The simple two-dimensional parameterisation for Flux Footprint Predictions FFP

N. Kljun, P. Calanca, M. W. Rotach, and H. P. Schmid

Responses to Referee #1

The manuscript is very well written, and provides a focused and well justified description of an improved approach for footprint modeling.

Many thanks.

I have several minor comments (listed below), regarding reference to recent publications that have used footprint models, and regarding the order and flow at which the formulation is described. I salute the fact that a link to the code is provided with the manuscript. I think this should be moved to an earlier point in the paper (perhaps just after the introduction) and not hidden past all the appendices, but this is just my preference and I will accept the authors preference for the placement of the "code availability" section. However, I checked the website listed and the source code is not provided there. There is only a link to an online version of the model, which is a far cry from the code itself. I assume that a link to the code will be posted when the paper is accepted, but the editor should verify this before the final posting of the manuscript.

Indeed, we await the acceptance of the paper before the new webpage with the model code goes live. We also plan to upload the footprint code as supplement to this paper. Thanks for the suggestion, we now do mention the availability of the code at an earlier point in the paper (end of Introduction).

P6759 Line 16- Matheny et al 2104 JGR 119:2292-2311 and Morin et al JGR 2014 119:2188–2208 are two additional example for novel applications of a 2-D footprint model, for scaling the contribution to flux measurements from a disturbance area and for gap-filling of CO2 and methane fluxes from a heterogeneous wetland site. Morin et al is also provides a relevant for Page 6761 Line 5, and for remote-sensing driven footprint climatology (see Morin's figure A1) discussed in page 6775, lines 15-20.

Many thanks for the above references. We want to stress that the articles listed in our manuscript are by far not exhaustive. As footprint modelling has become an established approach in the FLUXNET community, it is beyond the scope of this manuscript to list all articles dealing with such. We hence refrain from adding these additional references.

Page 6762 Line 8-10: What happens in airborne measurements? The vertical reference cannot be assumed as fixed there. Upon further reading, the topic of footprint for moving measurements, such as airborne flux measurements, is not addressed at all. I recommend removing the comment about airborne measurements in Page 6760 Line 8 as it is creates a false expectation that the solution you are about to present can handle these as well.

Recent research has shown that footprint models can be applied to airborne flux measurements. We refer to according studies from, for example, Hutjes et al. (2010), Kustas et al. (2006), Mauder et al. (2008) and Metzger et al. (2012, 2013). These articles are listed in our manuscript as examples for such approaches. Adding details on the processing of airborne flux measurements is beyond the scope of this manuscript.

Page 6762 – the formulation here tells us about the footprint function, but does not tell what it actually is. We end up with a symbolic representation of a footprint function (eq. 3). Took me a while to figure out where you are going with it and to get to the solution. Can you add a few words here to the effect that later in the manuscript you will derive the parameterized forms for D and (f^{y}) bar.

Many thanks for this suggestion. We have included the following sentences after Eq. (3) on page 6762 to clarify the aim of the parameterisation: "In the following sections, we present a scaling approach and a parameterisation for the derivation of (f^y) bar and D_y with the aim of simple and accessible estimation of f(x,y)."

Page 6772 – at some point around equation 13 I ran out of patience and started going over all the equations looking for a formulation of (f^{y}) bar and sigma_y, which are the key to solving the footprint function (eq 10). After a somewhat frustrating quest, I finally found it, way later, on page 6772, hidden in the numerical recipe of example 5.2, and not strictly formulated (the reader is instructed to invert equations 8 or 9 and 13). I admit that my jumpy reading style and short attention span should not be considered the norm or burden the authors, but would it be possible to write the inverted forms of eq9 (or eq8) and eq13 (i.e. (f^{x}) bar = . . . and sigma_y = . . .) at an earlier point, and say that they could be solved and substituted in eq10 to find the footprint function, provided empirical formulations for sigma_y* and F^y*. I think the end of section 3 would be a suitable spot for this, as it will provide a logical transition to the parameterization in section 4.

The structure of the manuscript is as follows: 1) real scale footprint data set, 2) scaling approach to be applied to footprint data, 3) parameterisation of scaled footprints, 4) derivation of real scaled footprints based on the parameterisation. We think that introducing an inversion of the scaling in between rather than at the end would be confusing. Nevertheless, we added a short explanation of the steps in Section 2 (see above) and hope this helps to clarify the approach.

Page 6777 Line 7 – See nice example of a flux tower-based study of the roughness parameters in a forest site in Maurer et al 2013 AFM.

Many thanks, very interesting study. We added a reference to Maurer et al. in Section 5.4.

Page 6777 lines 9-12 – the letter h is often associated with canopy height and not always with boundary layer height as in this paper. As it is mentioned immediately after z_0 (which is a function of canopy height) it confused me. Please move the explicit definition of h to this point, to prevent confusion, i.e. "Measurements of the boundary layer height, h, are available only rarely. . ." (it is currently about 5 lines later, in "a small variation in the input value of the boundary layer height, h . ..")

We have changed the sentences as suggested by the referee (Section 6.1).

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Metzger, S., Junkermann, W., Mauder, M., Butterbach-Bahl, K., Trancón y Widemann, B., Neidl, F., Schäfer, K., Wieneke, S., Zheng, X. H., Schmid, H. P., and Foken, T.: Spatially explicit regionalization of airborne flux measurements using environmental response functions, Biogeosciences, 10, 2193-2217, 2013

Responses to Referee #2

The authors state that "the aim of the present study is not to present a new footprint model, but to provide a simple and easily accessible parameterisation or "short-cut" for the much more sophisticated, but highly resource intensive, model". The aim is very much welcome and invaluable for the community carrying eddy covariance flux measurements, and the paper fulfils the aim. The paper is written and structured very clearly and is "user-friendly" and I have only few minor comments and recommend its acceptance after the comments are concerned.

Many thanks!

1. p. 6758 (Abstract), line 5: the sentence can be interpreted that single site flux gives information at sub-ecosystem scale and upscaling to ecosystem scale is needed. However, it is commonly thought that eddy covariance is operating, almost by definition, at ecosystem scale (or neighbourhood scale if urban surface). Can you clarify?

We agree that ideally, a flux tower does provide information on the ecosystem scale (which in reality is not always met). To clarify, we changed the wording in the abstract and replaced 'ecosystem scale' by 'local scale'.

2. p. 6760, line 25: there is a very recent article on footprints and LES: Hellsten et al., Footprint evaluation for flux and concentration measurements for an urban-like canopy with coupled Lagrangian stochastic and large-eddy simulation models. Boundary-Layer Met. DOI 10.1007/s10546-015-0062-4, 2015. Note that I am not asking you to necessarily refer to this article but mentioning it just for your notice.

Many thanks. As we haven't mentioned so far the footprint approach using a combination of LES and LS, we added the above reference and an additional paper to fill this gap in the Introduction.

3. P. 6764, line 26: from where the value for the zero-plane displacement height is obtained? It is maybe mentioned somewhere but it would be good to say/explain it here.

We assume the referee refers to p. 6763 (there is no line 26 on p. 6764). For the simulations of LPDM-B of Section 2, only z_m is of interest, as the model does not include the roughness sublayer. For footprint estimates of 'real' receptors mounted at z_receptor on a flux tower, the zero-plane displacement height, z_d, is needed for derivation of z_m. We added a couple of sentences on the possible derivation of d in Section 5.4, where real-scale flux footprints are discussed.

4. It would be good to have a section called "Results"; Does it include sub-sections in Section 3 or only 4 and/or 5? The present titles of the sections can be kept but they would be below Results.

This is a tricky request. As we developed a novel scaling approach, a new parameterisation, and a new approach for fast and simple real-scale footprint estimates, it is not really obvious which sections would be part of a Results section. We hence prefer to leave the structure as it is.

5. Table 1 and other relevant places: Measurement heights within the roughness sublayer (RSL) are disregarded. However, in reality, many flux measurements are in fact carried within RSL, although the (strict) recommendations are against it. I am not asking you to do anything right now for the paper but by raising this issue I would welcome the continuation of your work to include also RSL effects. Do you know to which direction the omission of RSL is leading? If someone is using your parameterisation for RSL measurements, is there overestimation or underestimation of the extension of the footprint?

The referee raises an important question. In fact, the inclusion of RSL is part of current work of the authors.

6. Table 4: why for neutral cases the value of R for the standard deviation is much lower (0.37) compared to other cases?

Many thanks – we managed to improve the performance metrics for the neutral scenarios by adjusting the proportionality factor ps2 to 0.35. The metrics in Tab. 3 and Tab. 4 were adjusted accordingly.

7. Fig. 5: The measurement (receptor) height is only 12m, as far as I know the tree height at Norunda is higher. Please, clarify. In addition, the background map is said to be tree height, but no scale is given.

For Figure 5, we used measurements at 33 m above ground. However, note that throughout the manuscript, we set $z_m = z_r$ eceptor $-z_d$, hence with $z_d = 21$ m, we get $z_m = 12$ m. We added this information to the figure captions to omit confusion.

8. General comment: I am not asking you to do anything right now for the paper but by raising this issue I would welcome the continuation of your work to calculate also concentration footprints. They would be valuable for tall tower absolute concentration measurements, but I am not sure how you could deal with advection/long-distance transport.

Yes, we agree, this is an important issue and again, it is part of current work of the authors.

