



# WIND AND ENERGY STORAGE

Optimal Control of Power Systems in Context of Wind  
Energy Generation and Storage

Shuyang Li

# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration





# MOTIVATION

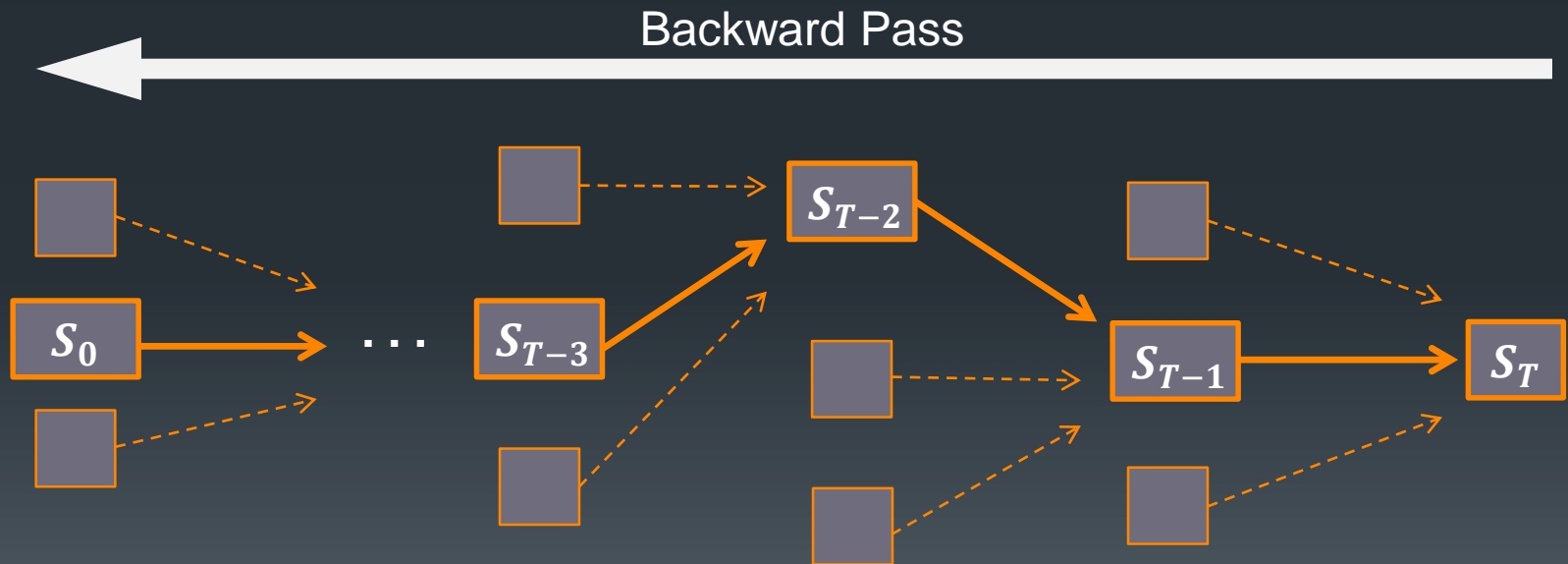
- Increasing reliance on wind energy
- Wind Energy Variance
  - Avoid waste
- Storing Wind
  - Storage/Unit Allocation



# MOTIVATION – Dynamic Programming

- Solving Bellman's Equation:

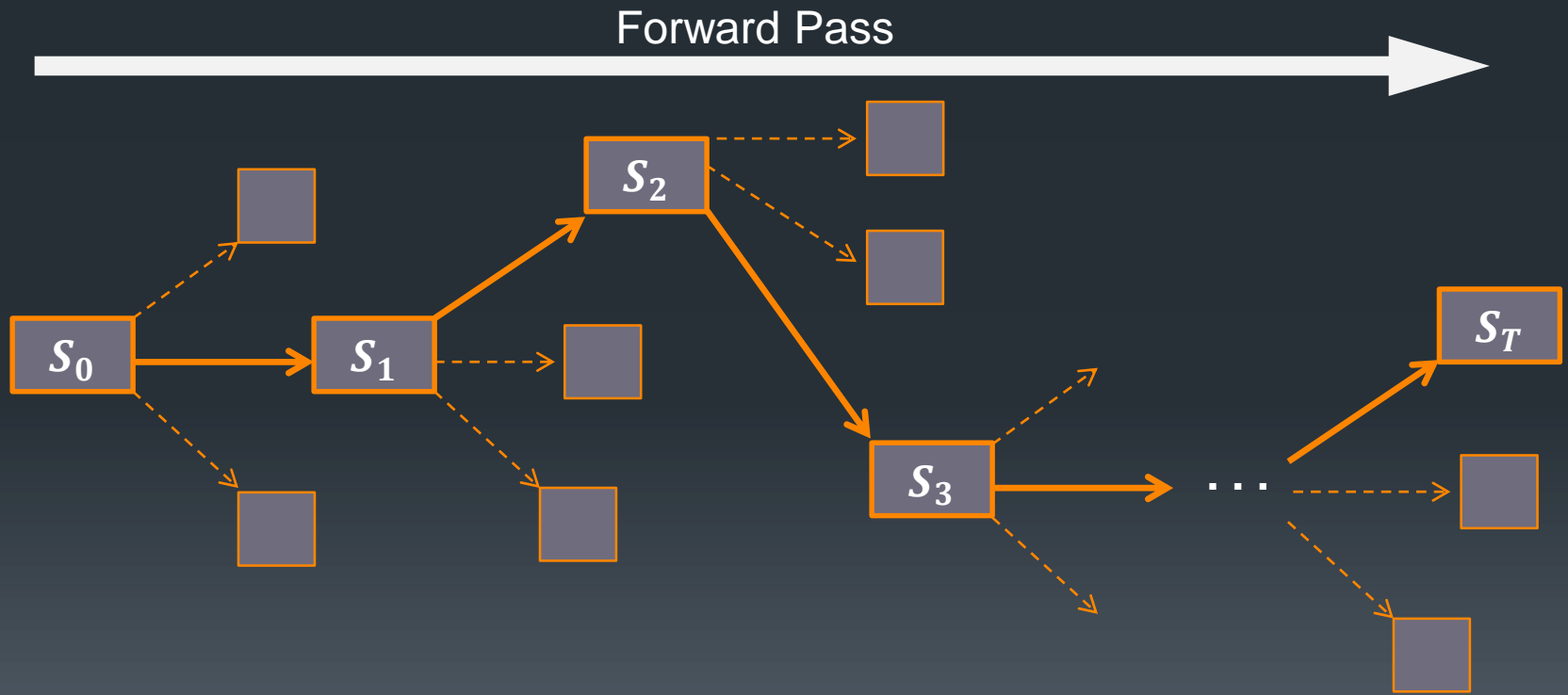
$$V(S^n) = \max_a (C(S^n, a) + \gamma \mathbb{E}\{V(S^{n+1}) | S^n\})$$



# MOTIVATION – ADP/RL



- *Monte Carlo Simulation*



# MOTIVATION - Literature

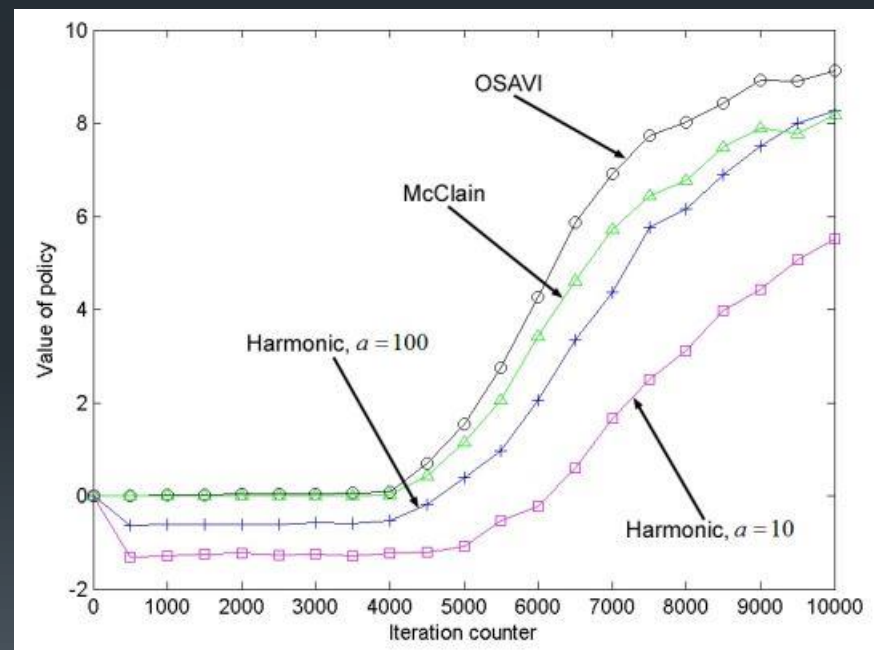
- *“A Comparison of Approximate Dynamic Programming Techniques on Benchmark Energy Storage Problems: Does Anything Work?”*
  - Jiang, Pham & Powell, 2014
- *“Benchmarking a Scalable Approximate Dynamic Programming Algorithm for Stochastic Control of Multidimensional Energy Storage Problems”*
  - Salas & Powell, 2014





# PROBLEM

- Algorithmic Performance
  - Q-Learning
  - SARSA( $\lambda$ )
  - Step Sizes



Ryzhov, Frazier & Powell (2014)

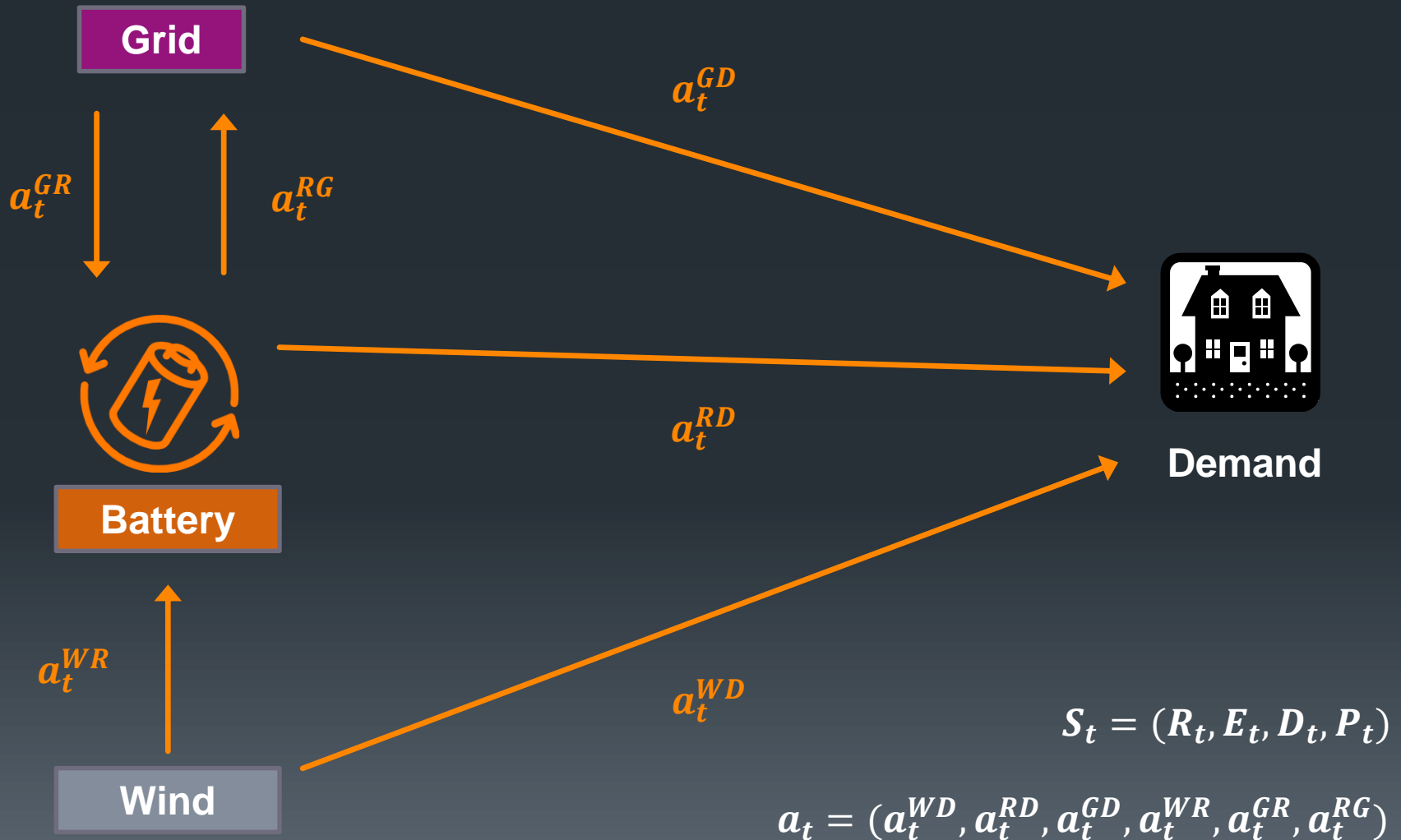
# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration





# MODEL





# MODEL – Action Constraints

Storage capacity:

