



Glad Hobo Express

Friday, June 9

13532385396179 precursors

One of the nice things about having James Davis' counterexample to Conway's conjecture is that it leads directly to other counterexamples (i.e., numbers that evolve into it). For example: $13^{5323^8} \cdot 5396179$, $13^{53238^5} \cdot 396179$, etc. Then one finds precursors of these numbers, and so on. Will this process eventually end? Is the total number of precursors, precursors of precursors, precursors of precursors, etc., finite?

Robert Gerbicz has kindly calculated 58 factorizations (13532385396179 plus 57 primary precursors, sorted and indexed here by number size; additionally, I show the <number of decimal digits>:

0.	$13^{53^2} \cdot 3853 \cdot 96179$	<14>
1.	$13^{5323^8} \cdot 5396179$	<38>
2.	$13^{53^{23}} \cdot 853 \cdot 96179$	<49>
3.	$13^{53^{23}} \cdot 853 \cdot 96179$	<69>
4.	$13^{53^{23}} \cdot 8^5 \cdot 396179$	<77>
5.	$13^{53^{23}} \cdot 8^5 \cdot 396179$	<77>
6.	$13^{53^{23}} \cdot 8^5 \cdot 3^9 \cdot 61 \cdot 79$	<90>

perp



Hans Havermann

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7.	$13^{53} \cdot 23^8 \cdot 53^9 \cdot 617^9$	<111>
8.	$13^{53} \cdot 23^8 \cdot 53^9 \cdot 61^79$	<227>
9.	$13^{53} \cdot 23^8 \cdot 53^9 \cdot 6179$	<238>
10.	$13^{53} \cdot 238 \cdot 5396179$	<419>
11.	$13^{532} \cdot 3853 \cdot 96179$	<602>
12.	$13^{53} \cdot 23^8 \cdot 53^9 \cdot 6179$	<1226>
13.	$13^{53} \cdot 23^8 \cdot 53^9 \cdot 6179$	<1729>
14.	$13^{5323} \cdot 853 \cdot 96179$	<3185>
15.	$13^{5323} \cdot 853 \cdot 96179$	<5938>
16.	$13^{53} \cdot 23^8 \cdot 539 \cdot 6179$	<11691>
17.	$13^{53} \cdot 23^8 \cdot 539 \cdot 617^9$	<11712>
18.	$13^{53} \cdot 23^8 \cdot 539 \cdot 61^79$	<11828>
19.	$13^{5323} \cdot 8539 \cdot 6179$	<24298>
20.	$13^{53} \cdot 23^8 \cdot 539 \cdot 6179$	<24333>
21.	$13^{53} \cdot 23^8 \cdot 539 \cdot 6179$	<24353>
22.	$13^{5323} \cdot 8539 \cdot 6179$	<30222>
23.	$13^{53} \cdot 23853 \cdot 96179$	<41136>
24.	$13^{53238539} \cdot 6179$	<47742>
25.	$13^{53238} \cdot 53 \cdot 96179$	<59311>
26.	$13^{53238} \cdot 5396179$	<59311>
27.	$13^{53238} \cdot 53^9 \cdot 6179$	<59324>
28.	$13^{53238} \cdot 53^9 \cdot 617^9$	<59345>
29.	$13^{53238} \cdot 53^9 \cdot 61^79$	<59461>
30.	$13^{53238} \cdot 53^9 \cdot 6179$	<59472>
31.	$13^{53238} \cdot 53^9 \cdot 6179$	<60964>
32.	$13^{53} \cdot 23^8 \cdot 5396 \cdot 179$	<116348>
33.	$13^{53} \cdot 23^8 \cdot 53^9 \cdot 6179$	<165910>

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34.	$13^{53238*53^96179}$	<225144>
35.	$13^{53^23*853^96179}$	<281937>
36.	$13^{53*23*853^96179}$	<281957>
37.	$13^{5323*853^96179}$	<287826>
38.	$13^{53^2*3853^96179}$	<344884>
39.	$13^{532*3853^96179}$	<345472>
40.	$13^{53^238539*61^79}$	<411312>
41.	$13^{53^238539*61^79}$	<411334>
42.	$13^{53^238539*61^79}$	<411450>
43.	$13^{5323853^96179}$	<646923>
44.	$13^{53*23^853961*79}$	<1162924>
45.	$13^{53^2385396*179}$	<4113085>
46.	$13^{5323853*96179}$	<5930476>
47.	$13^{53^23853961*79}$	<41130813>
48.	$13^{53238539*61^79}$	<59304721>
49.	$13^{53238539*61^79}$	<59304742>
50.	$13^{53238539*61^79}$	<59304858>
51.	$13^{53*23^85396179}$	<116286414>
52.	$13^{5323^85396179}$	<318199526>
53.	$13^{532385396*179}$	<593047175>
54.	$13^{532385396*17^9}$	<593047184>
55.	$13^{53^2385396179}$	<4113081073>
56.	$13^{5323853961*79}$	<5930471731>
57.	$13^{532385396179}$	<593047172939>

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I have a [work-in-progress version](#) of this table that also shows secondary precursor counts.

Consider $13^{532385396179}$. Take enough of its initial decimal digits to make a prime (*and*

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the next digit isn't zero; 68971066936841703995076128866117893410448319579 will do). Raise this to the power of the rest of the digits, thus creating a new (even larger) precursor. Repeat.

The number of initial decimal digits of $13^{532385396179}$ that may be used as primes in the above argument is 47, 50, 449, 4341, 5798, ... The sequence is necessarily finite but will we ever know for certain when it is full?

Keep an eye out for new comments in Sloane's [A195264](#).

Posted by [Hans Havermann](#) at [10:34 PM](#)



1 comment:



[James Davis](#) June 10, 2017 at 1:51 AM

Really interesting point. So there may (should?) be infinite numbers that map to the fixed point. I wonder if the density of those could be non-zero. Seems like it should go to zero eventually...

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