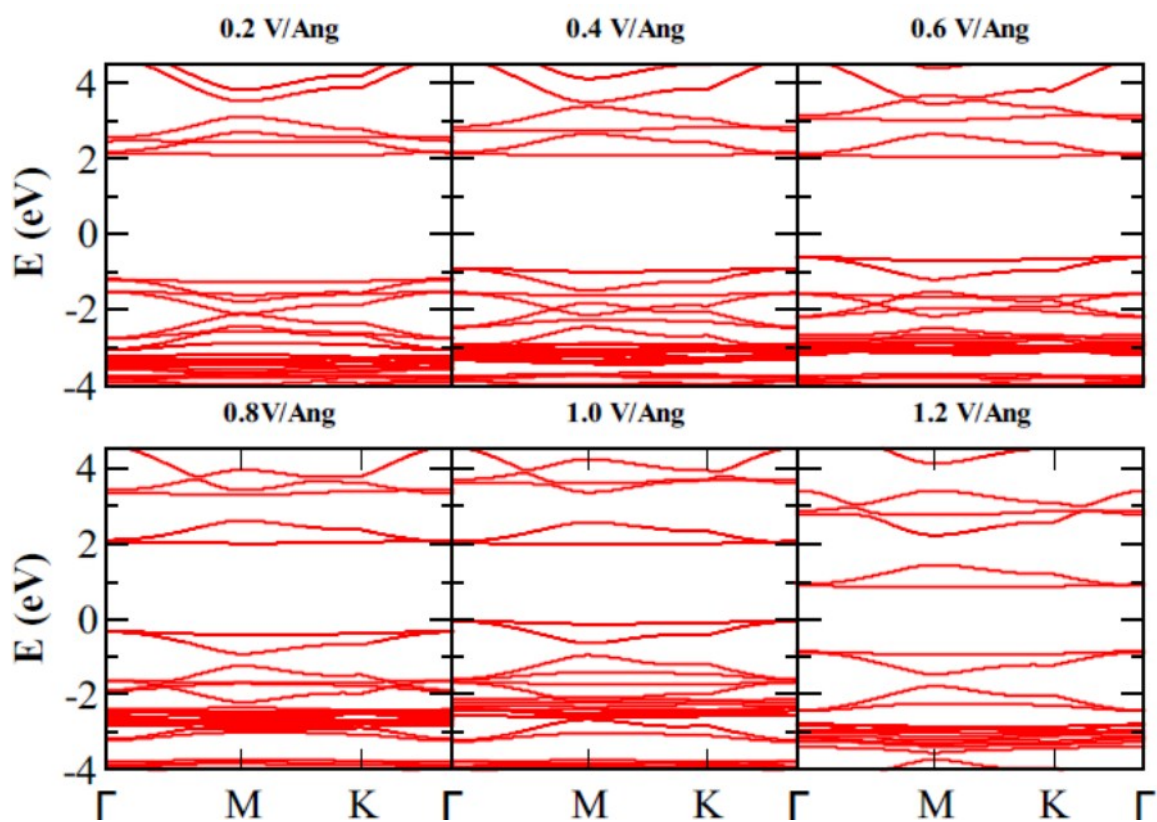


Figure S3: Bilayer B3O3 band structures at hybrid level of theory



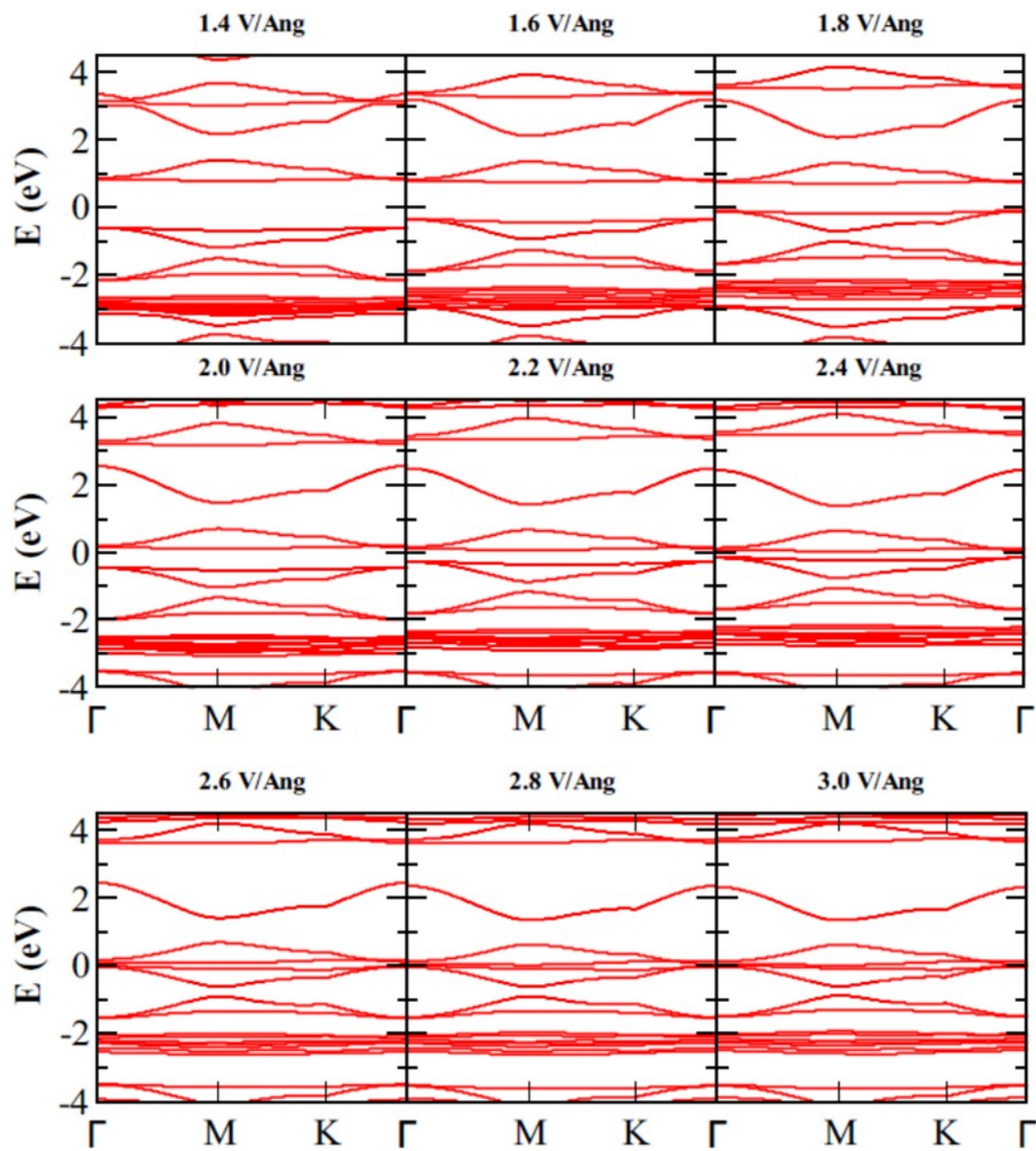


Figure S4: Electronic band structures of AB₂ stacked bilayer B₃O₃ in the presence of external electric field

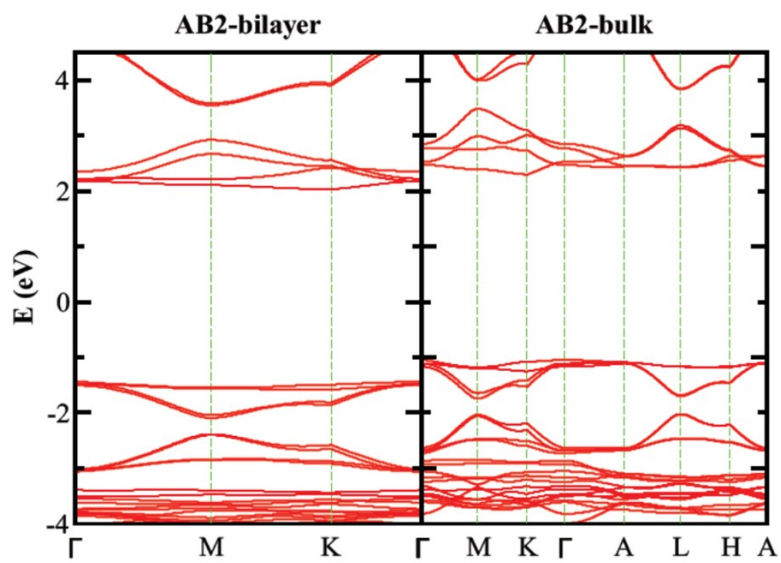


Figure S5: Comparison of the band structures of bilayer and bulk B3O3 at hybrid level of theory


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1 #-----
2
3 # CRYSTAL DATA
4
5 #-----
6
7 data_VESTA_phase_1
8
9
10 _chemical_name_common          'B3O3-PBE-D3
11 _cell_length_a                 7.82000
12 _cell_length_b                 7.82000
13 _cell_length_c                 20.00000
14 _cell_angle_alpha              90
15 _cell_angle_beta               90
16 _cell_angle_gamma              120.00
17 _space_group_name_H-M_alt      'P 1'
18 _space_group_IT_number         1
19
20 loop_
21 _space_group_symop_operation_xyz
22   'x, y, z'
23
24 loop_
25   _atom_site_label
26   _atom_site_occupancy
27   _atom_site_fract_x
28   _atom_site_fract_y
29   _atom_site_fract_z
30   _atom_site_adp_type
31   _atom_site_B_iso_or_equiv
32   _atom_site_type_symbol
33   B1          1.0      0.640757      0.972400      0.149790      Biso  1.000000 B
34   B2          1.0      0.331130      0.972395      0.150143      Biso  1.000000 B
35   B3          1.0      0.331131      0.662809      0.150149      Biso  1.000000 B
36   B4          1.0      0.204228      0.408949      0.150141      Biso  1.000000 B
37   B5          1.0      0.894609      0.099345      0.149779      Biso  1.000000 B
38   B6          1.0      0.204243      0.099371      0.150136      Biso  1.000000 B
39   O1          1.0      0.536195      0.767330      0.149853      Biso  1.000000 O
40   O2          1.0      0.536183      0.072900      0.149842      Biso  1.000000 O
41   O3          1.0      0.230582      0.767334      0.150399      Biso  1.000000 O
42   O4          1.0      0.999154      0.304403      0.149835      Biso  1.000000 O
43   O5          1.0      0.999176      0.998851      0.149827      Biso  1.000000 O
44   O6          1.0      0.304767      0.304424      0.150395      Biso  1.000000 O

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Cif file of monolayer B3O3 at PBE-D3 level. VESTA software is used for the conversion.⁹

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