- $a_t^{WR} + a_t^{GR} \leq R^{max} - R_t$
- $a_t^{RD} + a_t^{RG} \leq R_t$

Charging / Discharging

- $a_t^{WR} + a_t^{GR} \leq \gamma^c$
- $a_t^{RD} + a_t^{RG} \leq \gamma^d$

Demand satisfied:

- $a_t^{WD} + \eta^d a_t^{RD} + a_t^{GD} = D_t$

Flow Conservation

- $a_t^{WR} + a_t^{WD} \leq E_t$

**Maximal Wind Usage:**

- $a_t^{WD} = \min(D_t, E_t)$
- $a_t^{WR} = \min(R^{max} - R_t, E_t - a_t^{WD})$



# MODEL – Transition Functions

Storage:

$$R_{t+1} = R_t + \phi^T a_t; \phi = (0, -1, 0, \eta^c, \eta^c, -1)$$

Simplified in the stochastic model:

$$R_{t+1} = R_t - a_t^{RD} + a_t^{WR} + a_t^{GR} - a_t^{RG}$$

# MODEL – Transition Functions

Wind:

- $E_{t+1} = E_t + \hat{E}_{t+1}$
- $\hat{E}_t \sim \mathcal{N}(\mu_E, \sigma_E^2)$

Price:

- $P_{t+1} = P_t + \hat{P}_{0,t+1} + 1_{\{u_{t+1} \leq 0.031\}} \hat{P}_{1,t+1}$
- $\hat{P}_{0,t} \sim \mathcal{N}(\mu_P, \sigma_P^2)$
- $\hat{P}_{1,t} \sim \mathcal{N}(0, 50^2)$
- $u_t \sim \mathcal{U}(0,1)$

Demand:

- $D_t = \left\lceil \max \left[ 0, 3 - 4 \sin \left( \frac{2\pi t}{T} \right) \right] \right\rceil$



# MODEL – Objective Function

Reward Function:

$$C(S_t, a_t) = P_t D_t - P_t (a_t^{GR} - \eta^d a_t^{RG} + a_t^{GD}) - c^h R_{t+1}$$

Objective Function:

$$F^{\pi^*} = \max_{\pi \in \Pi} \mathbb{E} \left[ \sum_{t \in T} C(S_t, A_t^{\pi}(S_t)) \right]$$

# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration





# ALGORITHMS – Q-Learning

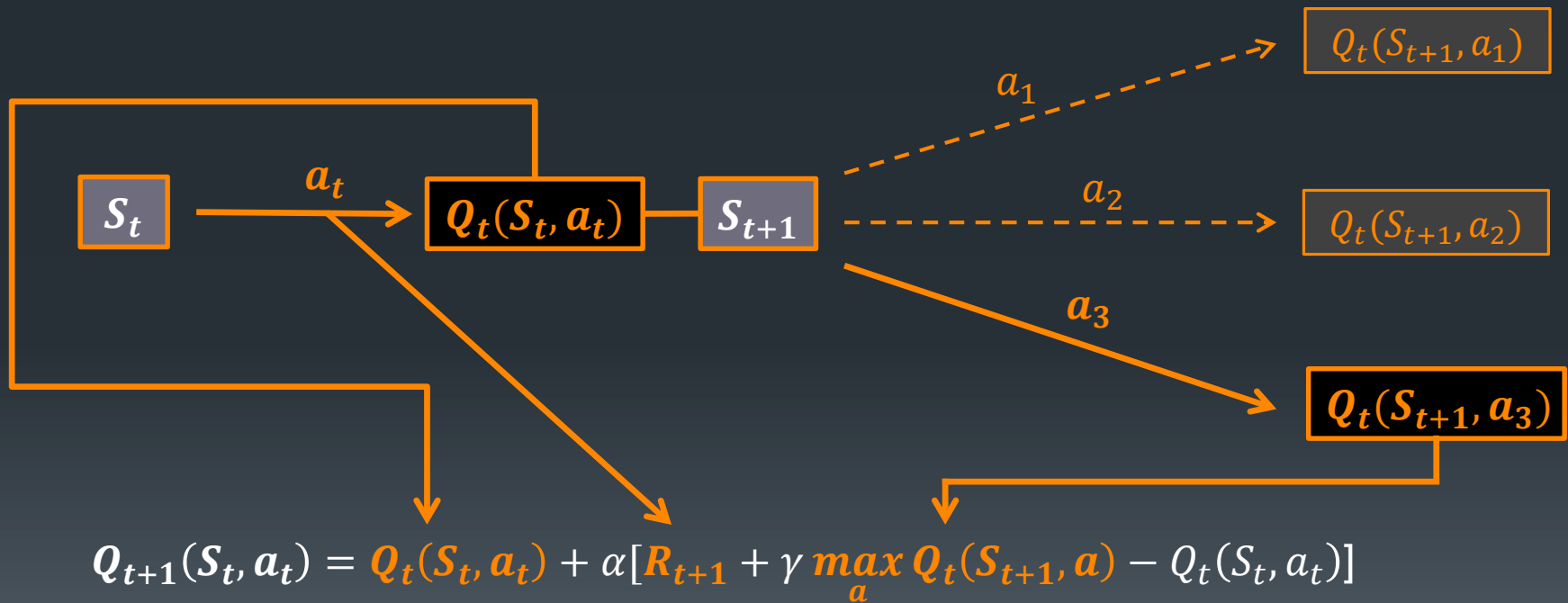
- Action-value function Q

$$Q_{t+1}(S_t, a_t) = Q_t(S_t, a_t) + \alpha [R_{t+1} + \gamma \max_a Q_t(S_{t+1}, a) - Q_t(S_t, a_t)]$$

- *Off-policy*
  - Selection policy:  $\epsilon$ -greedy
  - Evaluation policy: pure greedy



# ALGORITHMS – Q-Learning







# ALGORITHMS - SARSA

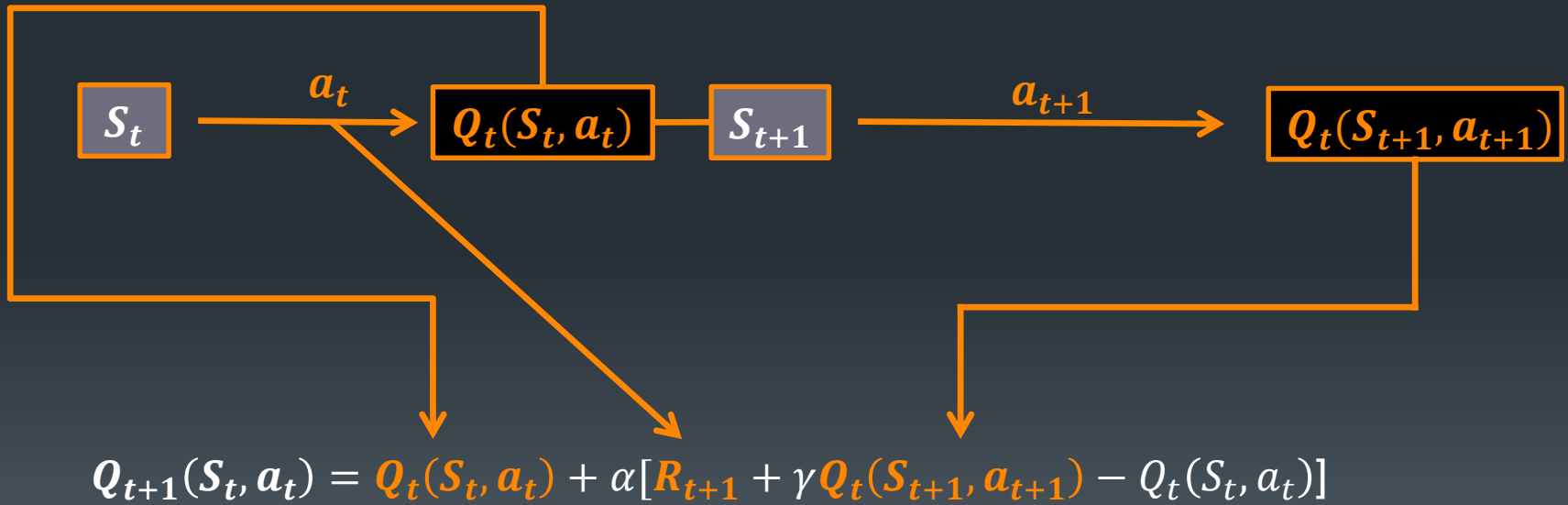
- SARSA [ $s_t$   $a_t$   $R_{t+1}$   $S_{t+1}$   $a_{t+1}$ ]

$$Q_{t+1}(S_t, a_t) = Q_t(S_t, a_t) + \alpha[R_{t+1} + \gamma Q_t(S_{t+1}, a_{t+1}) - Q_t(S_t, a_t)]$$

- *On-policy*
  - Evaluation policy is selection policy



# ALGORITHMS - SARSA





# ALGORITHMS – SARSA( $\lambda$ )

- SARSA( $\lambda$ ) includes a backward pass along a path (eligibility trace)

$$Q_{t+1}(S, a) = Q_t(S, a) + \alpha \delta_t Z_t(s, a)$$

$$\delta_t = R_{t+1} + \gamma Q_t(S_{t+1}, a_{t+1}) - Q_t(S_t, a_t)$$

$$Z_t = \begin{cases} \gamma \lambda Z_{t-1} + 1, & S = S_t, a = a_t \\ \gamma \lambda Z_{t-1}, & \textit{otherwise} \end{cases}$$



# ALGORITHMS – SARSA( $\lambda$ )

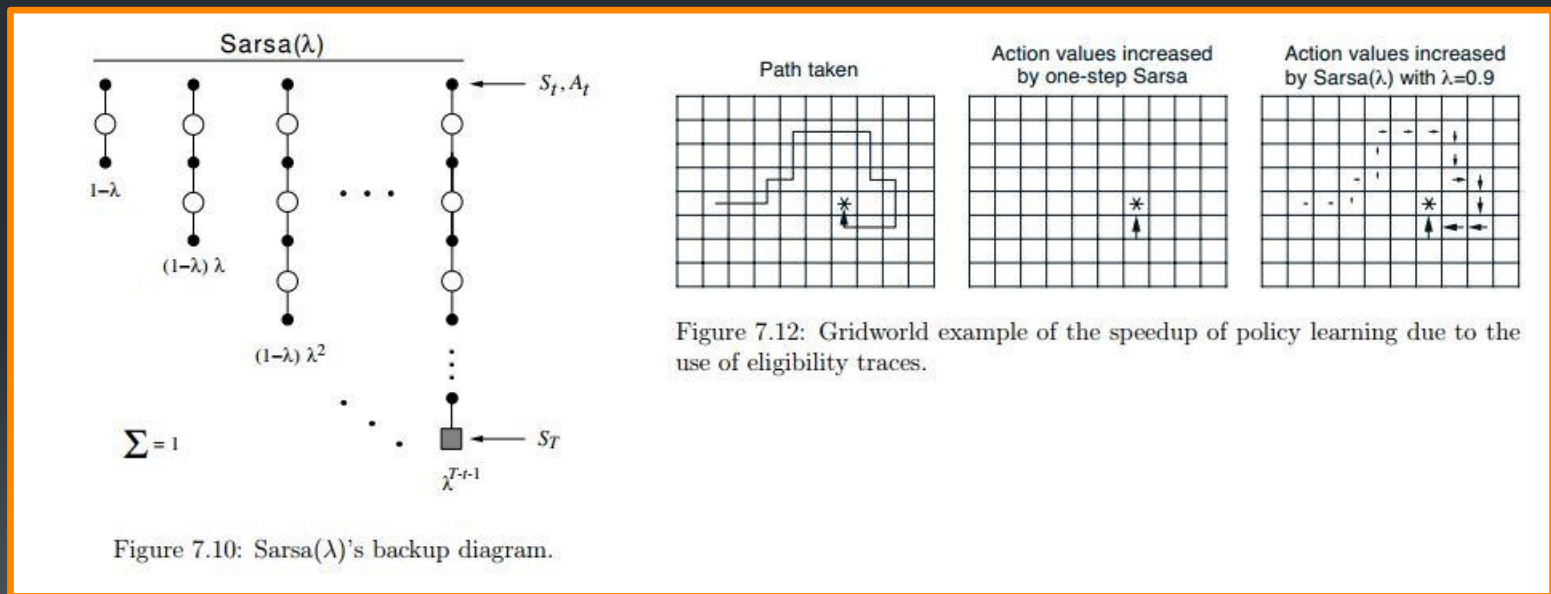


Figure 7.10: Sarsa( $\lambda$ )'s backup diagram.

Figure 7.12: Gridworld example of the speedup of policy learning due to the use of eligibility traces.



