

Wolfdieter Lang, Nov 30 2007
 A134832

$a(n,k)=C(n,k)$ tabl head (triangle) for A134832 (nr. of circular permutations of $\{1,2,\dots,n\}$ with exactly k successor pairs $(i,i+1)$).
 Note that due to cyclicity also $(n,1)$ is a successor pair.

$n \setminus k$	0	1	2	3	4	5	6	7	8	9 ...
0	1	0	0	0	0	0	0	0	0	0
1	0	1	0	0	0	0	0	0	0	0
2	0	0	1	0	0	0	0	0	0	0
3	1	0	0	1	0	0	0	0	0	0
4	1	4	0	0	1	0	0	0	0	0
5	8	5	10	0	0	1	0	0	0	0
6	36	48	15	20	0	0	1	0	0	0
7	229	252	168	35	35	0	0	1	0	0
8	1625	1832	1008	448	70	56	0	0	1	0
9	13208	14625	8244	3024	1008	126	84	0	0	1
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First ($k=0$) column: A000757= $[1,0,0,1,1,8,36,229,1625,13208,120288,1214673,13469897,\dots]$,
 circular permutations without any successor pair.

Row sums give $(n-1)! = A000142(n-1)$, $n \geq 1$.

Alternating row sums give: A134833 = $[1,-1,1,0,-2,12,-16,144,368,4768,\dots]$.

Because $C(n,k)=\text{binomial}(n,k)*C(n-k,0)$, $k \geq 1$, this is a Sheffer triangle of the Appell type:
 $((1-\ln(1-x))/e^x, x)$. See the e.g.f. of the first column ($k=0$) sequence A000757.
I.e. the e.g.f. for column nr. k is $((1-\ln(1-x))/e^x)*(x^k)/k!$, $k \geq 0$, hence
 $a(n,k)=\text{binomial}(n,k)*a(n-k,0)$, $n \geq 0$.

The a-sequence for Appel type Sheffer triangles has always (e.)g.f 1.
The z-sequence for such triangles is always $(1+1/g(x))/x$ if g is the e.g.f. of the first ($k=0$) column.

e.o.f.