Responses to Referee #3

By using scaling approach and suitable fitting functions, the authors present an easy to use, full (in terms of along wind and cross-wind representations) footprint function for variety of stabilities and Atmospheric Boundary Layer (ABL) flow regimes. It is the first such footprint model enabling to make fast footprint estimation for the measurements outside the Atmospheric Surface Layer (ASL) scaling domain. The model therefore serves as a useful tool not only for tall tower sites but also for the measurement conditions violating the ASL assumptions, which are typically constrained to the measurement heights less than or equal to the magnitude of the Obukhov length scale. I fully support publication and hope that addressing the comments below helps to improve the

manuscript.

Many thanks!

The scaling is performed via four dimensionless groups. The dimensionless groups do not include directly any parameters related to ABL flow characteristics such as the convective velocity scale. Have the authors considered including this velocity scale to improve (potentially) the footprint parameterization under convective conditions and would it help to explain different parameterization coefficients obtained for the convective regime (Table 6)?

Indeed, we have tried to include the convective velocity scale, but this did not prove to be successful. What we presented in this manuscript is the statistically best scaling approach we found and the result of research over an extended period of time.

The second comment is related to the third dimensionless group which is formulated based on the common phenomenon that the surface fluxes decrease approximately linearly with height in the ABL (page 6765, line 6-9). On the other hand, the footprint function is formulated such that it obeys the basic property of integration to unity (page 6769, line 13-15), which according to eq. (1) implies that the flux measured at zm equals to the surface flux. According to the given references (e.g. Kljun et al., 2004), the model LPDM-B is formulated such that the upper boundary condition of the simulation domain was not set to reflection. In forward Lagrangian approach this would imply that the surface release of particles eventually means absorption (or exit of the particles from the domain) at the upper boundary, and consequently constant particle flux with height up to the boundary layer top. The forward and backward Lagragian approaches are known to be equivalent and the same must apply to the backward approach. Please discuss the effect of the upper boundary condition used in LPDM-B on the results and help the reader to clarify the apparent inconsistency of the dimensionless scaling group 3 (or the reasoning behind it) with the footprint formulation eq. (1).

This must be a misunderstanding. Particles tracked by the model LPDM-B (Kljun et al. 2002) are reflected at either boundary, i.e. at the surface AND at the top of the planetary boundary layer. The particles are fully elastically reflected; i.e. no absorption or transformation at the boundaries is taken into account. A description of the reflection scheme can be found in Rotach et al. (1996) and in Wilson and Flesch (1993). We have added a sentenced highlighting the reflection at the surface and the top of the planetary boundary layer in Section 2.

The parameterization is based on the set of simulations for a range of values describing the flow as well as the surface conditions (the roughness length). The momentum flux (or the friction velocity used in the MS) is driven by the flow forcing as well as the surface characteristics (roughness) and therefore it the aerodynamically smooth surfaces induce lower momentum fluxes especially under stable conditions. For example for the roughness length value 0.01 m I would assume that the friction velocity 0.1 m/s is rather common under normal meteorological conditions (meaning that not under extreme stability conditions). The range of friction velocities used in the MS for stable conditions is quite narrow (Tables 1 and 2). Could the authors assure that scaling performs well also for low u*, in particular for the surfaces with low roughness?

To address the above, we have run three additional simulations with LPDM-B for a friction velocity of $u^* = 0.1 \text{ m/s}$, a roughness length of z0 = 0.01 m, and a measurement height of zm = 10 m. For the stable case, we set L = 500 m and h = 280 m; for the neutral case, $L = \inf$, h = 300 m, and $w^* = 0 \text{ m/s}$, and finally, for the convective case we set L = -50 m, h = 2500 m, and $w^* = 0.5 \text{ m/s}$.

Figure 1R shows the same density plot of all original LPDM-B simulations as Fig. 2 of the manuscript. We added the scaled footprints of the above additional simulations (stable case: dash-dotted line, neutral case: dashed line, convective case: solid line). As can be seen in Fig. 1R, the scaled footprints of the low-u* scenarios nicely fit the ensemble of other scenarios.

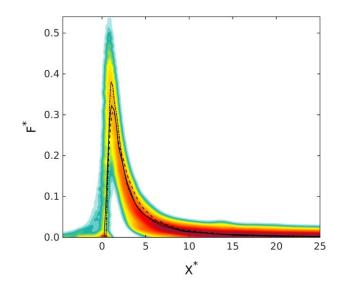


Figure 1R: Density plot of scaled crosswind-integrated footprints of LPDM-B simulations (cf. Fig. 2 of manuscript). Black lines depict additional low-u* scenarios (stable: dash-dotted line, neutral: dashed line, convective: solid line).

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The simple two-dimensional parameterisation for Flux Footprint Predictions FFP

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Discussion Paper

Abstract

Flux footprint models are often used for interpretation of flux tower measurements, to estimate position and size of surface source areas, and the relative contribution of passive scalar sources to measured fluxes. Accurate knowledge of footprints is of crucial importance for any upscaling exercises from single site flux measurements to ecosystem local or regional scale. Hence, footprint models are ultimately also of considerable importance for improved greenhouse gas budgeting. With increasing numbers of flux towers within large monitoring networks such as FLUXNET, ICOS, NEON, or AMERIFLUX, and with increasing temporal range of observations from such towers (order of decades) and availability of airborne flux measurements, there has been an increasing demand for reliable footprint estimation. Even though several sophisticated footprint models have been developed in recent years, most are still not suitable for application to long time series, due to their high computational demands. Existing fast footprint models, on the other hand, are based on Surface Layer theory and hence are of restricted validity for real case applications.

To remedy such shortcomings, we present the two-dimensional Flux Footprint Parameterisation, FFP, based on a novel scaling approach for the crosswind distribution of the flux footprint and on an improved version of the footprint parameterisation of Kljun et al. (2004b). Compared to the latter, FFP now provides not only the extent, but also the width and shape of footprint estimates, and explicit consideration of the effects of the surface roughness length. The footprint parameterisation has been developed and evaluated using simulations of the backward Lagrangian stochastic particle dispersion model LPDM-B (Kljun et al., 2002). Like LPDM-B, the parameterisation is valid for a broad range of boundary layer conditions and measurement heights over the entire planetary boundary layer. Thus it can provide footprint estimates for a wide range of real case applications.

The new footprint parameterisation requires inputs that can be easily determined from, for example, flux tower measurements or airborne flux data. FFP can be applied to data of long-term monitoring programmes as well as be used for quick footprint estimates in the field, or for designing new sites.

1 Introduction

Flux footprint models are used to describe the spatial extent and position of the surface area that is contributing to a turbulent flux measurement at a specific point in time, for specific atmospheric conditions and surface characteristics. They are hence very important tools when it comes to interpretation of flux measurements of passive scalars, such as the greenhouse gases carbon dioxide (CO_2), water vapour (H_2O), or methane (CH_4).

In recent years, the application of footprint models has become a standard task in analysis of measurements from flux towers (e.g., Aubinet et al., 2001; Rebmann et al., 2005; Nagy et al., 2006; Göckede et al., 2008; Mauder et al., 2013) or airborne flux measurements (Kustas et al., 2006; Mauder et al., 2008; Hutjes et al., 2010; Metzger et al., 2012) of inert (i.e., long-lived) greenhouse gases. Information about the sink and source location is even more crucial for towers in heterogeneous or disturbed landscapes (e.g., Sogachev et al., 2005), a topical study area in recent times. Schmid (2002) showed that the use of the footprint concept has been increasing exponentionally since 1972. Since then, footprint models have been used for planning and design of new flux towers and have been applied to most flux tower observations around the globe, to support the interpretation of such measurements.

Long-term and short-term flux observations are exposed to widely varying atmospheric conditions and their interpretation therefore involves an enormous amount of footprint calculations. Despite the widespread use of footprint models, the selection of a suitable model still poses a major challenge. Complex footprint models based on Large Eddy Simulations (LES; e.g., Luhar and Rao, 1994; Leclerc et al., 1997; Steinfeld et al., 2008; Wang and Davis, 2008), Eulerian models of higher order turbulence closure (e.g., Sogachev and Lloyd, 2004), or Lagrangian stochastic particle dispersion (LS; e.g., Leclerc and Thurtell, 1990; Horst and Weil, 1992; Flesch, 1996; Baldocchi, 1997; Rannik et al., 2000; Kljun et al., 2002; Hsieh et al., 2003), or a combination of LES and LS (e.g., Markkanen et al., 2009; Hellsten et al., 2015) can, to a certain degree, offer the ability to resolve complex flow structures (e.g., flow over a forest edge or a street canyon) and surface heterogeneity. However, to date they

are laborious to run, still highly CPU-intensive, and hence can in practice be applied only for case studies over selected hours or days, and most are constrained to a narrow range of atmospheric conditions. These complex models are not suited for dealing with the vast increase of long-term flux tower data or the more and more frequent airborne flux measurements. Instead, quick footprint estimates are needed, models that can deal with large amounts of input data, for example several years of half-hourly data points at several observational levels at multiple locations. For these reasons, analytical footprint models are often used as a compromise (e.g., Schuepp et al., 1990; Leclerc and Thurtell, 1990; Schmid and Oke, 1990; Wilson and Swaters, 1991; Horst and Weil, 1992, 1994; Schmid, 1994, 1997; Haenel and Grünhage, 1999; Kormann and Meixner, 2001). These models are simple and fast, but their validity is often constrained to ranges of receptor heights and boundary layer conditions that are much more restricted than those commonly observed.