# ALGORITHMS – Step Sizes

- Updating equation:

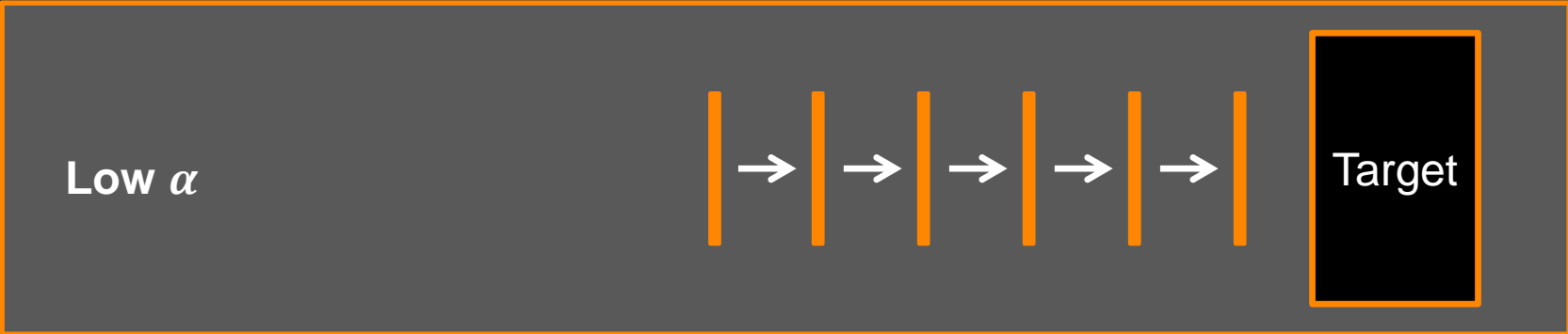
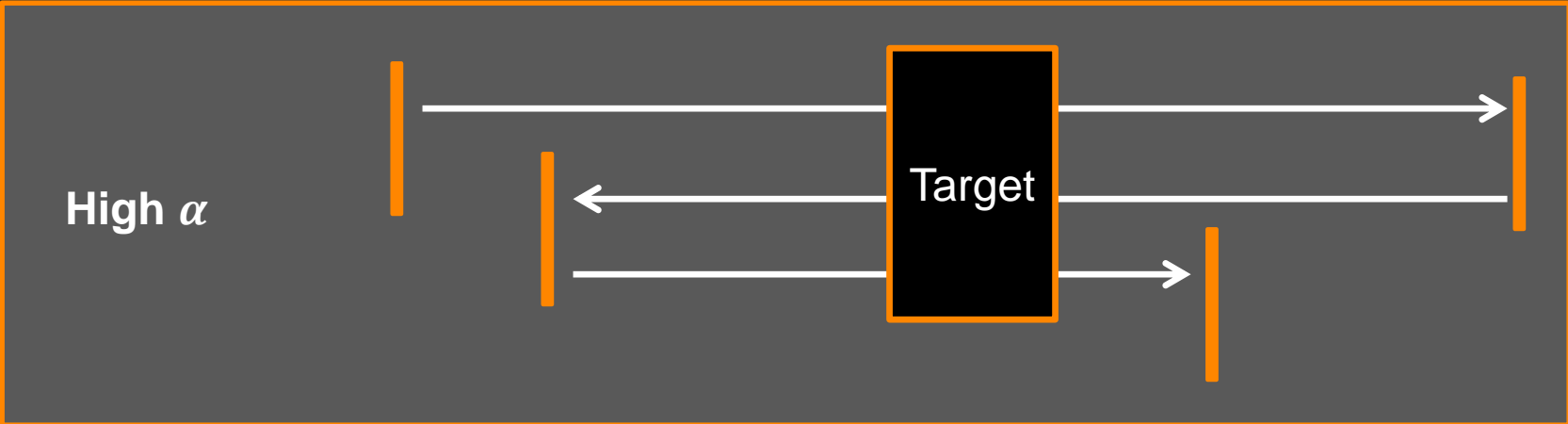
$$Q_{t+1}(S_t, a_t) = Q_t(S_t, a_t) + \alpha [R_{t+1} + \gamma \max_a Q_t(S_{t+1}, a) - Q_t(S_t, a_t)]$$

- Rearranged:

$$Q_{t+1}(S_t, a_t) = (1 - \alpha)Q_t(S_t, a_t) + \alpha [R_{t+1} + \gamma \max_a Q_t(S_{t+1}, a)]$$



# ALGORITHMS – Step Sizes





# ALGORITHMS – Step Sizes

- Constant :  $\alpha = k$
- Harmonic :  $\alpha = \frac{a}{a+n}$
- $1/n$  :  $\alpha = \frac{1}{n}$
- Ryzhov Formula
  - Ryzhov, Frazier & Powell (2014)

# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration







# METHODOLOGY - Simulation

- 1 Deterministic Problem
- 17 Stochastic Problems
  
- 256 Sample Paths per stochastic problem
  
- Training iterations: transitions by Monte Carlo simulation
  - $\epsilon$ -greedy action selection
  
- Evaluation: Averaged over all sample paths

# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration

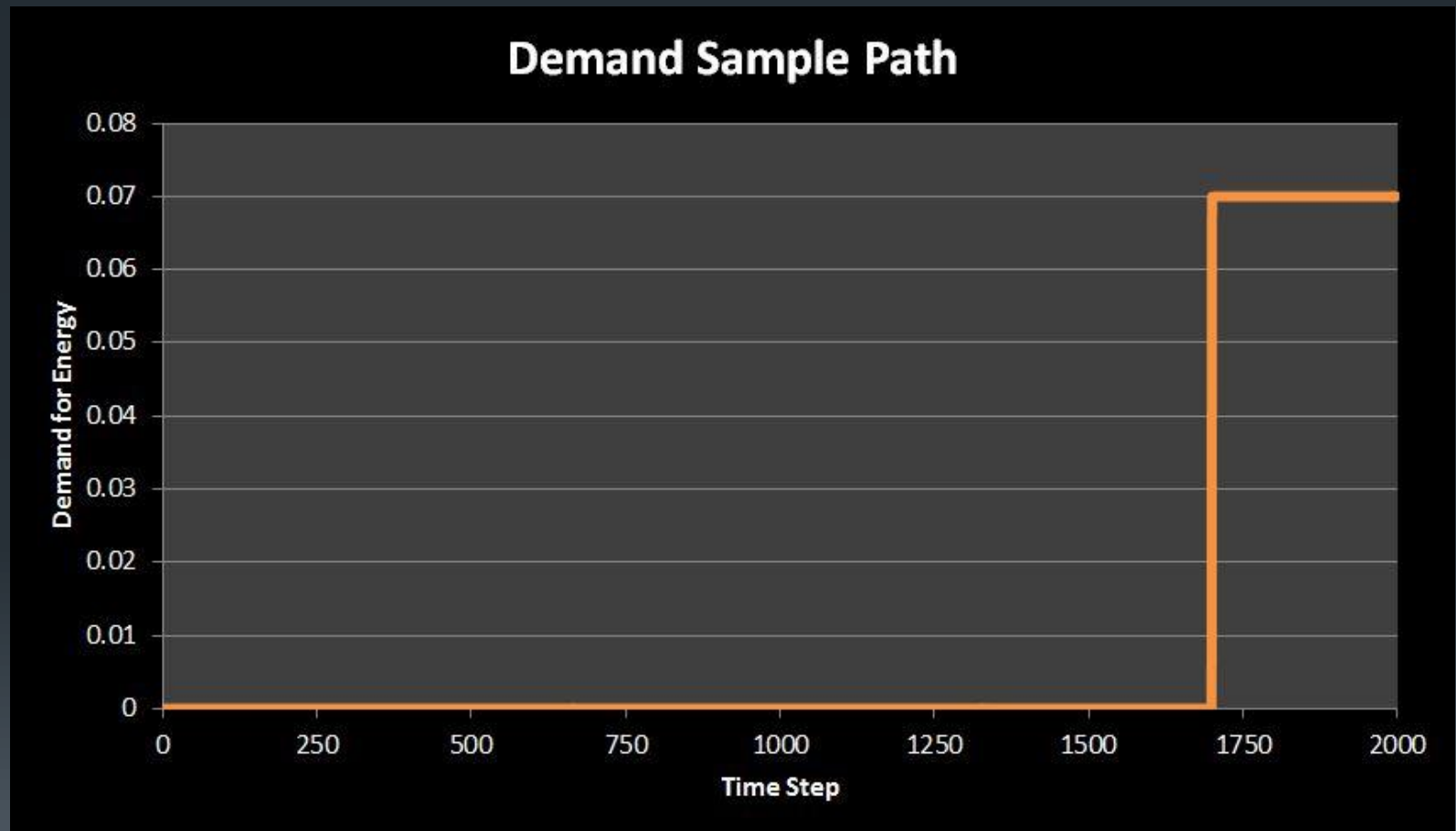




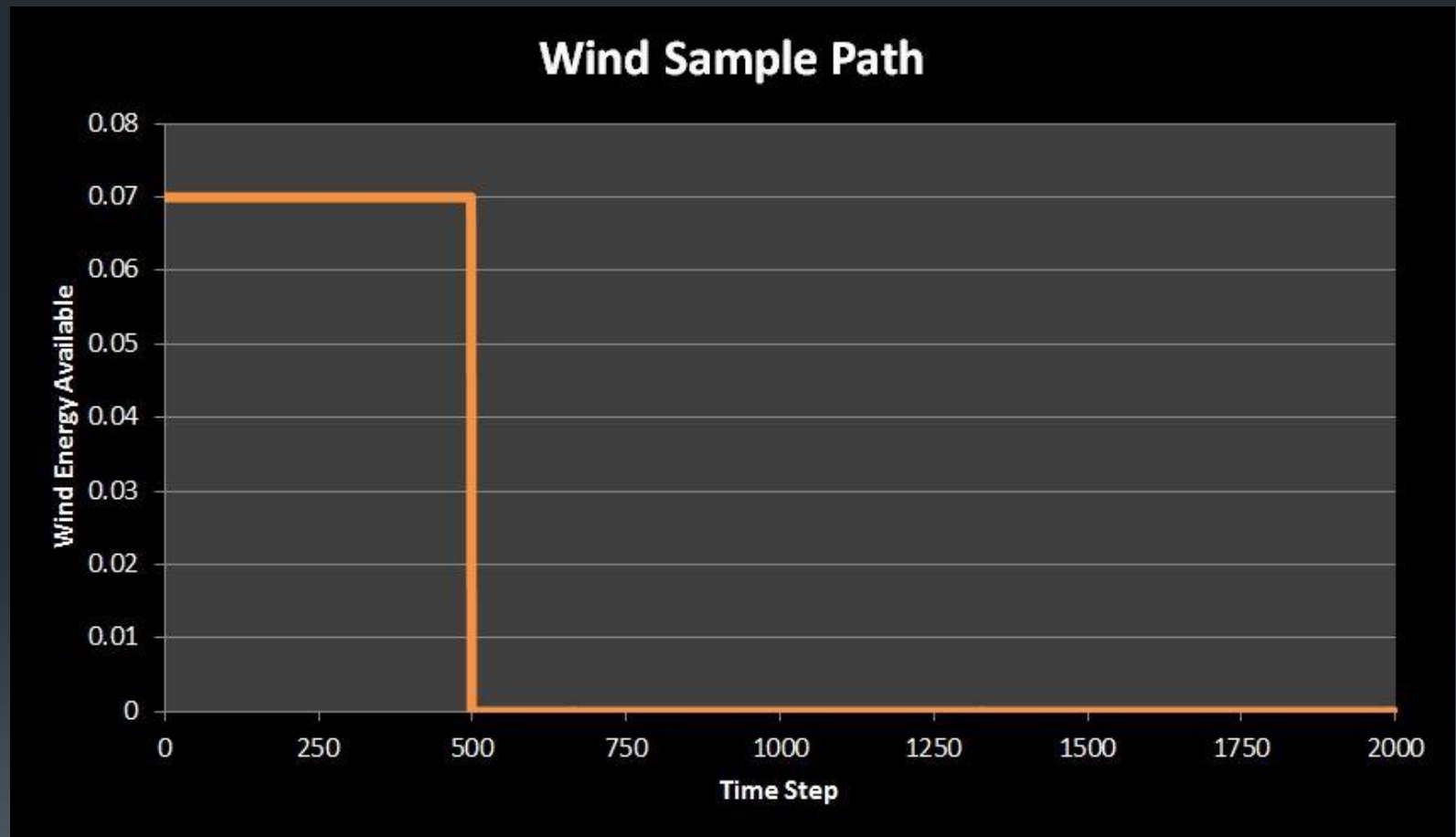
# DATA – Deterministic Parameters

- $R^{max} = 100$
- $R^{min} = 0$
- $R_0 = 0$
- $\eta^c = \eta^d = 0.90$
- $\gamma^c = \gamma^d = 0.10$
  
