OEIS A002494

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ABSTRACT. Sequence A002494 counts unlabeled simple graphs on n nodes without isolated nodes, which means the degree of each node is at least 1. Simple means: no loops (edges that connect a node with itself), no multiedges.

1. Introduction

Sequence [1, A002494] counts 1, 2, 7, 23,... simple graphs on n = 2, 3, ... nodes where the degree of each node is ≥ 1 . The subset of connected graphs is [1, A001349], which implies the subset of graphs with more than one component is [1, A327075].

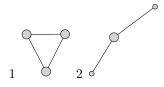
If the nodes are labeled (graphs counted with the multiplicity of n!/|Aut(G)|), sequence A006129 ensues.

Graphs with more than one component are placed in frames. The nodes are symbolized by grey circles with a diameter growing with the degree (just as an aid to visualize the symmetries).

2. 1 Graph on 2 nodes



3. 2 Graphs on 3 nodes

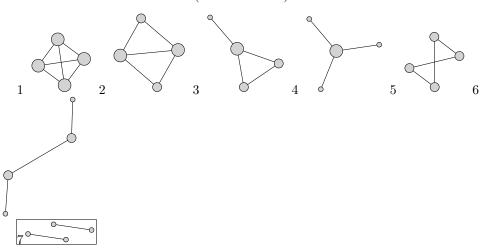


Date: November 21, 2023.

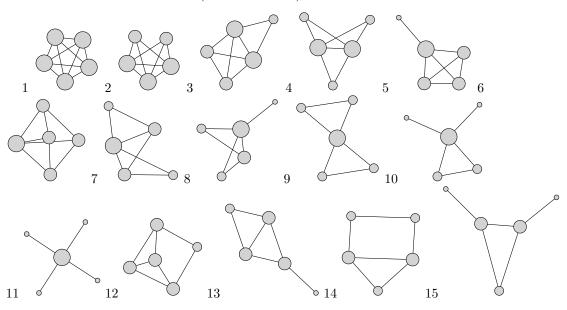
 $2020\ Mathematics\ Subject\ Classification.\ Primary\ 05C30;\ Secondary\ 05C75,\ 81Q15.$

Key words and phrases. Simple Unlabeled Graphs.