Existing footprint modelling studies offer the potential for simple parameterisations as, for example, proposed by Horst and Weil (1992; 1994), Weil and Horst (1992), Schmid (1994) or Hsieh et al. (2000). The primary drawback of these parameterisations is their limitation to a particular turbulence scaling domain (often Surface Layer scaling), or to a limited range of stratifications. Conversely, measurement programs of even just a few days are regularly exposed to conditions spanning several turbulence scaling domains.

To fill this gap, Kljun et al. (2004b) introduced a footprint parameterisation based on a fit to scaled footprint estimates derived from the Lagrangian stochastic particle dispersion model LPDM-B (Kljun et al., 2002). LPDM-B is one of very few LS footprint models valid for a wide range of boundary layer stratifications and receptor heights. Likewise, the parameterisation of LPDM-B is also valid for outside Surface Layer conditions and for non-Gaussian turbulence, as for example for the Convective Boundary Layer. However, the parameterisation of Kljun et al. (2004b) comprises only the crosswind-integrated footprint, i.e. it describes the footprint function's upwind extent but not its width.

In recent time, footprint model outputs have frequently been combined with surface information, such as remote sensing data (e.g., Schmid and Lloyd, 1999; Kim et al., 2006; Li et al., 2008; Barcza et al., 2009; Chasmer et al., 2009; Sutherland et al., 2014). As re-

mote sensing data is increasingly available in high spatial resolution, a footprint often covers more than one pixel of remote sensing data; hence there is a need for information of the crosswind spread of the footprint. Similar to FSAM (Schmid, 1994), the footprint model of Kormann and Meixner (2001) includes dispersion in crosswind direction. Detto et al. (2006) provided a crosswind extension of the footprint model of Hsieh et al. (2000). However, all these models are of limited validity restricted to measurements close to the surface. For more details on their validity and restrictions, and for a comprehensive review on existing footprint techniques and approaches the reader is referred to Schmid (2002), Vesala et al. (2008), or Leclerc and Foken (2014).

This study addresses the issues and shortcomings mentioned above. We present the new footprint parameterisation FFP, with improved footprint predictions for elevated measurement heights in stable stratifications. The influence of the surface roughness has been implemented into the scaling approach explicitly. Further and most importantly, the new parameterisation describes also the crosswind spread of the footprint and hence, it is suitable for many practical applications. Like all footprint models that do not simulate the full time- and space-explicit flow, FFP implicitely assumes stationarity over the eddy-covariance integration period (typically 30 min) and horizontal homogeneity of the flow (but not of the scalar source/sink distribution). As in Kljun et al. (2004b), the new parameterisation is based on a scaling approach of flux footprint results of the thoroughly tested Lagrangian footprint model LPDM-B (Kljun et al., 2002). Its most important scaling variables are readily available through common turbulence measurements that are typically performed at flux tower sites. The code of FFP can be obtained in several platform-independent programming languages at www.footprint.kljun.net and is also supplied as a supplement of this publication.

2 Footprint dataset

Mathematically, the flux footprint, f, is the transfer function between sources or sinks of passive scalars at the surface, Q_c , and the turbulent flux, F_c , measured at a receptor at height z_m (e.g., Pasquill and Smith, 1983; Schmid, 2002). We define a local footprint coor-

dinate system, where the receptor is mounted above the origin (0,0) and positive x indicates upwind distance, such that

$$F_c(\mathbf{0},\mathbf{0},z_{\mathsf{m}}) = \int_{\Re} Q_c(x,y) f(x,y) \, \mathsf{d}x \, \mathsf{d}y, \tag{1}$$

where \Re denotes the integration domain. As the footprint function is always specific to a given measurement height, the vertical reference in f is neglected, for simplicity. It follows that the footprint function is proportional to the flux increment arising from a single unit point source or sink, Q_u , i.e.,

$$f(x,y) = \frac{F_c(0,0,z_m)}{Q_u(x,y)}.$$
(2)

As F_c is a flux density (per unit area) and Q_u is a source or sink integrated over a unit area, the two-dimensional footprint function has the dimension of [1/area]. Assuming that crosswind turbulent dispersion can be treated independently from vertical or streamwise transport, the footprint function can be expressed in terms of a crosswind-integrated footprint, $\overline{f^y}$, and a crosswind dispersion function, D_y , (see, e.g., Horst and Weil, 1992)

$$f(x,y) = \overline{f^y}(x) D_y.$$
(3)

In the following sections, we present a scaling approach and a parameterisation for the derivation of $\overline{f^y}$ and D_y with the aim of simple and accessible estimation of f(x,y).

Derivation and evaluation of the footprint parameterisation are based on footprint calculations using LPDM-B (Kljun et al., 2002). LPDM-B is a footprint model of the Lagrangian stochastic particle dispersion type, with three-dimensional dispersion of inert particles as described by Rotach et al. (1996) and de Haan and Rotach (1998). LPDM-B fulfils the wellmixed condition (Thomson, 1987) and is valid for stable, neutral, and convective boundary layer stratifications, assuming stationary flow conditions. It has been shown to reproduce wind-tunnel simulations very well (Kljun et al., 2004a). LPDM-B reflects particles fully

elastically at the surface and at the top of the planetary boundary layer and tracks particles backward in time, from the receptor location to the source / sink, at the surface (i.e., particle touchdown location, see Kljun et al., 2002, for details). Hence, footprint calculation can be based on all computed particle tracks directly without the need for coordinate transformation. We refer to Rotach et al. (1996), de Haan and Rotach (1998), and Kljun et al. (2002) for details in the formulation and evaluation of the model.

Compared to the original parameterisation of Kljun et al. (2004b), we have increased the parameter space for LPDM-B simulations especially for stable boundary layer conditions. We also increased the covered range of roughness lengths, z_0 , to include roughness lengths that may be found over sparse forest canopies. For the parameterisation, a total of 200 simulations were run with LPDM-B for measurement heights between 1 and 1000 m and boundary layer conditions between strongly convective, neutral, to strongly stable. With that, the simulations span a range of stability regimes, namely the Surface Layer, Local Scaling Layer, Z-less Scaling Layer, Neutral Layer, the Free Convection Layer, and the Mixed Layer (cf. Holtslag and Nieuwstadt, 1986). Table 1 gives an overview of the parameter space for the simulated scenarios. We use standard definitions for the friction velocity, u_{*} , the convective velocity scale, w_* , and the Obukhov length, L (see, e.g., Stull, 1988, and Appendix B for details and for the definition of L). Each scenario was run for the whole set of roughness lengths and for all listed measurement heights. Note that we define the measurement height as $z_{\rm m} = z_{\rm receptor} - z_{\rm d}$, where $z_{\rm receptor}$ is the height of the receptor above ground and z_d is the zero-plane displacement height. 47 cases with measurement height within the roughness sublayer (z_*) were excluded from later analysis $[z_* \approx n h_{rs}]$; where commonly $2 \le n \le 5$ (Raupach et al., 1991; Rotach and Calanca, 2014), with h_{rs} , the mean height of the roughness elements, approximated by $h_{rs} = 10 z_0$ (Grimmond and Oke, 1999)]. Here, we use $z_* = 2.75 h_{rs}$.

As expected for such a broad range of scenarios, the resulting footprints of LPDM-B simulations show a vast range of extents and sizes. Fig. 1 depicts this range by means of peak location of the footprints and their extent, when integrated from their peak to 80% contribution of the total footprint (cf. Sect. 5.3). For example, the 80% footprint extents

ranged from a few tens to a few hundreds of meters upwind of the tower location for the lowest measurement heights. For the highest measurements, the 80 % footprints ranged up to 270 km.

An additional set of 27 LPDM-B simulations was run for independent evaluation of the footprint parameterisation. Measurement heights that are typical for flux tower sites were selected for this evaluation set, with boundary layer conditions again ranging from convective to stable. Table 2 lists the characteristics of these additional scenarios.

3 Scaling of footprints

The vast range in footprint sizes presented above clearly manifests that it is not practical to fit a single footprint parameterisation to all real-scale footprints. An additional step of footprint scaling is hence needed, with the goal of deriving a universal non-dimensional footprint. Ideally, such dimensionless footprints collapse to a single shape or narrow ensemble of curves. We follow a method that borrows from Buckingham Π dimensional analysis (e.g., Stull, 1988), using dimensionless Π -functions to scale the footprint estimates of LPDM-B, similar to Kljun et al. (2004b), and scale the two components of the footprint, the crosswindintegrated footprint and its crosswind dispersion (Eq. 3), in two separate steps.