- **$T = 2000$**

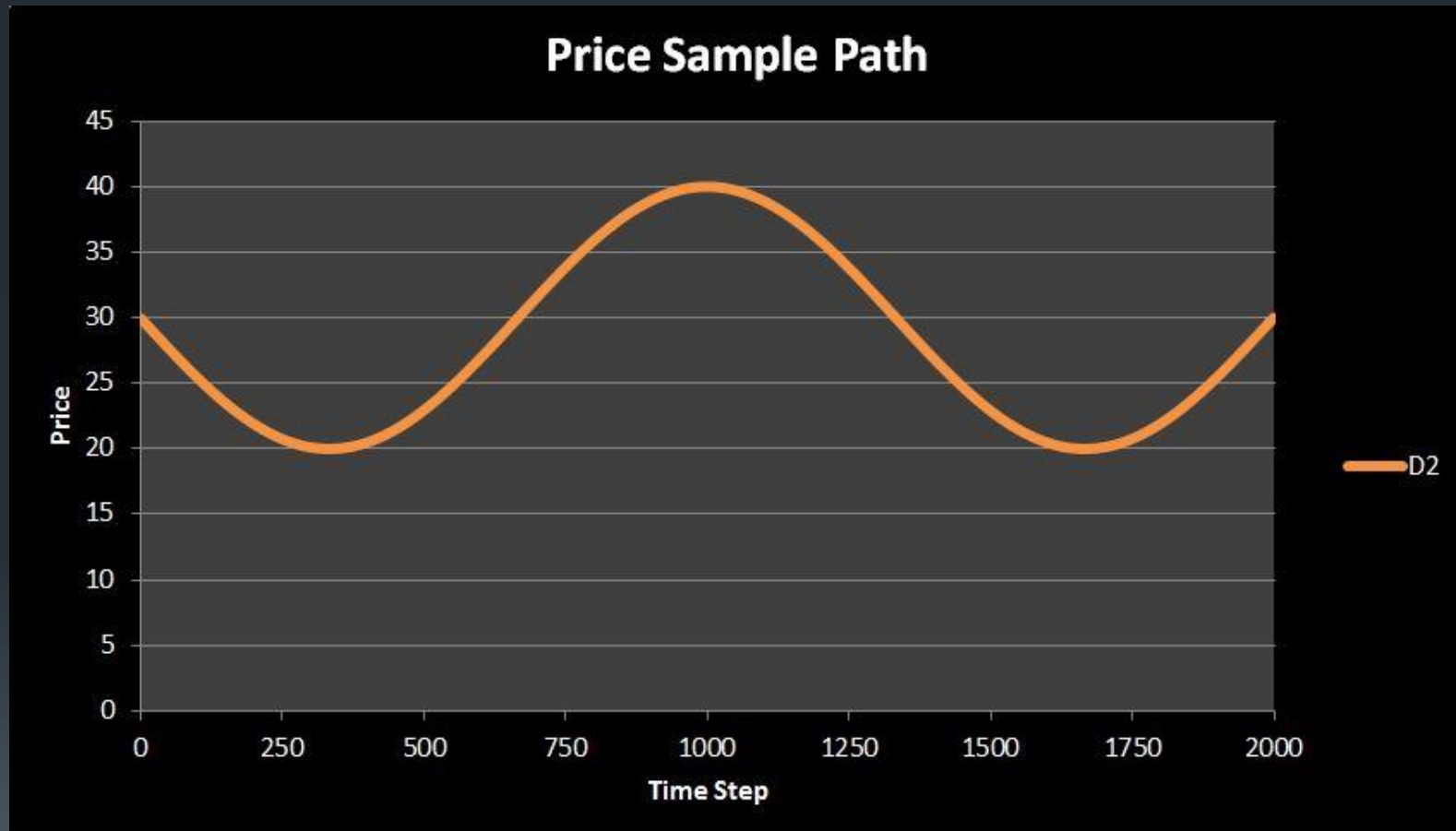
# DATA – Deterministic Problems



# DATA – Deterministic Problems



# DATA – Deterministic Problems

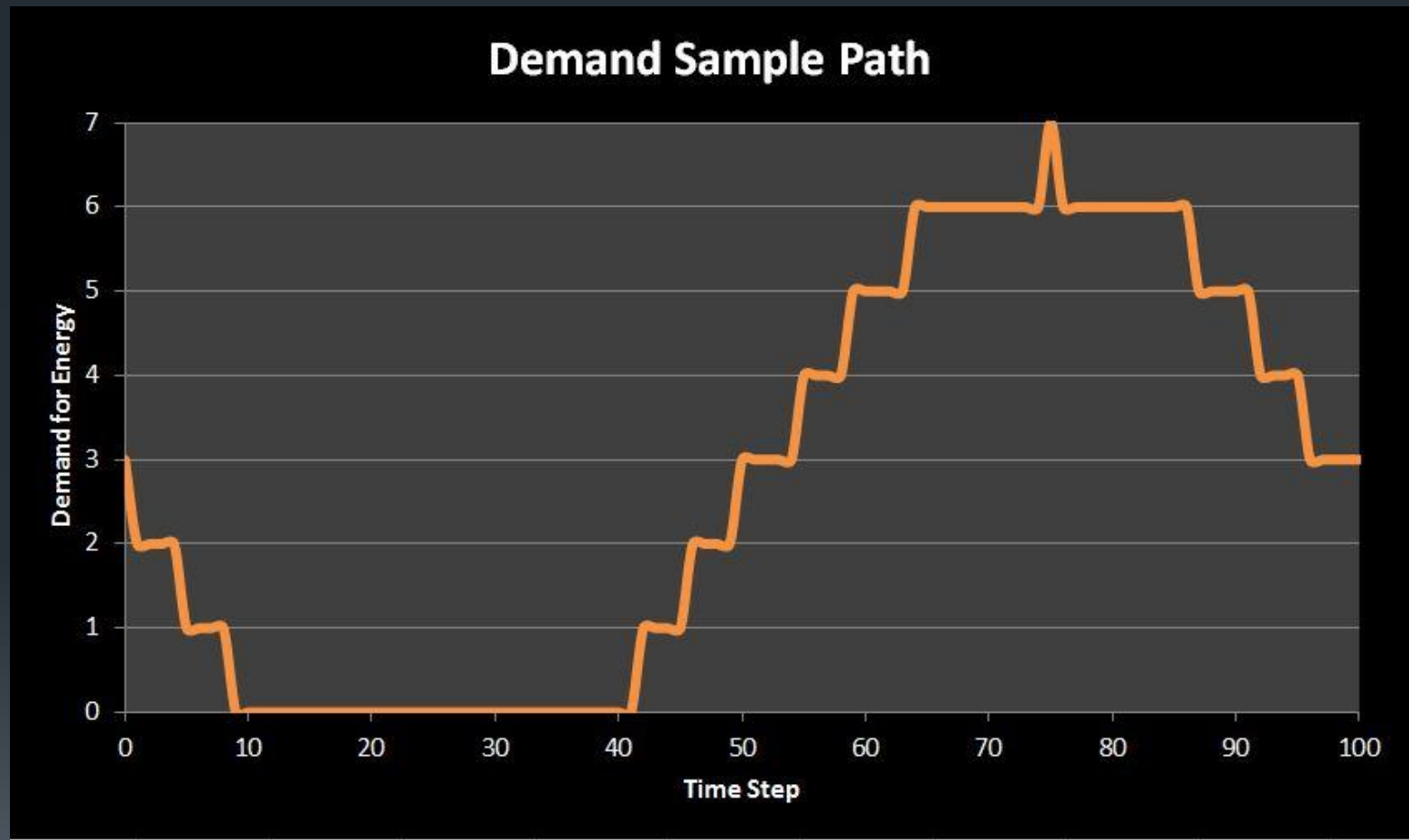




# DATA – Stochastic Parameters

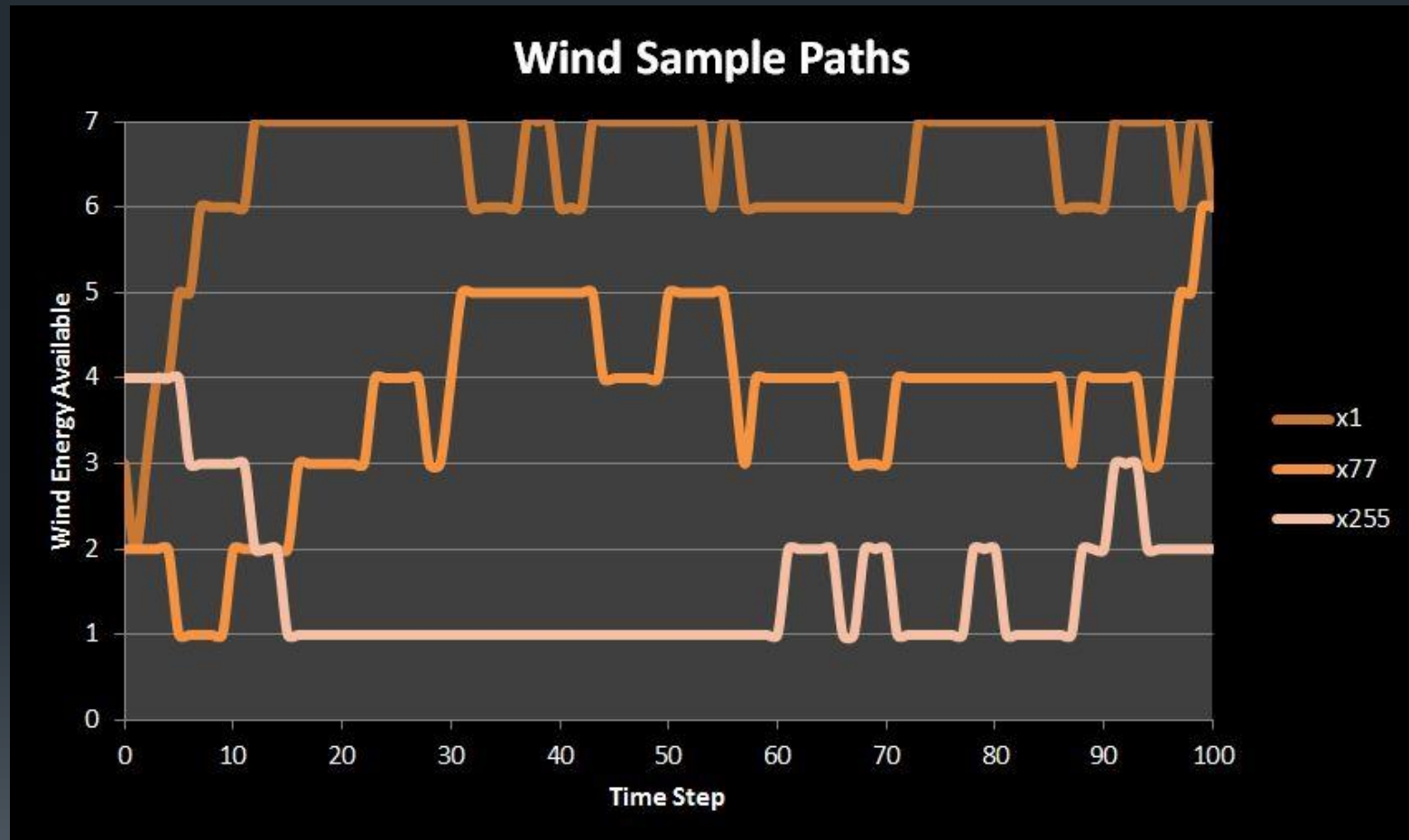
- $R^{max} = 30$
- $R^{min} = 0$
- $R_0 = 25$
- $\eta^c = \eta^d = 1.00$
- $\gamma^c = \gamma^d = 5$
- $T = 100$
- $p^{max} = 70$
- $p^{min} = 30$
- $E^{max} = 7.00$
- $E^{min} = 1.00$

# DATA – Stochastic Problems





# DATA – Stochastic Problems



# DATA – Stochastic Problems



# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration





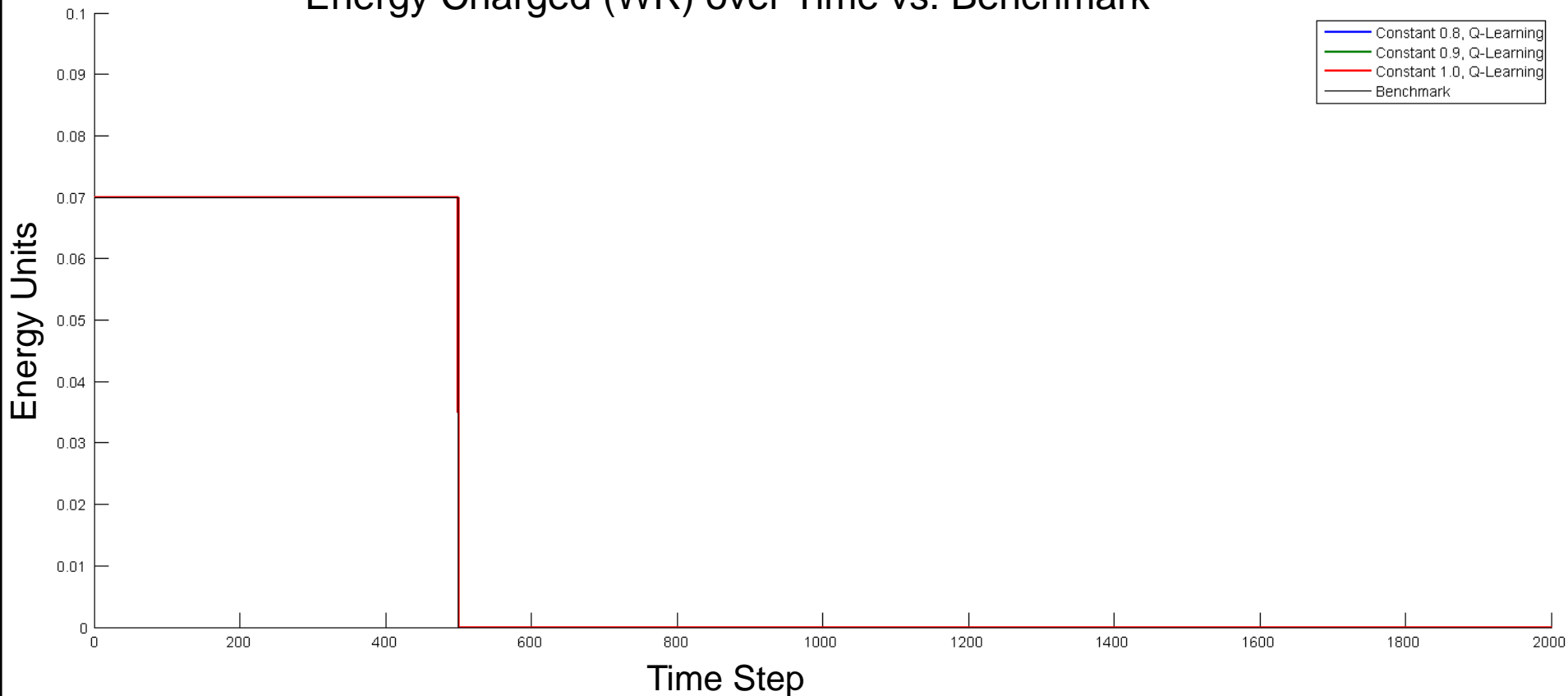
# RESULTS – METRICS

- Action Traces (Deterministic)
- Step Size over Updates
- Stored Energy over Time vs. Benchmark
- Performance over # of Training Iterations