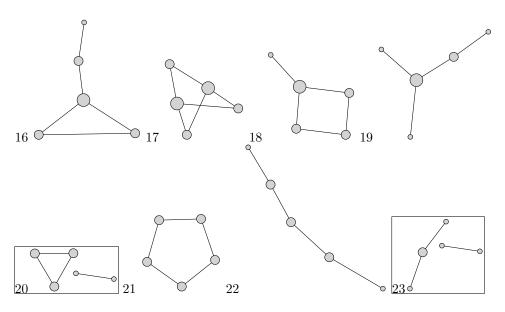
4. 7 Graphs (6 connected) on 4 nodes



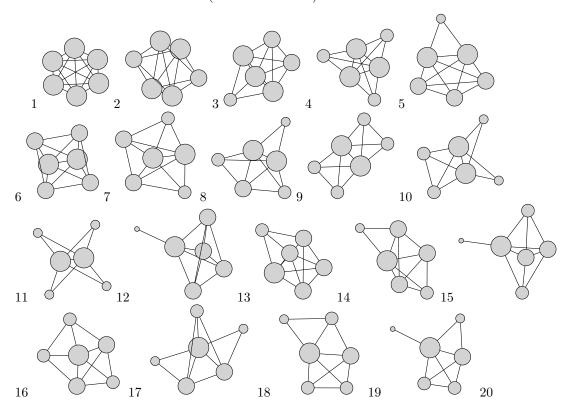
5. 23 graphs (21 connected) on 5 nodes

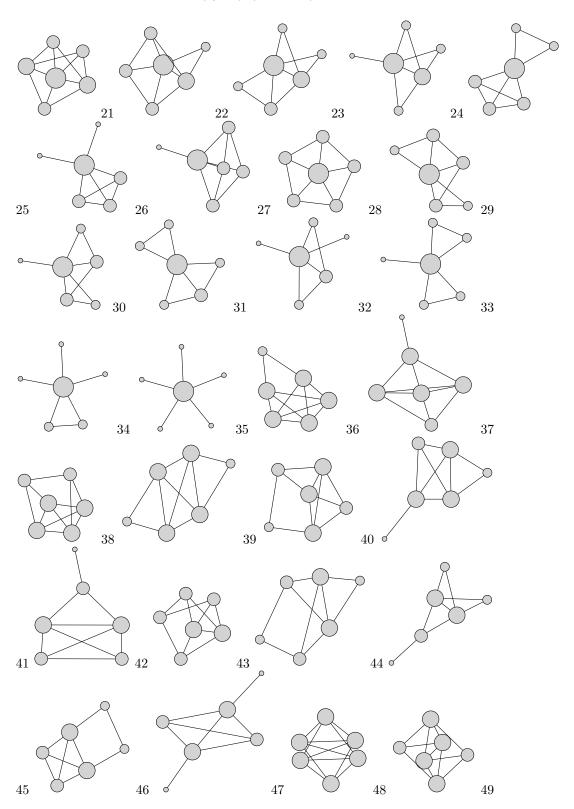


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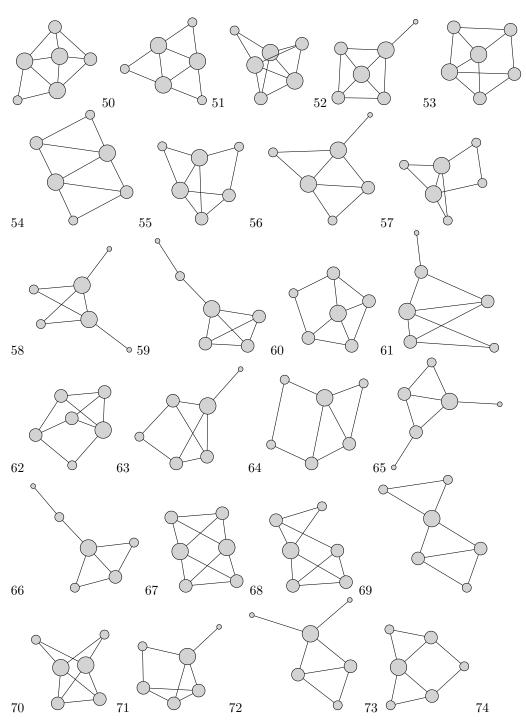


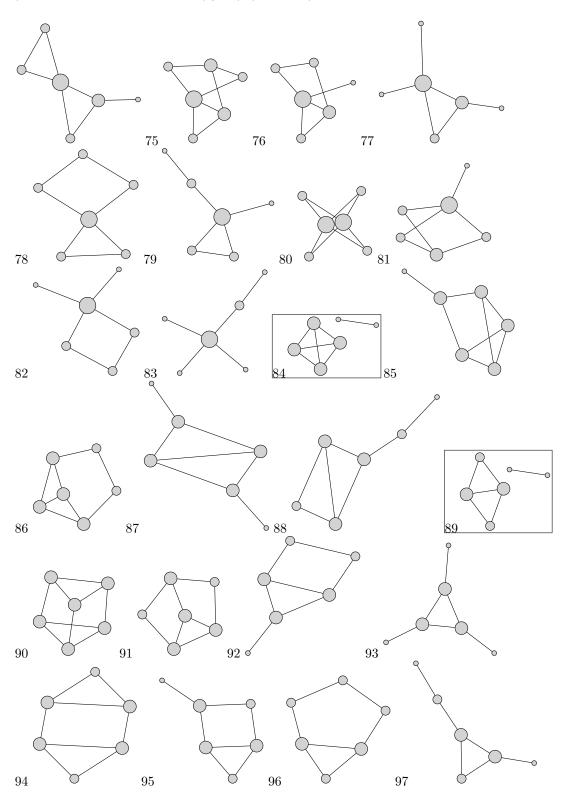
6. 122 graphs (112 connected) on 6 nodes



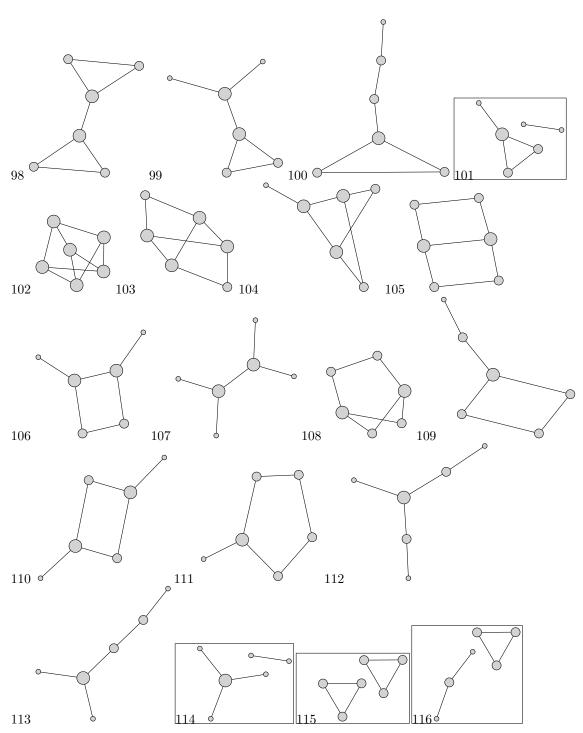


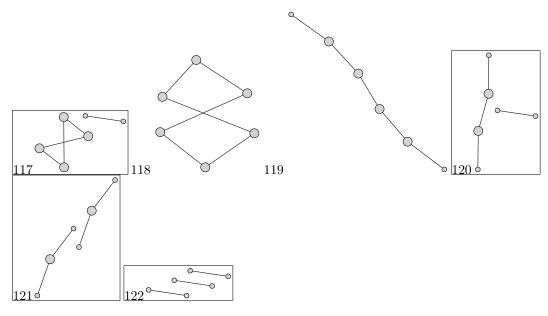
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References

1. O. E. I. S. Foundation Inc., The On-Line Encyclopedia Of Integer Sequences, (2023), https://oeis.org/. MR 3822822

 $\mathit{URL} : \verb|https://www.mpia-hd.mpg.de/homes/mathar||$

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