3.1 Scaled crosswind-integrated footprint

As in Kljun et al. (2004b), we choose scaling parameters relevant for the crosswindintegrated footprint function, $\overline{f^y}(x)$. The first choice is the receptor height, z_m , as experience shows that the footprint (both its extent and footprint function value) is most strongly dependent on this height. Secondly, as indicated in Eq. (2), the footprint is proportional to the flux at height z_m . We hence formulate another scaling parameter based on the common finding that turbulent fluxes decline approximately linearly through the planetary boundary layer, from their surface value to the boundary layer height, h, where they disappear (e.g., Stull, 1988). Lastly, as a transfer function in turbulent boundary layer flow, the footprint is directly affected by the mean wind velocity at the measurement height, $\overline{u}(z_m)$, as well as by the surface shear stress, represented by the friction velocity, u_* . The well-known diabatic Surface Layer wind speed profile (e.g., Stull, 1988) relates $\overline{u}(z_m)$ to the roughness length, z_0 , and the integrated form of the non-dimensional wind shear, Ψ_M , that accounts for the effect of stability (z_m/L) on the flow.

With the above scaling parameters we form four dimensionless Π groups as

$$\Pi_{1} = \overline{f^{y}} z_{m}$$

$$\Pi_{2} = \frac{x}{z_{m}}$$

$$\Pi_{3} = \frac{h - z_{m}}{h} = 1 - \frac{z_{m}}{h}$$

$$\Pi_{4} = \frac{\overline{u}(z_{m})}{u_{*}} k = \ln\left(\frac{z_{m}}{z_{0}}\right) - \Psi_{M}$$
(4)

where k = 0.4 is the von Karman constant. We use Ψ_M as suggested by Högström (1996):

$$\Psi_{M} = \begin{cases} -5.3\frac{z_{m}}{L} & \text{for } L > 0, \\ \ln\left(\frac{1+\chi^{2}}{2}\right) + 2\ln\left(\frac{1+\chi}{2}\right) - 2\tan^{-1}(\chi) + \frac{\pi}{2} & \text{for } L < 0. \end{cases}$$
(5)

with $\chi = (1 - 19 z_m/L)^{1/4}$. In principle, Ψ_M is based on Monin-Obukhov similarity and valid within the Surface Layer. Hence special care was taken in testing this scaling approach for measurements outside the Surface Layer (see below). In contrast to Kljun et al. (2004b), the present study incorporates the roughness length directly in the scaling procedure: high surface roughness (i.e., large z_0) enhances turbulence relative to the mean flow, and thus shortens the footprints. Here, z_0 is either directly used as input parameter or is implicitly included through the fraction of $\overline{u}(z_m)/u_*$.

The non-dimensional form of the crosswind-integrated footprint, F^{y*} , can be written as a yet unknown function φ of the non-dimensional upwind distance, X^* . Thus $F^{y*} = \varphi(X^*)$,

(7)

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$$X^* = \frac{x}{z_{\rm m}} \left(1 - \frac{z_{\rm m}}{h} \right) \left(\frac{\overline{u}(z_{\rm m})}{u_*} k \right)^{-1} \tag{6}$$

$$= \frac{x}{z_{\rm m}} \left(1 - \frac{z_{\rm m}}{h}\right) \left(\ln\left(\frac{z_{\rm m}}{z_0}\right) - \Psi_M\right)^{-1}$$
$$F^{y*} = \overline{f^y} z_{\rm m} \left(1 - \frac{z_{\rm m}}{1 - \frac{z_$$

$$\overline{f^{y*}} = f^y z_{\mathsf{m}} \left(1 - \frac{z_{\mathsf{m}}}{h} \right) \qquad \frac{u(z_{\mathsf{m}})}{u_*} k \tag{8}$$

$$= \overline{f^y} z_{\mathsf{m}} \left(1 - \frac{z_{\mathsf{m}}}{h} \right)^{-1} \left(\ln \left(\frac{z_{\mathsf{m}}}{z_0} \right) - \Psi_M \right). \tag{9}$$

As a next step, the above scaling procedure is applied to all footprints of Scenarios 1 to 8 (Table 1) derived by LPDM-B. Despite the huge range of footprint extents (Fig. 1), the resulting scaled footprints collapse into an ensemble of footprints of very similar shape, peak location, and extent (Fig. 2). Hence the new scaling procedure for crosswind-integrated flux footprints proves to be successful across the whole range of simulations, including the large range of surface roughness lengths and stability regimes.

3.2 Scaled crosswind dispersion

Crosswind dispersion can be described by a Gaussian distribution function with σ_y as the standard deviation of the crosswind distance (e.g., Pasquill and Smith, 1983). In contrast to vertical dispersion, Gaussian characteristics are valid for crosswind dispersion for the entire stability range and are even appropriate over complex surfaces (e.g., Rotach et al., 2004). The three-dimensional particle dispersion of LPDM-B incorporates the Gaussian lateral dispersion (cf. Kljun et al., 2002). Note that variations of the mean wind direction by the Ekman effect are neglected. Hence, assuming Gaussian characteristics for the crosswind dispersion function, D_y , in Eq. (3), the flux footprint, f(x,y), can be described as (e.g.,

Horst and Weil, 1992)

$$f(x,y) = \overline{f^y}(x) \frac{1}{\sqrt{2\pi\sigma_y}} \exp\left(-\frac{y^2}{2\sigma_y^2}\right).$$
(10)

Here, y is the crosswind distance from the centreline (i.e., the *x*-axis) of the footprint. The standard deviation of the crosswind distance, σ_y , depends on boundary layer conditions and the upwind distance from the receptor.

Similar to the crosswind-integrated footprint, we aim to derive a scaling approach of the lateral footprint distribution. We choose y and σ_y as the relevant length scales, and combine them with two scaling velocities, the friction velocity, u_* , and the standard deviation of lateral velocity fluctuations, σ_v . In addition to the Π groups of Eq. (4), we therefore set

$$\Pi_{5} = \frac{y}{z_{m}}$$

$$\Pi_{6} = \frac{\sigma_{y}}{z_{m}}$$

$$\Pi_{7} = \frac{\sigma_{v}}{u_{*}}.$$
(11)

In analogy to, for example, Nieuwstadt (1980), we define a non-dimensional standard deviation of the crosswind distance, σ_y^* , proportional to $\Pi_6 \Pi_7^{-1}$. The non-dimensional crosswind distance from the receptor, Y^* , is linked to σ_y^* through Eq. (10) and accordingly has to be proportional to $\Pi_5 \Pi_7^{-1}$. With that

$$Y^* = p_{s1} \frac{y}{z_m} \frac{u_*}{\sigma_v}$$
(12)
$$\sigma_y^* = p_{s1} \frac{\sigma_y}{z_m} \frac{u_*}{\sigma_v},$$
(13)

where p_{s1} is a proportionality factor depending on stability. Based on the LPDM-B results, we set $p_{s1} = \min(1, |z_m/L|^{-1} 10^{-5} + p)$, with p = 0.8 for $L \le 0$ and p = 0.55 for L > 0, respectively. In Fig. 3 unscaled distance from the receptor, x, and scaled, non-dimensional

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distance X^* are plotted against the unscaled and scaled deviations of the crosswind distance, respectively (see Appendix C for information on the derivation of σ_u from LPDM-B simulations). The scaling procedure is clearly successful, as the scaled deviation of the crosswind distance, σ_u^* , of all LPDM-B simulations collapse into a narrow ensemble when plotted against X^* (Fig. 3, right-hand panel). For large X^* , the ensemble spread increases mainly due to increased scatter of LPDM-B simulations for distances far away from the receptor.

Flux Footprint Parameterisation FFP 4

The successful scaling of both along-wind and crosswind shapes of the footprint into narrow ensembles within a non-dimensional framework provides the basis for fitting a parameterisation curve to the ensemble of scaled LPDM-B results. Like for the scaling approach, the footprint parameterisation is set up in two separate steps, the crosswind-integrated footprint, and its crosswind dispersion.

4.1 Crosswind-integrated footprint parameterisation

The ensemble of scaled crosswind-integrated footprints $F^{y*}(X^*)$ of LPDM-B is sufficiently coherent that it allows fitting a single representative function to it. We choose the product of a power function and an exponential function as a fitting function for the parameterised cross-wind integrated footprint $\hat{F}^{y*}(\hat{X}^*)$:

$$\hat{F}^{y*} = a \left(\hat{X}^* - d \right)^b \, \exp\left(\frac{-c}{\hat{X}^* - d} \right). \tag{14}$$

Derivation of the fitting parameters, a, b, c, d is dependent on the constraint that the integral of the footprint parameterisation (cf. Eq. 14) must equal unity to satisfy the integral condition $\int_{-\infty}^{\infty} F^{y*}(X^*) dX^* = 1$ (cf. Schmid, 1994; Kljun et al., 2004b). Hence

$$\int_{d}^{\infty} \hat{F}^{y*}(\hat{X}^{*}) d\hat{X}^{*} = 1$$

$$= \int_{d}^{\infty} a (\hat{X}^{*} - d)^{b} \exp\left(\frac{-c}{\hat{X}^{*} - d}\right) d\hat{X}^{*}$$

$$= a c^{b+1} \Gamma(-b-1), \qquad (16)$$

where $\Gamma(b)$ is the gamma function, and here $\Gamma(-b-1) \equiv \int_0^\infty t^{-b-2} \exp(-t) dt$.