# DETERMINISTIC ACTIONS



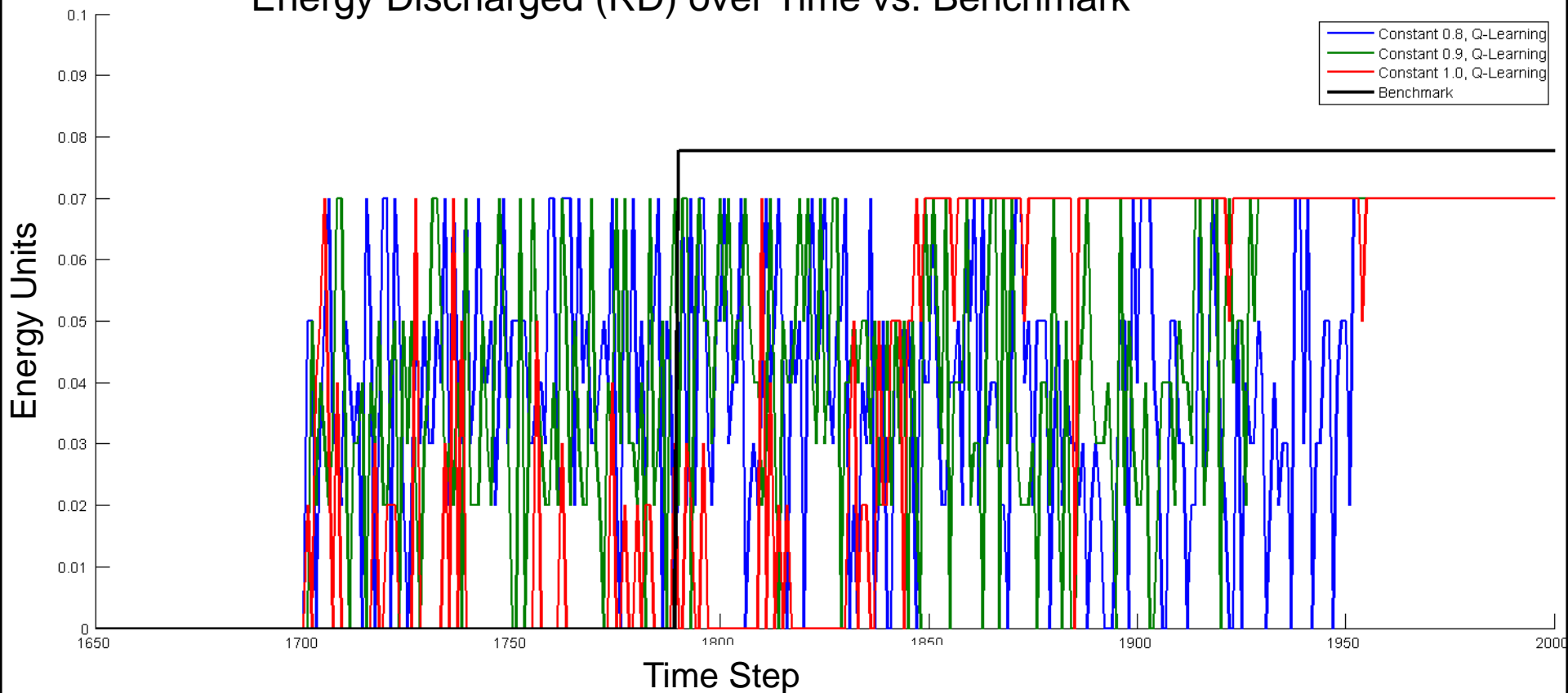
Energy Charged (WR) over Time vs. Benchmark



# DETERMINISTIC ACTIONS



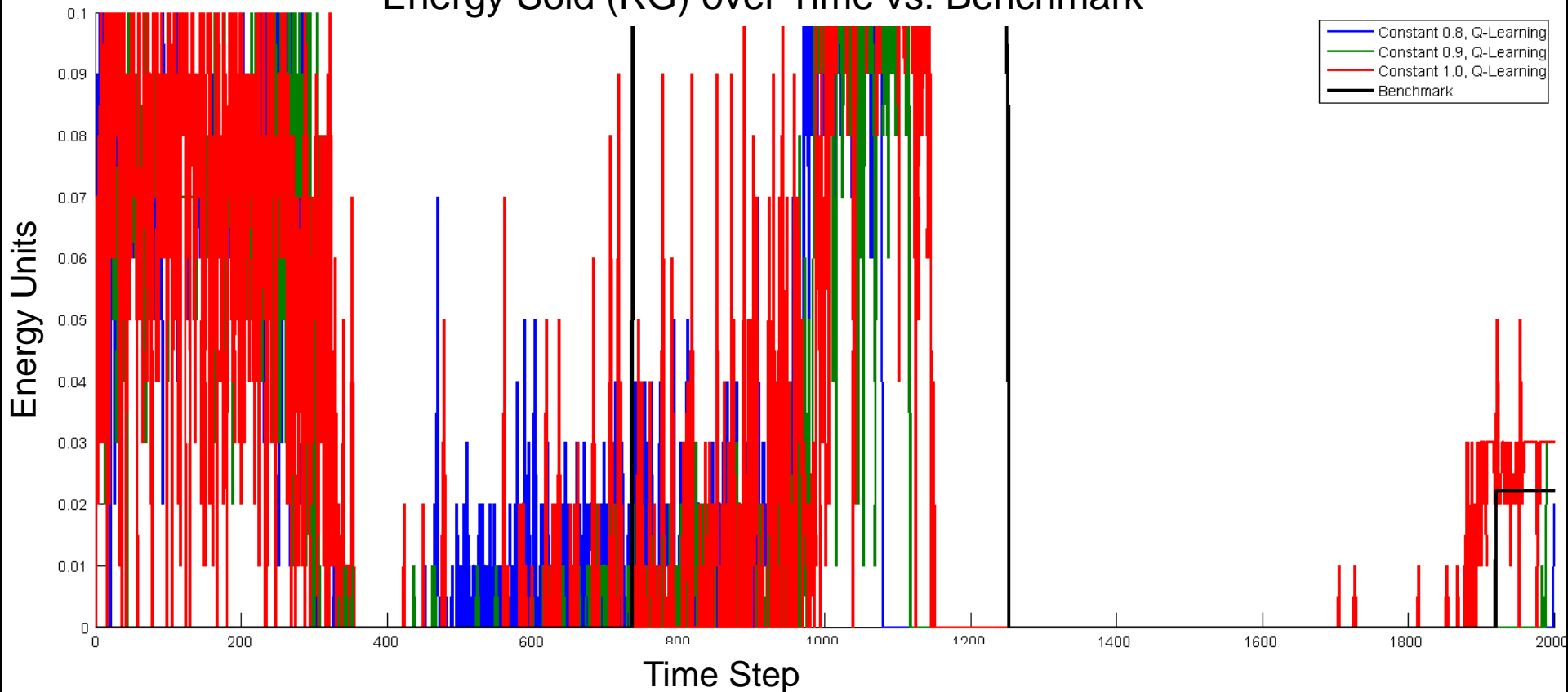
Energy Discharged (RD) over Time vs. Benchmark



# DETERMINISTIC ACTIONS



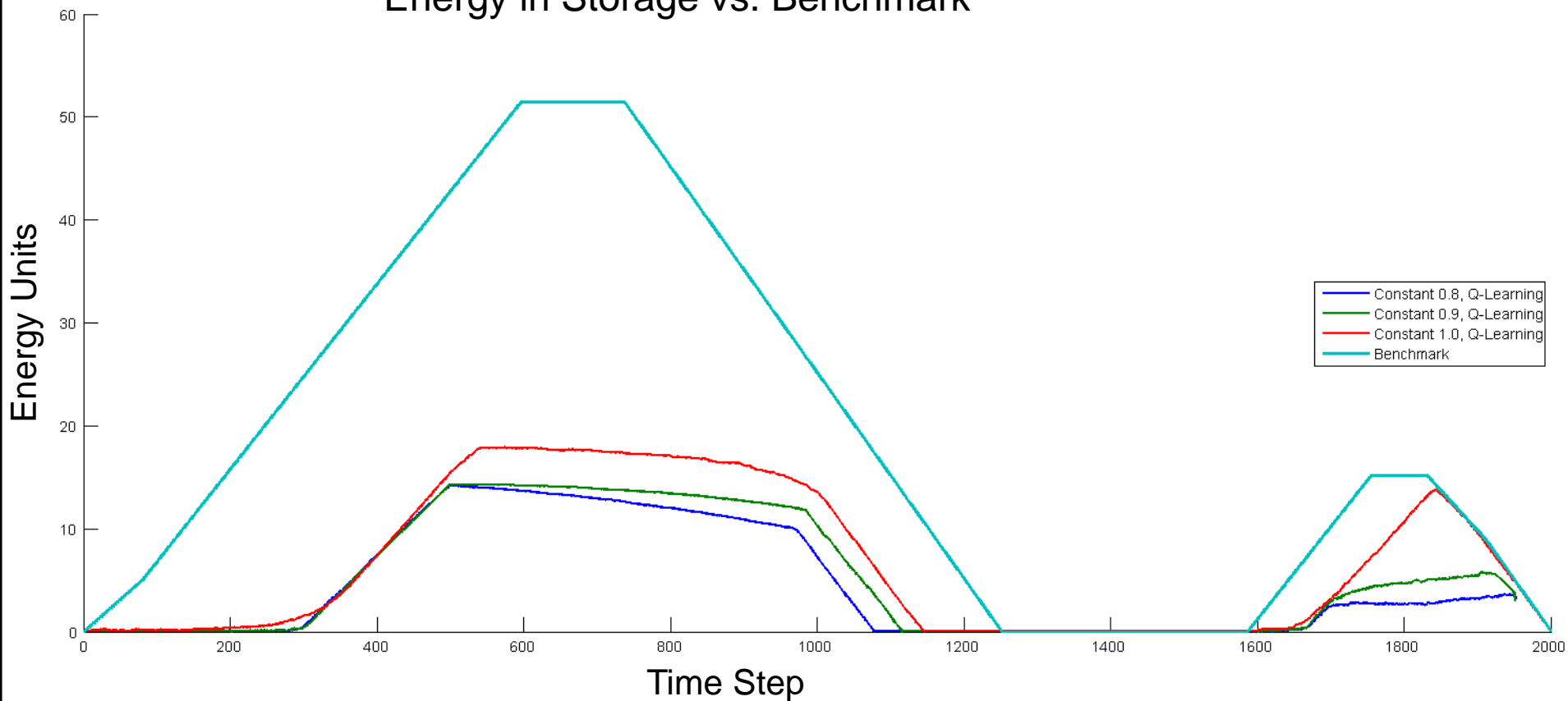
Energy Sold (RG) over Time vs. Benchmark