The footprint parameterisation (Eq. 14) is fitted to the scaled footprint ensemble using an unconstrained nonlinear optimization technique based on the Nelder-Mead simplex direct search algorithm (Lagarias et al., 1998). With that, we find

$$a = 1.452$$

 $b = -1.991$
 $c = 1.462$
 $d = 0.136$. (17)

Figure 2 shows that the parameterisation of the crosswind-integrated footprint represents all scaled footprints very well. The goodness-of-fit of this single parameterisation to the ensemble of scaled footprints for all simulated measurement heights, stability conditions, and roughness lengths, is evident from model performance metrics (see, e.g., Hanna et al., 1993; Chang and Hanna, 2004), including the Pearson's correlation coefficient (R), the fractional bias (FB), the fraction of the parameterisation within a factor of two of the scaled footprints (FAC2), the geometric variance (VG), and the normalised mean square error (NMSE). Table 3 lists these performance metrics for the parameterisation of the full extent of the crosswind-integrated footprint curve, for the footprint peak location, and for the footprint peak value of the parameterisation against the corresponding scaled LPDM-B results. The fit can be improved even more if the parameters are optimised to represent footprints of convective or neutral and stable conditions only (see Appendix A).

4.2 Parameterisation of the crosswind footprint extent

A single function can be fitted also to the scaled crosswind dispersion. In conformity with Deardorff and Willis (1975), the fitting function was chosen to be of the form

$$\hat{\sigma}_y^* = a_{\rm c} \left(\frac{b_{\rm c} (\hat{X}^*)^2}{1 + c_{\rm c} \hat{X}^*} \right)^{1/2}.$$
(18)

A fit to the data of scaled LPDM-B simulations results in

$$a_{\rm c} = 2.17$$

 $b_{\rm c} = 1.66$
 $c_{\rm c} = 20.0.$ (19)

The above parameterisation of the scaled deviation of the crosswind distance of the footprint is plotted in Fig. 3 (right panel). The performance metrics confirm that the σ_y^* of the scaled LPDM-B simulations are very well reproduced by the parameterisation $\hat{\sigma}_y^*$ (Table 3).

5 Real-scale flux footprint

Typically, users of footprint models are interested in footprints given in a real-scale framework, such that distances (e.g., between the receptor and maximum contribution to the measured flux) are given in metres or kilometers. Depending on the availability of observed parameters, the conversion from the non-dimensional (parameterised) footprints to realscale dimensions can be based on either Eqs. (6) and (8), or on Eqs. (7) and (9). For convenience, the necessary steps of the conversion are described in the following, by means of some examples.

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5.1 Maximum footprint contribution

The distance between the receptor and the maximum contribution to the measured flux can be approximated by the peak location of the crosswind-integrated footprint. The maximum's position can be deduced from the derivative of Eq. (14) with respect to X^* :

$$\hat{X}_{\max}^* = \frac{-c}{b} + d. \tag{20}$$

Using the fitting parameters as listed in Eq. (17) to evaluate \hat{X}^*_{max} , the peak location is converted from the scaled to the real-scale framework applying Eq. (6)

$$x_{\max} = \hat{X}_{\max}^* z_{\max} \left(1 - \frac{z_{\max}}{h}\right)^{-1} \frac{\overline{u}(z_{\max})}{u_*} k$$
$$= 0.87 z_{\max} \left(1 - \frac{z_{\max}}{h}\right)^{-1} \frac{\overline{u}(z_{\max})}{u_*} k, \qquad (21)$$

or, alternatively applying Eq. (7)

$$x_{\max} = \hat{X}_{\max}^{*} z_{\max} \left(1 - \frac{z_{\max}}{h}\right)^{-1} \left(\ln\left(\frac{z_{\max}}{z_{0}}\right) - \Psi_{M}\right)$$
$$= 0.87 z_{\max} \left(1 - \frac{z_{\max}}{h}\right)^{-1} \left(\ln\left(\frac{z_{\max}}{z_{0}}\right) - \Psi_{M}\right), \tag{22}$$

with Ψ_M as given in Eq. (5). Hence x_{\max} can easily be derived from observations of z_m , h, and $\overline{u}(z_m)$, u_* , or z_0 , L, and the constant value of \hat{X}^*_{\max} . For suggestions on how to estimate the planetary boundary layer height, h, if not measured, see Appendix B.

5.2 Two-dimensional flux footprint

The two-dimensional footprint function can be calculated by applying the crosswind dispersion (Eq. 10) to the crosswind-integrated footprint. With inputs of the scaling parameters $z_{\rm m}$, h, u_* , σ_v , and $\overline{u}(z_{\rm m})$ or z_0 , L, the two-dimensional footprint for any (x, y) combination can be derived easily by the following steps:

- 1. Evaluate X^* using Eq. (6) or (7) for given x.
- 2. Derive \hat{F}^{y*} and $\hat{\sigma}^*_y$ by inserting X^* for \hat{X}^* in Eqs. (14) and (18).
- 3. Invert Eqs. (8) or (9) and (13) to derive $\overline{f^y}$ and σ_y , respectively.
- 4. Evaluate f(x, y) for given x and y using Eq. (10).

Fig. 4 depicts an example footprint for convective conditions, computed by applying the described approach to arrays of (x, y) combinations.

5.3 Relative contribution to the total footprint area

Often, the interest lies in the extent and location of the area contributing to, for example, 80% of the measured flux. For such applications, there are two approaches: (i) the crosswind-integrated footprint function, $\overline{f^y}(x)$, is integrated from the receptor location to the upwind distance where the contribution of interest is obtained; (ii) the two-dimensional footprint function f(x,y) is integrated from the footprint peak location into all directions along constant levels of footprint values until the contribution of interest is obtained. The result is the source area: the smallest possible area containing a given relative flux contribution (cf. Schmid, 1994). This approach can also be used as a one-dimensional equivalent to the source area, for the crosswind-integrated footprint.

For case (i) starting at the receptor location, we denote \hat{X}_R^* as the upper limit of the footprint parameterisation $\hat{F}^*(\hat{X}^*)$ containing the area of interest, i.e. the fraction R of the total footprint (that integrates to 1). The integral of Eq. (14) up to \hat{X}_R^* can be simplified (see Appendix D for details) as

$$R = \exp\left(\frac{-c}{\hat{X}_R^* - d}\right).$$
(23)

With that, the distance between the receptor and \hat{X}_{R}^{*} can be determined very simply as

$$\hat{X}_{R}^{*} = \frac{-c}{\ln(R)} + d,$$
(24)

and in real-scale

$$x_{R} = \left(\frac{-c}{\ln(R)} + d\right) \quad z_{m} \left(1 - \frac{z_{m}}{h}\right)^{-1} \quad \frac{\overline{u}(z_{m})}{u_{*}}k$$
$$= \left(\frac{-c}{\ln(R)} + d\right) \quad z_{m} \left(1 - \frac{z_{m}}{h}\right)^{-1} \left(\ln\left(\frac{z_{m}}{z_{0}}\right) - \Psi_{M}\right), \tag{25}$$

where R is a value between 0.1 and 0.99. As the above is based on the crosswind-integrated footprint, the derivation includes the full width of the footprint at any along-wind distance from the receptor.

There is no near-analytical solution for the description of the source area, the extent of the fraction R, when integrating from the peak location (e.g., Schmid, 1994; Kormann and Meixner, 2001). Instead, the size of the source area has to be derived through iterative search. For crosswind-integrated footprints, the downwind $(\hat{X}_{Rd}^* < \hat{X}_{max}^*)$ and upwind $(\hat{X}_{max}^* < \hat{X}_{Ru}^*)$ distance from the receptor including the fraction R can be approximated as a function of \hat{X}_{R}^* using LPDM-B results:

$$\hat{X}_{Rd,u}^{*} = n_1 \left(\hat{X}_R^{*} \right)^{n_2} + n_3 \tag{26}$$

For the downwind limit \hat{X}_{Rd}^* , $n_1 = 0.44$, $n_2 = -0.77$, $n_3 = 0.24$. For the upwind limit, \hat{X}_{Ru}^* , the approximation is split into two parts, $n_1 = 0.60$, $n_2 = 1.32$, $n_3 = 0.61$ for $\hat{X}_{max}^* < \hat{X}_R^* \le 1.5$, and $n_1 = 0.96$, $n_2 = 1.01$, $n_3 = 0.19$ for $1.5 < \hat{X}_R^* < \infty$. The scaled distances $\hat{X}_{*,Rd}$ and $\hat{X}_{*,Ru}$ can again be transformed into real-scale values using Eqs. (6) or (7).

If the size and position of the two-dimensional R-source area are of interest, but not the footprint function value (i.e. footprint weight) itself, the pairs of x_R and y_R describing its shape can be drawn from a lookup table of the scaled corresponding X_R^* and Y_R^* values. If the footprint function values are needed for weighting of source emissions or sinks, iterative search procedures have to be applied to each footprint. Figure 4 (left panel) illustrates examples of contour lines of R-fractions from 10 to 90% of a footprint.

5.4 Footprint estimates for extended time series

The presented footprint model is computationally inexpensive and hence can be run easily for several years of data in, for example, half-hourly time steps. Each single data point can be associated with its source area by converting the footprint coordinate system to geographical coordinates, and positioning a discretised spatial array containing the footprint function onto a map or aerial image surrounding the receptor position. In many cases, an aggregated footprint, a so-called footprint climatology, is of more interest to the user than a series of footprint estimates. The aggregated footprint can be normalised and presented for several levels of relative contribution to the total aggregated footprint. Figure 5 shows an example of such a footprint climatology for one month of half-hourly input data for the ICOS flux tower site Norunda in Sweden (cf. Lindroth et al., 1998). A footprint climatology can be derived for selected hours of several days, for months, seasons, years, etc., depending on interest.

Combined with remotely sensed data, a footprint climatology provides spatially explicit information on vegetation structure, topography, and possible source/sink influences on the measured fluxes. This additional information has proven to be beneficial for analysis and interpretation of flux data (e.g., Rahman et al., 2001; Rebmann et al., 2005; Kim et al., 2006; Chasmer et al., 2008; Barcza et al., 2009; Gelybó et al., 2013; Maurer et al., 2013). A combination of the footprint parameterisation presented here with high-resolution remote sensing data can be used not only to estimate the footprint area for measurements, but also to weigh or classify spatially continuous information on the surface and vegetation for its impact on measurements.

Certain remotely sensed data, for example airborne LiDAR data, allow for approximate derivation of the zero-plane displacement height and the surface roughness length (Chasmer et al., 2008). Alternatively, z_d and z_0 may be estimated from flux tower measurements . If z_0 varies (e.g., Rotach, 1994; Kim et al., 2006). If these measures vary substantially for different wind directions, we suggest running a spin-up of the footprint model, updating the measurement height ($z_m = z_{receptor} - z_d$) and the footprint-weighted z_0 input with each

step, until a "steady state" of the footprints is reached. We recommend such a spin-up procedure despite the fact that footprint models are in principle not valid for non-scalars, such as momentum.

6 Discussion

6.1 Evaluation of FFP and sensitivity to input parameters

Exhaustive evaluation of footprint models is still a difficult task, and clearly, tracer-flux field experiments would be very helpful. We are aware that in reality such experiments are both challenging and expensive to run. However, the aim of the present study is not to present a new footprint model, but to provide a simple and easily accessible parameterisation or "short-cut" for the much more sophisticated, but highly resource intensive, Lagrangian stochastic particle dispersion footprint model LPDM-B of Kljun et al. (2002). For the current study, we hence restrict the assessment of the presented footprint parameterisation to an evaluation against an additional set of LPDM-B simulations. A description of these additional scenarios can be found in Table 2.

The capability of the footprint parameterisation to reproduce the real-scale footprint of LPDM-B simulations is tested by means of the full extent of the footprint, its peak location, peak value, and its crosswind dispersion. Performance metrics show that for all stability classes (convective, neutral, and stable scenarios), the footprint parameterisation is able to predict the footprints simulated by the much more sophisticated Lagrangian stochastic particle dispersion model very accurately (Table 4).

Results shown here clearly demonstrate that our objective of providing a short-cut to LPDM-B has been achieved. The full model was tested successfully against wind tunnel data (Kljun et al., 2004a). Further, the dispersion core of LPDM-B was evaluated successfully against wind tunnel and water tank data, large eddy simulations, and a full-scale tracer experiment (Rotach et al., 1996). These considerations lend confidence to the validity of LPDM-B and thus FFP. They suggest that, despite its simplicity, FFP is suitable for a wide

range of real-world applications, and is fraught with much less restrictive assumptions and turbulence regime limitations than what most other footprint models are faced with. We have applied the new scaling aproach to LPDM-B, but it is likely applicable similarly to other complex footprint models.

For the calculation of footprints with FFP, the values of the input parameters z_m , $\overline{u}(z_m)$, u_* , L, and σ_v can be derived from measurements typically available from flux towers. Input values for the roughness length, $z_{0,}$ may be derived from turbulence measurements or estimated using the mean height of the roughness elements (e.g., Grimmond and Oke, 1999). In the case of not perfectly homogeneous surfaces, these z_0 values may vary depending on wind direction (see also Sect. 5.4). Measurements of the boundary layer height, h_x are available only rarely, and the accuracy of estimates of h may vary substantially. In the following, we hence evaluate the sensitivity of the footprint parameterisation on the input parameters z_0 and h.

The sensitivity of the FFP derived footprint estimate to changes in h and z_0 by ± 5 , ± 10 , and $\pm 20\%$ is tested for all scenarios of Table 2. For all scenarios, even changes of 20% in h and z_0 result in only minor shifts or size alterations of the footprint (Table 5). As to be expected, a small variation in the input value of the boundary layer height, h, does hardly alter footprint estimates for stability regimes with large h, namely convective and neutral regimes. This finding is rather convenient, as reliable estimates of h are difficult to derive for convective stabilities (see Appendix B). For stable scenarios, the footprint peak location is shifted closer to the receptor for overestimated h and shifted further from the receptor for underestimated h. For these cases, overestimated h will also very slightly increase the width of the footprint as described by σ_y and vice versa. The impact of variations in the roughness length is quite similar for all atmospheric conditions, slightly decreasing the footprint extent for overestimated z_0 . Changes of the roughness length do not directly impact σ_y but the absolute value of the footprint f(x, y) can still vary, as a result of imposed changes in $\overline{f^y}(x)$ (cf. Eq. 10).

6.2 Limitations of FFP

Since FFP is based on LPDM-B simulations, LPDM-B's application limits are also applicable to FFP. As for most footprint models, these include the requirements of stationarity and horizontal homogeneity of the flow over time periods that are typical for flux calculations (e.g., 30-60 min). If applied outside these restrictions, FFP will still provide footprint estimates, but their interpretation becomes difficult and unreliable. Similarly, LPDM-B does not include roughness sublayer dispersion near the ground, nor dispersion within the entrainment layer at the top of the Convective Boundary Layer. Hence, we suggest limiting FFP simulations to measurement heights above the roughness sublayer and below the entrainment layer (e.g., for airborne flux measurements). The Π functions of the scaling procedure also set some limitations to the presented footprint parameterisation (see below). Further, the presented footprint parameterisation has been evaluated for the range of parameters of Table 1 and application outside this range should be considered with care. For calculations of source areas of fractions *R* of the footprint, we suggest $R \leq 0.9$ (note that the source area for R = 1 is infinite). In most cases, R = 0.8 is sufficient to estimate the area of the main impact to the measurement.

The requirements and limits of FFP for the measurement height and stability mentioned above can be summarised as follows:

20 $z_0 < z_{\sf m} < h_{\sf e}$	
$-15.5 \leq rac{z_{m}}{L}$,	(27)

where 20 z_0 is of the same order as the roughness sublayer height, z_* (see Sect. 2), and h_e is the height of the entrainment layer (typically, $h_e \approx 0.8h$, e.g., Holtslag and Nieuwstadt, 1986). Eq. (27) is required by Π_4 for a measurement height just above z_* and may be adjusted for different values of z_* . At the same time, Eq. (27) also restricts application of the footprint parameterisation for very large measurement heights in strongly convective situations. For such cases, scaled footprints of LPDM-B simulations are of slightly shorter extent than those of the parameterisation and also include small contributions to the footprint from

downwind of the receptor location (see Fig. 2). To account for such conditions, we suggest FFP parameters specific to the strongly convective stability regime (see Appendix A).

6.3 Comparison with other footprint models

In the following, we compare footprints of three of the a most commonly used models with results of FFP: the parameterisation of Hsieh et al. (2000) with crosswind extension of Detto et al. (2006), the model of Kormann and Meixner (2001), and the footprint parameterisation of Kljun et al. (2004b), hereinafter denoted HKC00, KM01, and KRC04, respectively.

For the comparison, the three above models and FFP were run for all scenarios listed in Table 1. As mentioned earlier, these scenarios span stability regimes ranging from the Mixed Layer (ML), Free Convection Layer (FC), Surface Layer (SL, here further differentiated into convective, c, neutral, n, and stable, s), the Neutral Layer (NL), Z-less Scaling Layer (ZS), and finally Local Scaling Layer (LS). The wide range of stability regimes means that, unlike FFP, HKC00 and KM01 were in some cases run clearly outside their validity range. As, in practice, footprint models are run outside of their validity range quite frequently when they are applied to real environmental data, these simulations are included here.

Figure 6 shows the upwind extents of 80% of the crosswind-integrated footprint (x_{80}) of these simulations of HKC00 against the corresponding results of FFP. Clearly, HKC00's footprints for neutral and stable scenarios extend further from the receptor than corresponding FFP's footprints by a factor of 1.5 to 2. This is the case for scenarios outside and within the Surface Layer. The results show most similar footprint extents for the convective part of the Surface Layer regime. In contrast, HKC00's footprints for elevated measurement heights within the Free Convection Layer and footprints within the Mixed Layer are of shorter extent. The peak locations of the footprints (not shown) exhibit very similar behaviour to their 80% extent. HKC00's estimates are again larger than that of FFP for most scenarios except for Mixed Layer and Free Convection conditions; this is also found at half and at twice the peak location (not shown).

The alongwind extents of the footprint predictions of KM01 are very similar to HKC00's results, and hence the comparison of KM01 against FFP is similar as well: larger footprint extents resulting from KM01 than from FFP in most cases except for Free Convection and Mixed Layer scenarios, where FFP's footprints extend further (Fig. 7). Again, the peak location of the footprints also follow this pattern (not shown). Kljun et al. (2003) have discussed possible reasons for differences between KM01 and KRC04, relating these to LPDM-B capabilities of modelling alongwind dispersion that is also included in KRC04, but not in KM01. These reasons also apply to FFP. For crosswind dispersion, results of KM01 and FFP are relatively similar at the peak location of the footprint, x_{max} (Fig. 7). Differences are most evident for the neutral Surface Layer and for measurement heights above the Surface Layer. Nevertheless, the shape of the two-dimensional footprint is different between the two models. For most scenarios, the footprint is predicted to be wider by KM01 downwind of the footprint peak, and for scenarios within SL_c and FC it is predicted to be narrower upwind of the peak (not shown).