# DETERMINISTIC STORAGE



Energy in Storage vs. Benchmark







# DETERMINISTIC PERFORMANCE

Performance of Constant Step Sizes, D2





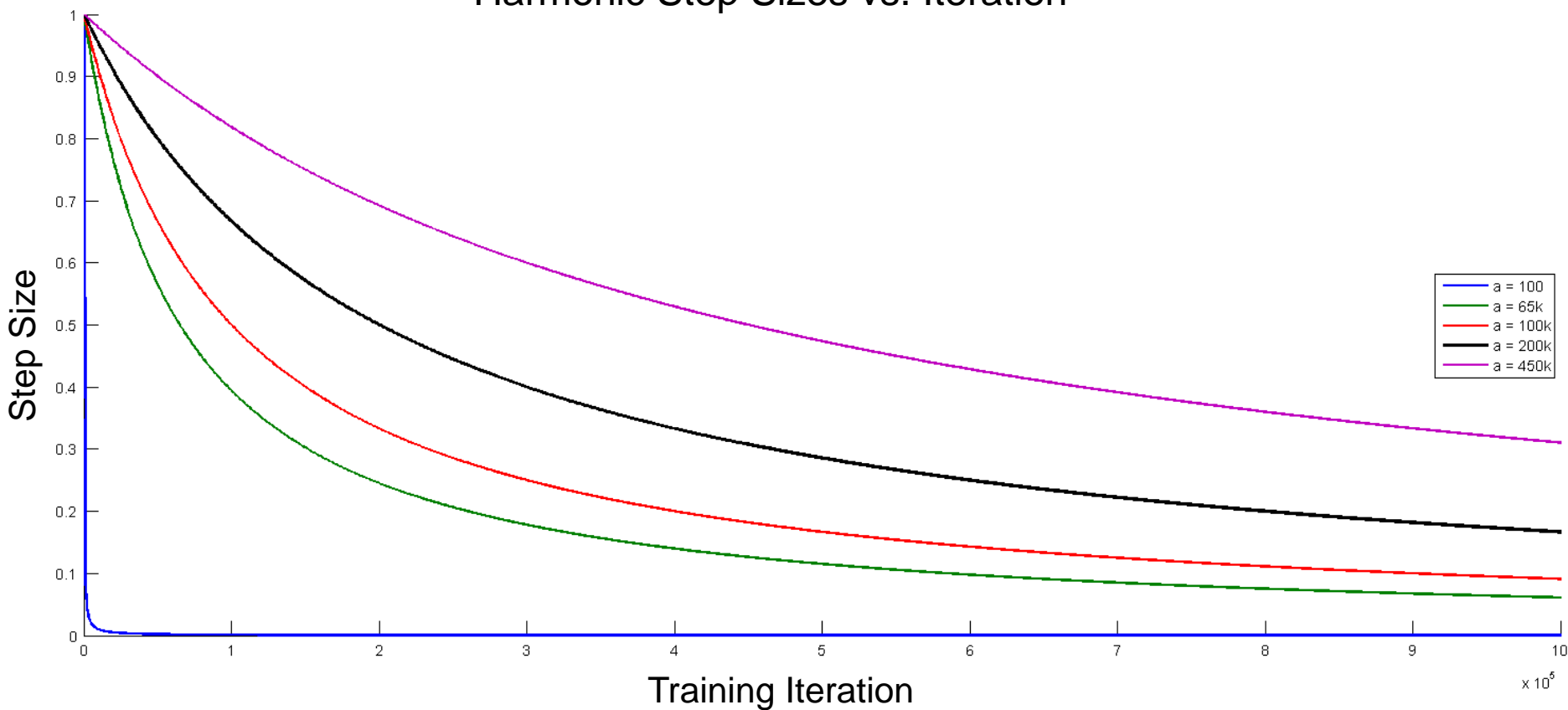
# STEP SIZE TUNING

- Declining Step Sizes
- Tunable parameters
  - Harmonic:  $\frac{a}{a+n}$
  - Ryzhov: Estimator update factor  $\nu$

# HARMONIC STEP SIZES



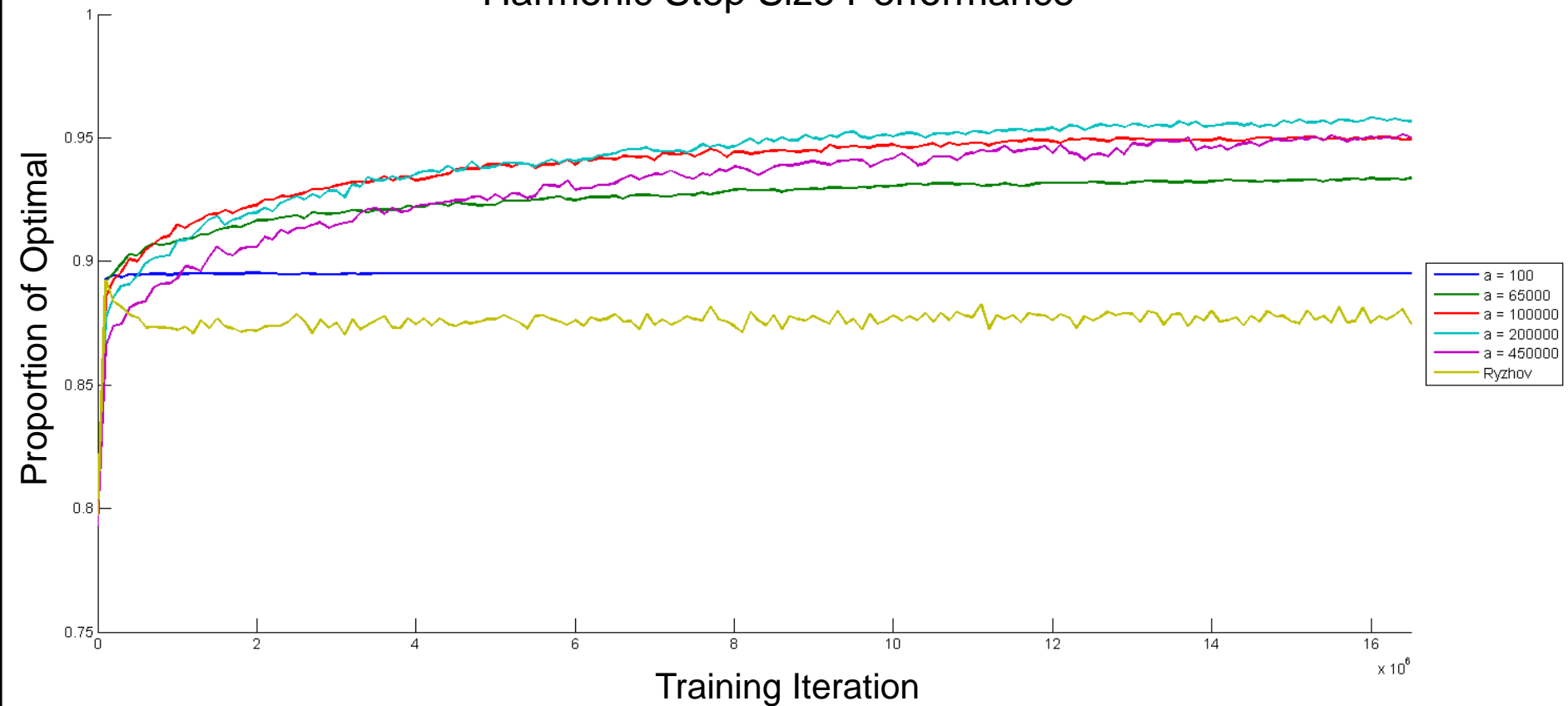
Harmonic Step Sizes vs. Iteration





# HARMONIC PERFORMANCE

Harmonic Step Size Performance



# RYZHOV STEP SIZE

- No-discount formula:

$$\alpha_{n-1} = \frac{(\bar{c}^n)^2}{(\bar{c}^n)^2 + (\bar{\sigma}^n)^2}$$

- Tunable parameter:

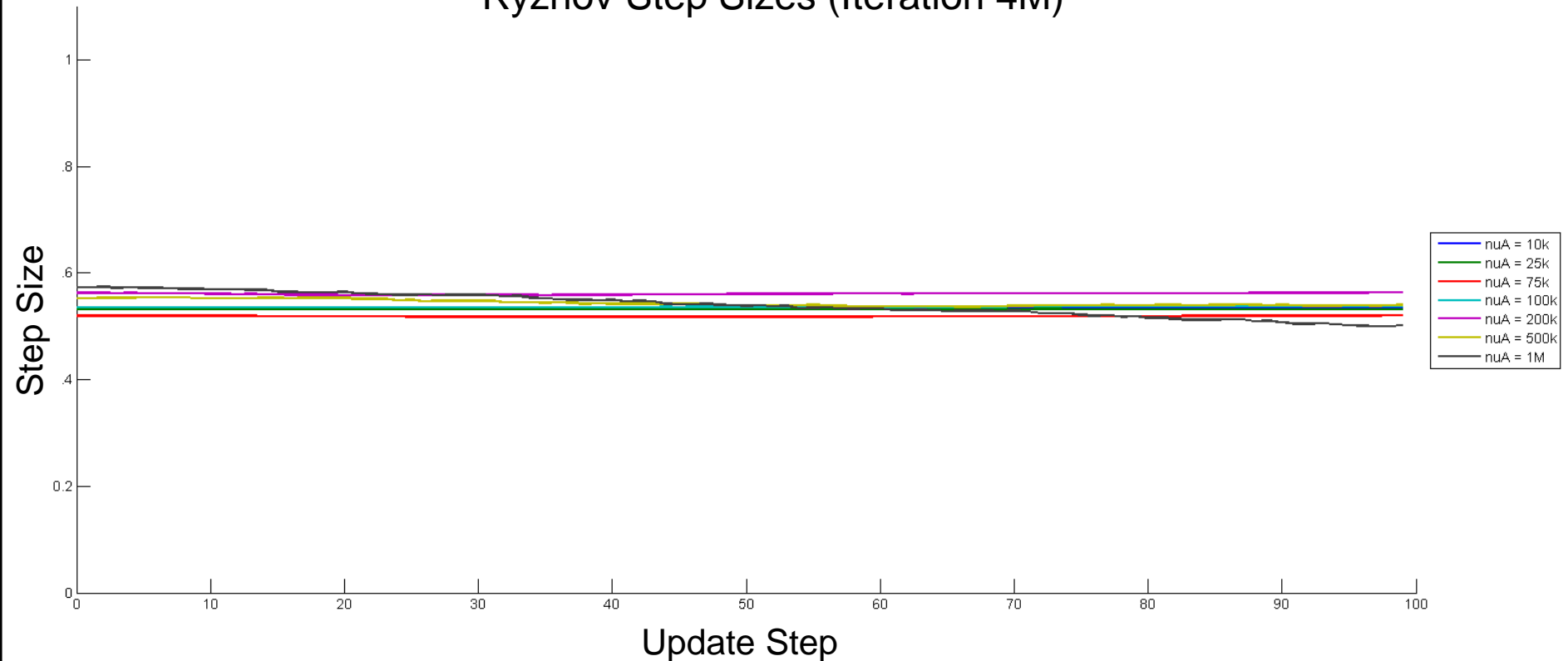
$$\bar{c}^n = (1 - \nu_{n-1})\bar{c}^{n-1} + \nu_{n-1}\hat{c}^n$$

$$(\bar{\sigma}^n)^2 = (1 - \nu_{n-1})(\bar{\sigma}^{n-1})^2 + \nu_{n-1}(\hat{c}^n - \bar{c}^{n-1})^2$$



# RYZHOV STEP SIZES

Ryzhov Step Sizes (Iteration 4M)

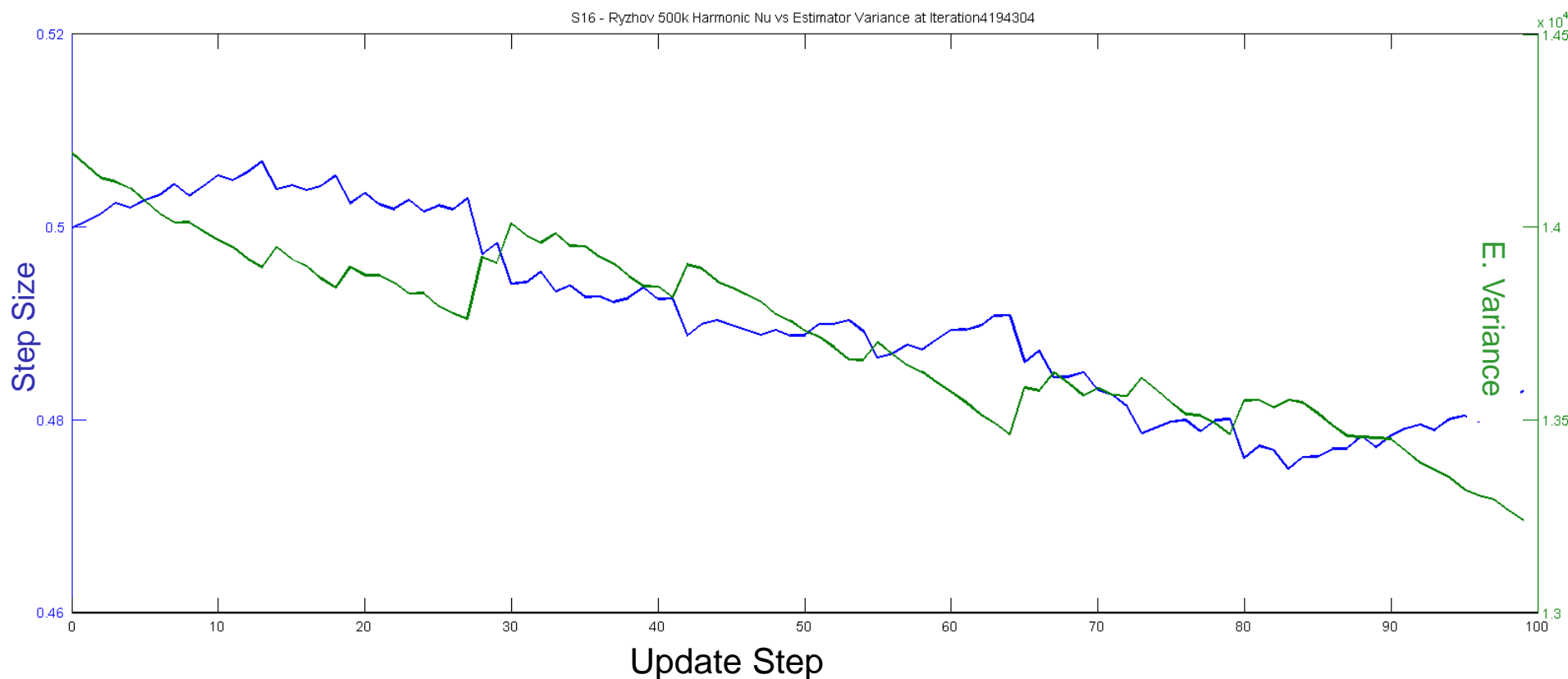




# Ryzhov explanation

- It should even out at a certain constant depending on the variance in the rewards
- For this problem, the rewards are deterministic, so the variance measured is the variance in the different states that we reach/are in