KRC04 and FFP were both developed on the basis of LPDM-B simulations. Hence, as expected, the results of these two footprint parameterisations agree quite well (Fig. 8). FFP suggests that footprints extend slightly further from the receptor than KRC04 does, the difference is increasing with measurement height. FFP and KRC04 footprint predictions clearly differ for elevated measurement heights within the Neutral Layer, Local Scaling, and Z-less Scaling scenarios, which is due to the improved scaling approach of FFP. The footprint peak locations are predicted to be further away from the receptor by KRC04 than by FFP, with the difference decreasing for increasing measurement height (not shown).

To date, the availability of observational data suitable for direct evaluation of footprint models is very limited, and hence the performance of footprint models cannot be tested against "the truth". Nevertheless, as stated in Sect. 6.1, LPDM-B and its dispersion core, the basis for FFP, have been evaluated successfully against experimental data, supporting the validity of FFP results.

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Flux footprint models describe the area of influence of a turbulent flux measurement. They are typically used for the design of flux tower sites, and for the interpretation of flux measurements. Over the last decades, large monitoring networks of flux tower sites have been set up to study greenhouse gas exchanges between the vegetated surface and the lower atmosphere. These networks have created a great demand for footprint modelling of longterm data sets. However, to date available footprint models are either too slow to process such large data sets, or are based on too restrictive assumptions to be valid for many realcase conditions (e.g., large measurement heights or turbulence conditions outside Monin-Obukhov scaling).

In this study, we present a novel scaling approach for real-scale two-dimensional footprint data from complex models. The approach was applied to results of the backward Lagrangian stochastic particle dispersion model LPDM-B. This model is one of only few that have been tested against wind tunnel experimental data. LPDM-B's dispersion core was specifically designed to include the range from convective to stable conditions and was evaluated successfully using wind tunnel and water tank data, large eddy simulation and a field tracer experiment.

The scaling approach forms the basis for the two-dimensional flux footprint parameterisation FFP, as a simple and accessible short-cut to the complex model. FFP can reproduce simulations of LPDM-B for a wide range of boundary layer conditions from convective to stable, for surfaces from very smooth to very rough, and for measurement heights from very close to the ground to high up in the boundary layer. Unlike any other current fast footprint model, FFP is hence applicable for day and night time measurements, for measurements throughout the year, and for measurements from small towers over grassland to tall towers over mature forests, and even for airborne surveys.

Appendix A: Footprint parameterisation optimised for specific stability conditions

There may be situations where footprint estimates are needed for only one specific stability regime, for example, when footprints are calculated for only a short period of time, or for a certain daytime over several days. For such cases, it may be beneficial to use footprint parameterisation settings optimised for this stability regime only. While scaled footprint estimates for neutral and stable conditions collapse to a very narrow ensemble of curves, footprints for strongly convective situations may also include contributions from downwind of the receptor location. For neutral and stable conditions, a specific set of fitting parameters for FFP has been derived using the LPDM-B simulations of Scenarios 4 to 6 (Table 1). For convective conditions, additional LPDM-B simulations to Table 1 (Scenarios 1 to 3) have been included, to represent more strongly convective situations. These simulations (Scenario 1*) were run for the same set of receptor heights and surface roughness length as listed in Table 1, but with $u_* = 0.2 \text{ m s}^{-1}$, $w_* = 2.0 \text{ m s}^{-1}$, L = -5 m, and h = 2000 m. The resulting values for the parameters a, b, c, and d for the crosswind-integrated footprint parameterisation, and a_c , b_c , and c_c for the crosswind dispersion parameterisation are listed in Table 6.

Please note that when applying these fitting parameters, the footprint functions for convective and neutral/stable conditions will not be continuous. We hence suggest to use the universal fitting parameters of Eqs. (17) and (19) for cases where a transition between stability regimes may occur.

Appendix B: Derivation of the boundary layer height

Determination of the boundary layer height, h, is a delicate matter, and no single "universal approach" can be proposed. Clearly, any available nearby observation (e.g., from LiDAR or radio sounding) should be used. h may also be diagnosed from assimilation runs of high-resolution numerical weather predictions. For unstable (daytime) conditions, Seibert et al. (2000) give a comprehensive overview on different methods and discuss the associated

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caveats and uncertainties. For stable conditions, Zilitinkevich et al. (2012) and Zilitinkevich and Mironov (1996) provide a theoretical assessment of the boundary layer height under various limiting conditions. If none of the above measurements or approaches for h are applicable, a so-called "meteorological pre-processor" may be used. A non-exhaustive suggestion for the latter is provided in the following.

For stable and neutral conditions there are simple diagnostic relations with which the boundary layer height can be estimated. Nieuwstadt (1981) proposed an interpolation formula for neutral to stable conditions:

$$h = \frac{L}{3.8} \left[-1 + \left(1 + 2.28 \frac{u_*}{fL} \right)^{1/2} \right],$$
(B1)

where *L* is the Obukhov length $(L = -u_*^3\overline{\Theta}/(kg(\overline{w'\Theta'})_0))$, $\overline{\Theta}$ is the mean potential temperature, k = 0.4 the von Karman constant, *g* the acceleration due to gravity, $(\overline{w'\Theta'})_0$ the surface (kinematic) turbulent flux of sensible heat, and $f = 2\Omega sin\phi$ is the Coriolis parameter (ϕ being latitude and Ω the angular velocity of the Earth's rotation). Eq. (B1) is widely used in pollutant dispersion modelling (e.g., Hanna and Chang, 1993) and has the desired property to have limiting values corresponding to theoretical expressions. For large *L* (i.e., approaching near-neutral conditions), Eq. (B1) tends towards

$$h_n = c_n \frac{u_*}{|f|}.$$
(B2)

In their meteorological pre-processor, Hanna and Chang (1993) recommend $c_n = 0.3$ corresponding to Tennekes (1973). Strictly speaking, Eq. (B2) is valid only as long as the stability of the free atmosphere is also close to neutral, i.e. $10 < N|f|^{-1} < 70$, where N is the Brunt-Väisälä frequency above the boundary layer defined as $N = (g/\overline{\Theta} d\Theta/dz)^{1/2}$ (Zilitinkevich et al., 2012). If this is not the case, but L is still very large, using $c_{nn} = 1.36$ the asymptotic limit becomes (Zilitinkevich et al., 2012)

$$h_{\underline{n}\underline{n}} = c_{nn} \frac{u_*}{|fN|^{1/2}} \,. \tag{B3}$$

For strongly stable conditions, Eq. (B1) approaches

$$h_s = c_s \left(\frac{u_*L}{|f|}\right)^{1/2},\tag{B4}$$

as already proposed by Zilitinkevich (1972) who later termed this equation an "intermediate asymptote" for the more complete asymptotic expression derived for the stable boundary layer height by Zilitinkevich and Mironov (1996). They assign Eq. (B4) to an applicability range of $4 \ll u_*L/|f| \ll 100$. The numerical parameters in Eq. (B1) suggest $c_s \approx 0.4$ for the limit of very strong stability. Zilitinkevich and Mironov (1996) suggested $c_s \approx 0.63$ and Zilitinkevich et al. (2007) later proposed $c_s \approx 0.3$ based on LES results (here, both values are adapted for the above definition of L).

For convective conditions, the boundary layer height cannot be diagnosed due to the nearly symmetric diurnal cycle of the surface heat flux. It must therefore be integrated employing a prognostic expression, and starting at sunrise (before the surface heat flux first becomes positive) when the initial height is diagnosed using one of the above expressions. The slab-model of Batchvarova and Gryning (1991) is based on a simplified TKE (turbulence kinetic energy) equation including thermal and mechanical energy. The resulting rate of change for the boundary layer height is implicit in h and may be solved iteratively or using $h(t_i)$ to determine the rate of change to yield $h(t_{i+1})$:

$$\frac{\mathrm{d}h}{\mathrm{d}t} = \frac{(\overline{w'\Theta'})_0}{\gamma} \left[\left(\frac{h^2}{(1+2A)h - 2BkL} \right) + \frac{Cu_*^2 T}{\gamma g[(1+A)h - BkL]} \right]^{-1}.$$
(B5)

Here, γ is the gradient of potential temperature above the Convective Boundary Layer (CBL). The latter is often not available for typical applications and can be approximated by a constant parameter (e.g., $\gamma \approx 0.01 \,\mathrm{K \, m^{-1}}$, a typical mid-latitude value adopted from Batchvarova and Gryning, 1991). It must be noted, however, that dh/dt in Eq. (B5) is quite sensitive to this parameter. The model parameters, finally, A = 0.2, B = 2.5, and C = 8, are derived from similarity relations in the CBL that have been employed to find the growth rate of its height.