# RYZHOV STEP SIZES vs. ESTIMATOR VARIANCE







# AGGREGATE PARAMETERS

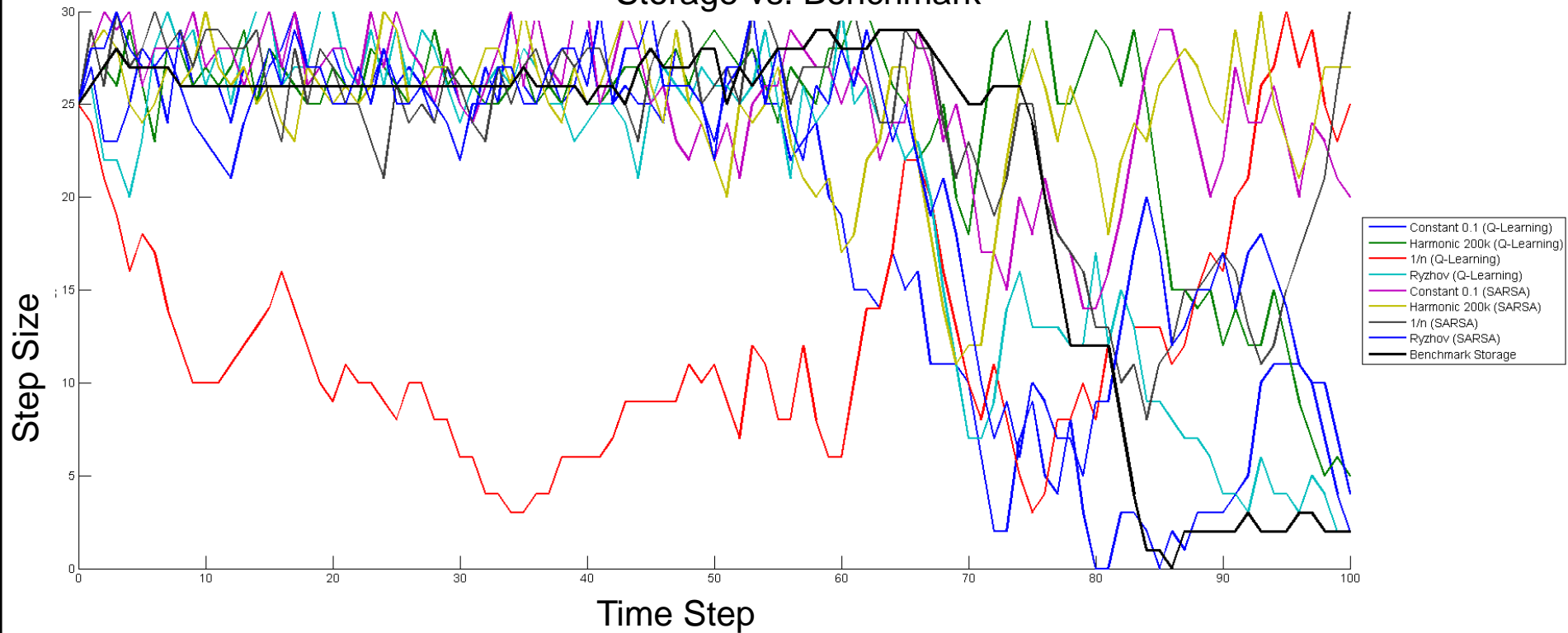
| Label | Resource, $R_t$ |            | Wind, $E_t$ |            |                         | Price, $P_t$ |                  |                         |
|-------|-----------------|------------|-------------|------------|-------------------------|--------------|------------------|-------------------------|
|       | Levels          | $\Delta R$ | Levels      | $\Delta E$ | $\hat{E}_t$             | Levels       | Process          | $\hat{P}_{0,t}$         |
| S1    | 61              | 0.50       | 13          | 0.50       | $\mathcal{U}(-1, 1)$    | 7            | Sinusoidal       | $\mathcal{N}(0, 25^2)$  |
| S2    | 61              | 0.50       | 13          | 0.50       | $\mathcal{N}(0, 0.5^2)$ | 7            | Sinusoidal       | $\mathcal{N}(0, 25^2)$  |
| S3    | 61              | 0.50       | 13          | 0.50       | $\mathcal{N}(0, 1.0^2)$ | 7            | Sinusoidal       | $\mathcal{N}(0, 25^2)$  |
| S4    | 61              | 0.50       | 13          | 0.50       | $\mathcal{N}(0, 1.5^2)$ | 7            | Sinusoidal       | $\mathcal{N}(0, 25^2)$  |
| S5    | 31              | 1.00       | 7           | 1.00       | $\mathcal{U}(-1, 1)$    | 41           | 1st-order + jump | $\mathcal{N}(0, 0.5^2)$ |
| S6    | 31              | 1.00       | 7           | 1.00       | $\mathcal{U}(-1, 1)$    | 41           | 1st-order + jump | $\mathcal{N}(0, 1.0^2)$ |
| S7    | 31              | 1.00       | 7           | 1.00       | $\mathcal{U}(-1, 1)$    | 41           | 1st-order + jump | $\mathcal{N}(0, 2.5^2)$ |
| S8    | 31              | 1.00       | 7           | 1.00       | $\mathcal{U}(-1, 1)$    | 41           | 1st-order + jump | $\mathcal{N}(0, 5.0^2)$ |
| S9    | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 0.5^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 5.0^2)$ |
| S10   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.0^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 5.0^2)$ |
| S11   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.5^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 5.0^2)$ |
| S12   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 2.0^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 5.0^2)$ |
| S13   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 0.5^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 1.0^2)$ |
| S14   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.0^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 1.0^2)$ |
| S15   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.5^2)$ | 41           | 1st-order + jump | $\mathcal{N}(0, 1.0^2)$ |
| S16   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 0.5^2)$ | 41           | 1st-order        | $\mathcal{N}(0, 1.0^2)$ |
| S17   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.0^2)$ | 41           | 1st-order        | $\mathcal{N}(0, 1.0^2)$ |
| S18   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.5^2)$ | 41           | 1st-order        | $\mathcal{N}(0, 1.0^2)$ |
| S19   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 0.5^2)$ | 41           | 1st-order        | $\mathcal{N}(0, 5.0^2)$ |
| S20   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.0^2)$ | 41           | 1st-order        | $\mathcal{N}(0, 5.0^2)$ |
| S21   | 31              | 1.00       | 7           | 1.00       | $\mathcal{N}(0, 1.5^2)$ | 41           | 1st-order        | $\mathcal{N}(0, 5.0^2)$ |

Table 2: Stochastic test problems.

# AGGREGATE STORAGE



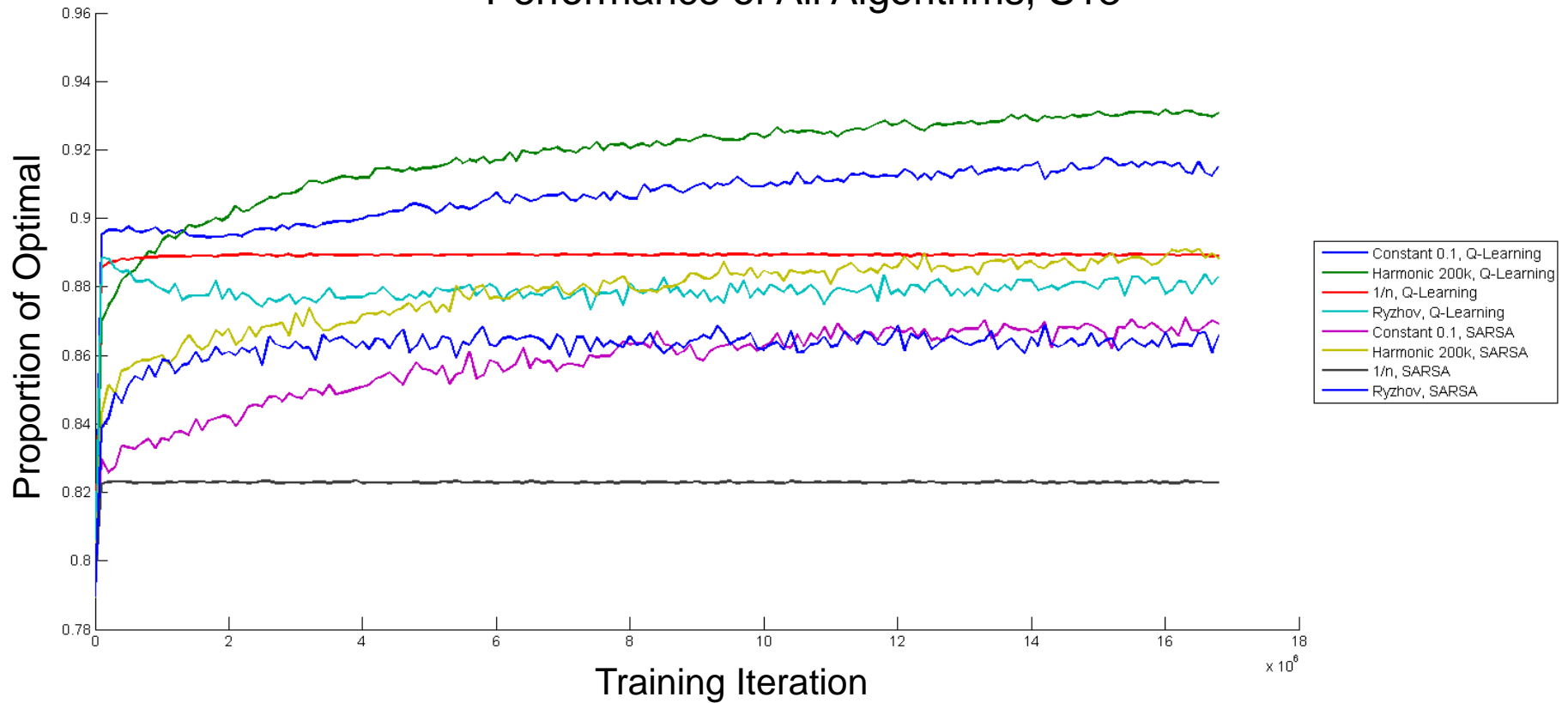
Storage vs. Benchmark





# AGGREGATE PERFORMANCE

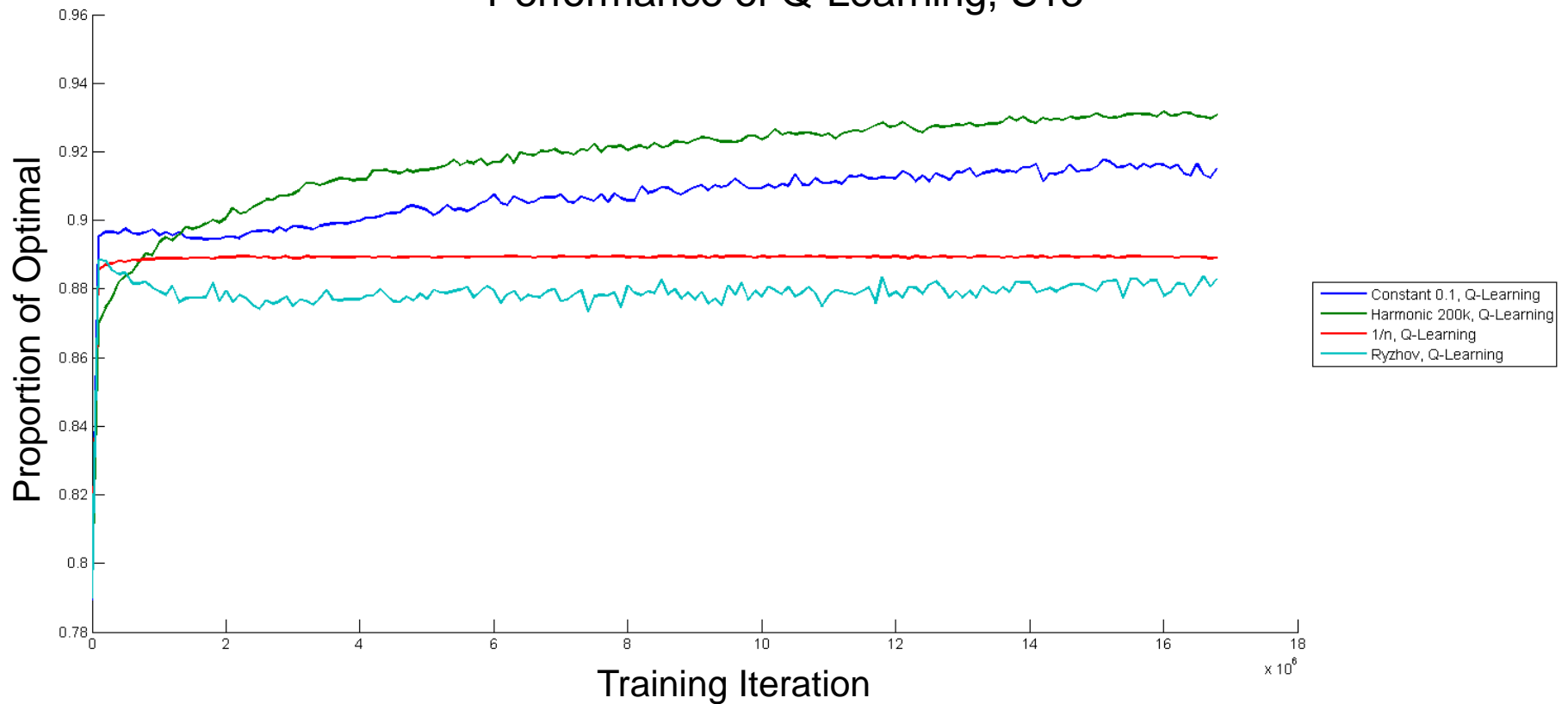
Performance of All Algorithms, S13



# AGGREGATE PERFORMANCE



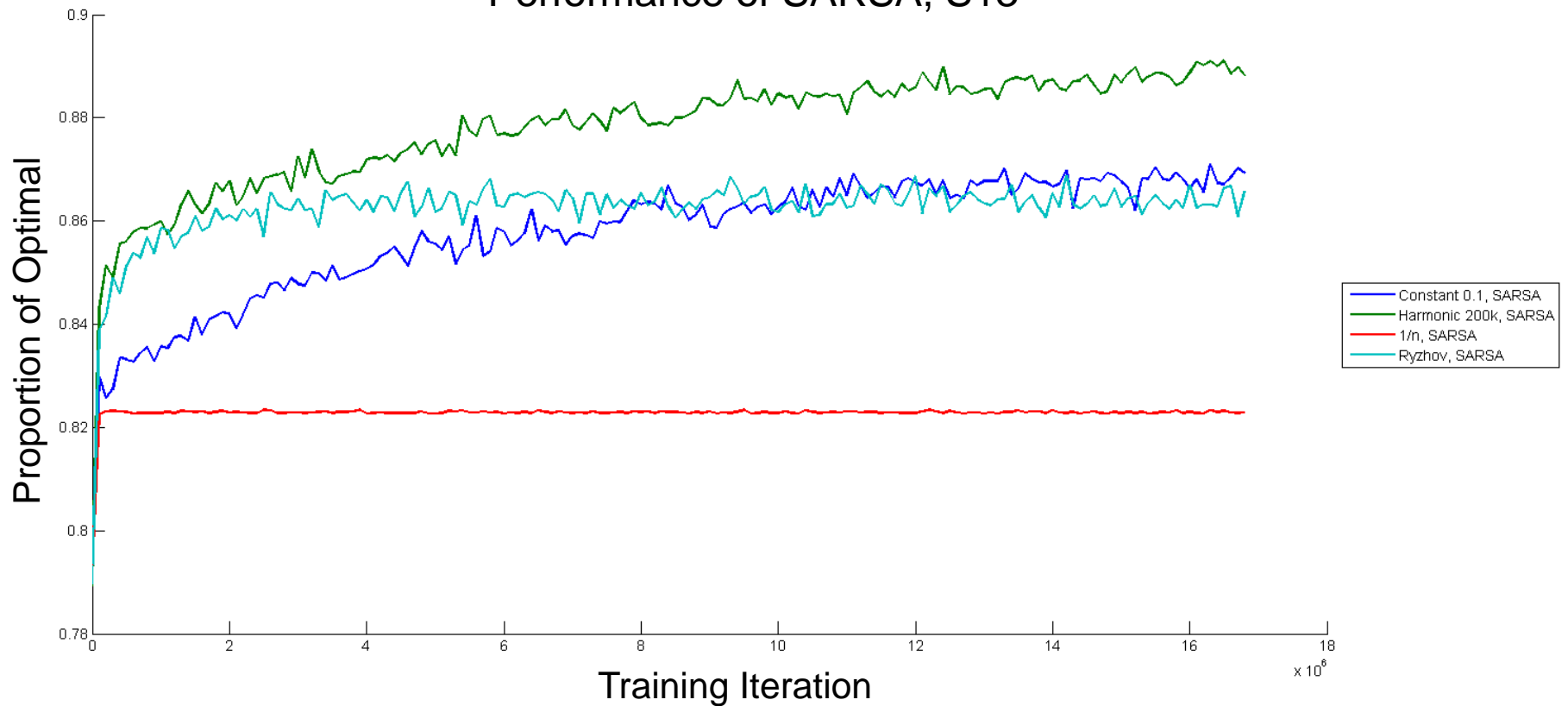
## Performance of Q-Learning, S13



# AGGREGATE PERFORMANCE



Performance of SARSA, S13





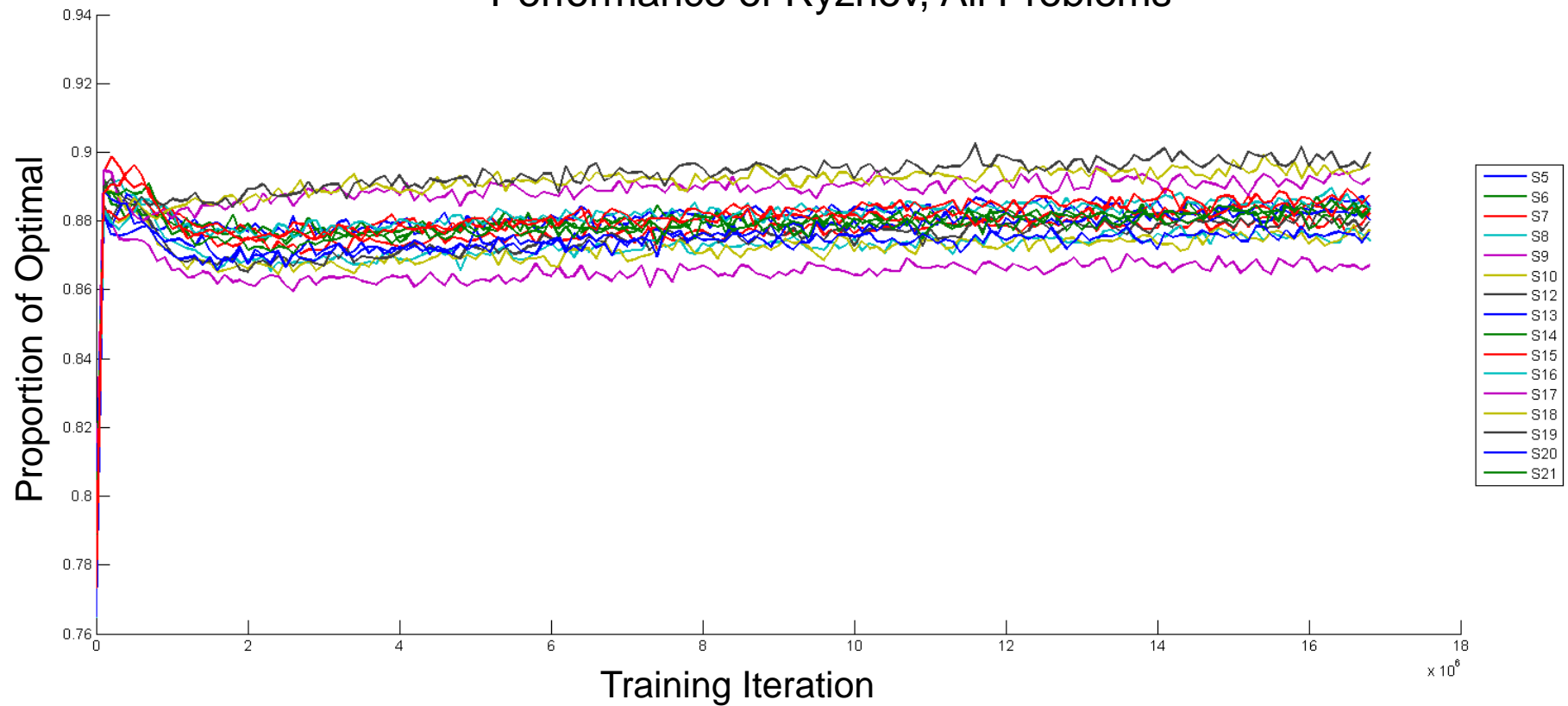
# Explanations

- Ryzhov flattens out very noticeably because the step size is too high, it repeatedly overcompensates and bounces around.
- Harmonic looks like it's still getting better! Need to have it decline more slowly / not go to 0 so quickly. Ryzhov harmonic constant maybe?



# STEP SIZE PERFORMANCE

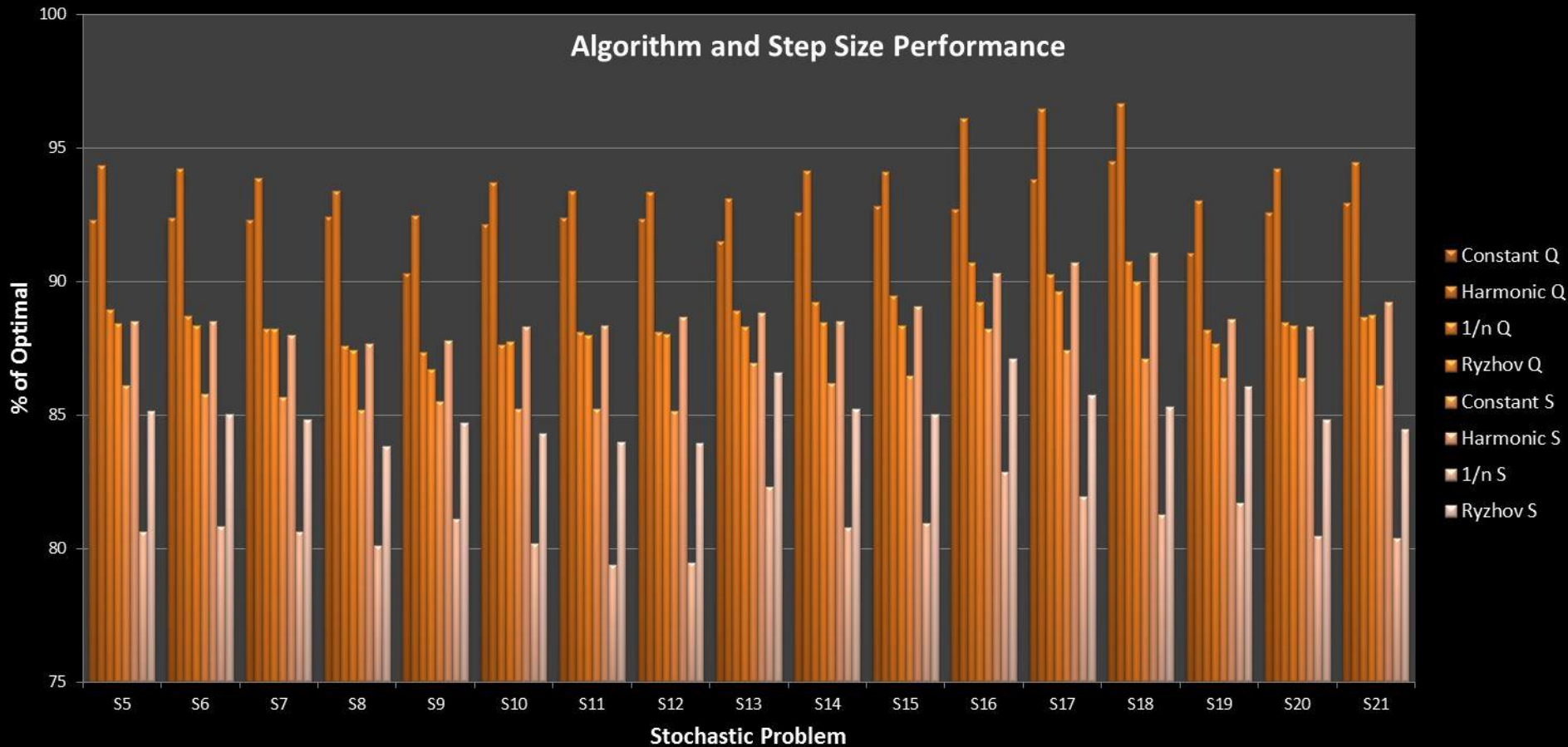
Performance of Ryzhov, All Problems







# AGGREGATE PERFORMANCE



# Overview

- Motivation
- Model
- Algorithms
- Methodology
- Data
- Results
- Further Exploration





# FURTHER EXPLORATION

- Additional renewable energy sources / storage devices
- Finer levels of discretization
- Remove wind usage restriction
- Additional algorithms
  - Actor-Critic
  - Gradient Descent (Linear/Non-Linear VFAs)



# Questions?