Discussion Paper

Appendix C: Addressing the finite nature of stochastic particle dispersion footprint models

For the parameterisation of the scaled footprints, using continuous functions, we need to address an issue that arises from the discrete nature of LPDM-B. Like in all stochastic particle dispersion models, the number of particles (*n*) released is necessarily finite. Despite a large *n* (typically, $n \sim 10^6$ for simulations of this study), the distribution of particle locations is also finite, with a finite envelope. Hence, estimates of dispersion statistics become spurious near the particle envelope. In particular, the touchdown distribution statistics that form the basis of footprint calculations are truncated in close vicinity of the receptor, creating a "blind zone" of the footprint. The extent of this blind zone is related to the finite time, *T*, a particle takes to travel the vertical distance between source/sink and the receptor at z_m . As the vertical dispersion scales with u_* , *T* can be expressed as $T = p_{s2} z_m/u_*$ where p_{s2} is again a proportionality factor depending on stability. In effect, no particle touchdown can be scored closer to the receptor than the horizontal travel distance for time *T*.

For the crosswind-integrated footprint, mean advection of the particle plume over time T is the principal effect of the blind zone. This effect can be accounted for by a shift in X^* by a constant distance, d, which is treated as a free parameter and determined by the fitting routine. For the crosswind dispersion of the footprint, the effect of the blind zone needs to be corrected for by the contribution to crosswind dispersion over time T, which is not accounted for in the source/sink particle touchdown distribution of LPDM-B. This contribution to the dispersion can be estimated as $\sigma_{y,0} = \sigma_v * T$, in accordance with Taylor's classical results for the near-source limit (Taylor, 1921). Hence σ_y of Eq. (10) becomes $\sigma_y = \sigma_{y,0} + \sigma_{y,\text{res}}$ where the latter is the crosswind dispersion explicitly resolved by LPDM-B. B. Based on LPDM-B results, we set $p_{s2} = 0.35$, 0.30.35, 0.5 for convective (L < 0), neutral ($L \to \infty$), and stable conditions (L > 0), respectively.

Appendix D: Derivation of relative contribution to total footprint area

For the integration of the footprint parameterisation $\hat{F}^*(\hat{X}^*)$ to an upper limit at $\hat{X}_{*,R}$, we introduce the auxiliary variables $x_d = \hat{X}_* - d$ and $r = \hat{X}_{*,R} - d$. With that, and based on Eq. (15), the integral of the footprint parameterisation up to r can be expressed as

$$R = \int_{d}^{X_{*,R}} \hat{F}^{*}(\hat{X}^{*}) d\hat{X}^{*} = \int_{0}^{r} a(x_{d})^{b} \exp\left(\frac{-c}{x_{d}}\right) dx_{d}.$$
 (D1)

Substituting c/x_d with t, the above integral can be solved as follows

$$R = \int_{\infty}^{c/r} a \left(\frac{c}{t}\right)^{b} \exp(-t) \frac{-c}{t^{2}} dt$$

$$= a c^{b+1} \int_{c/r}^{\infty} t^{-b-2} \exp(-t) dt$$

$$= a c^{b+1} \Gamma(-b-1, c/r)$$

$$= a c^{b+1} \Gamma(-b-1, \frac{c}{\hat{X}_{*,R} - d}).$$
(D3)

Here, $\Gamma(-b-1, c/(\hat{X}_{*,R}-d))$ is the upper incomplete gamma function defined as $\Gamma(s,l) \equiv \int_{l}^{\infty} t^{s-1} \exp(-t) dt$. As $b = -1.991 \approx -2$, $a \approx c$ (Eq. 17), and $c^{b+1} \approx c^{-1}$, Eq. (D2) can be further simplified to

$$\begin{split} R &\approx \int_{c/r}^{\infty} \exp(-t) \, \mathrm{d}t \\ &= \exp\left(\frac{-c}{r}\right) = \exp\left(\frac{-c}{\hat{X}_{*,R} - d}\right). \end{split}$$

(D4)

Code availability

The code of the presented two-dimensional flux footprint parameterisation FFP and the crosswind-integrated footprint can be obtained as a supplement to this publication and from www.footprint.kljun.net. It The code is available in several different platform-independent programming languages, including an app for mobile devices. Updated versions will be freely available at . On . Check the same webpage , for an online version of the footprint parameterisation is available and for updates.

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Table 1. Velocity scales (friction velocity, u_* , and convective velocity scale, w_*), Obukhov length (L), and planetary boundary layer height (h) characterising the stability regimes of LPDM-B simulations at measurement height z_m and with roughness length z_0 . Cases with measurement height within the roughness sublayer were disregarded (see text for details).

Scenario		$u_* [{ m ms^{-1}}]$	$w_* [{ m ms^{-1}}]$	<i>L</i> [m]	h [m]
1	convective	0.2	1.4	-15	2000
2	convective	0.2	1.0	-30	1500
3	convective	0.3	0.5	-650	1200
4	neutral	0.5	0.0	∞	1000
5	stable	0.4	-	1000	800
6	stable	0.4	-	560	500
7	stable	0.3	_	130	250
8	stable	0.3	-	84	200

Receptor heights at $z_m/h = [0.005, 0.01, 0.075, 0.25, 0.50]$ Roughness lengths $z_0 = [0.01, 0.1, 0.3, 1.0, 3.0]$ m

Scenario		$u_* [\mathrm{ms^{-1}}]$	$w_* [{ m ms^{-1}}]$	<i>L</i> [m]	h [m]	
10	convective	0.20	1.00	-50	2500	
11	convective	0.20	0.80	-100	2500	
12	convective	0.25	0.75	-200	2160	
15	neutral	0.40	0.00	∞	800	
13	neutral	0.60	0.00	∞	1200	
14	neutral	0.80	0.00	∞	1600	
16	stable	0.30	_	200	310	
17	stable	0.50	_	100	280	
18	stable	0.35	-	50	170	
$[z_m, z_0] = [20 \text{ m}, 0.05 \text{ m}], [30 \text{ m}, 0.5 \text{ m}], [50 \text{ m}, 0.05 \text{ m}]$						

Table 2. Velocity scales (u_*, w_*) , Obukhov length (L), planetary boundary layer height (h) describing the stability regimes of LPDM-B simulations for evaluation of the footprint parameterisation at measurement heights z_m and with roughness lengths z_0 .

Table 3. Performance of the footprint parameterisation evaluated against all (200) scaled footprints of LPDM-B simulations as in Table 1. Performance of the crosswind-integrated footprint parameterisation was tested against the complete footprint curve (F^{y*}) , the footprint peak location (X^*_{\max}) , and the footprint peak value (F^{y*}_{\max}) . The parameterisation for crosswind dispersion $(\hat{\sigma}^*_y)$ was similarly tested against $\sigma^*_y(x)$ for all scaled footprints. In all cases the following performance measures were used: Pearson's correlation coefficient (R), fractional bias (FB), fraction of the parameterisation within a factor of two of the scaled footprints (FAC2), geometric variance (VG), and normalised mean square error (NMSE). Note that R is not evaluated for X^*_{\max} and F^{y*}_{\max} as the footprint parameterisation provides a single value for each of these.

Performance metrics	F^{y*}	X^*_{\max}	F^{y*}_{\max}	σ_y^*
R	0.96	_	_	0.90
FB	0.022	0.050	0.008	- 0.006 0.120
FAC2	0.71	1.00	1.00	1.00
VG	2.86	1.04	1.05	1.02
NMSE	0.48	0.05	0.05	0.02

Table 4. Performance of the footprint parameterisation evaluated against the second set of LPDM-B footprints of Table 2 (9 simulations for each stability regime), in real scale. Performance of the crosswind-integrated footprint parameterisation was tested against the crosswind-integrated footprint curve $(\overline{f^y})$, the footprint peak location (x_{\max}) , the footprint peak value $(\overline{f^y}_{\max})$, and the standard deviation of the crosswind distance at the peak location $(\sigma_y(x_{\max}))$. See Table 3 for abbreviations of performance measures.

Performance metrics	$\overline{f^y} [{ m m}^{-1}]$	$x_{\sf max} [{\sf m}]$	$\overline{f^y}_{\max} [\mathrm{m}^{-1}]$	$\sigma_y(x_{\sf max})$ [m]			
Convective scenarios 10, 11, 12							
R	0.97	0.99	0.97	0.99			
FB	0.014	0.109	-0.063	0.125			
FAC2	0.99	1.00	1.00	1.00			
VG	43.36	1.06	1.02	1.07			
NMSE	0.33	0.09	0.03	0.07			
Neutral scenarios 13,	14, 15						
R	0.97	0.99	0.96	0.37 0.47			
FB	0.020	0.174	-0.067	0.008 0.05			
FAC2	0.99	1.00	1.00	1.00			
VG	1.62	1.11	1.04	1.13 1.12			
NMSE	0.27	0.22	0.03	0.13 0.12			
Stable scenarios 16, 17, 18							
R	0.99	0.99	0.99	0.88			
FB	0.020	0.092	0.000	-0.013			
FAC2	0.89	1.00	1.00	1.00			
VG	1.16	1.03	1.03	1.02			
NMSE	0.09	0.13	0.01	0.03			

Table 5. Sensitivity of footprint peak location (x_{max}) , peak value $(\overline{f^y}_{max})$ and the standard deviation of the crosswind distance at the peak location $(\sigma_y(x_{max}))$ of the footprint parameterisation FFP to changes of the input parameters h (boundary layer height) and z_0 (roughness length) by ± 5 , ± 10 , ± 20 % for all scenarios of Table 2, in real scale. Changes are denoted in % deviation from the footprint parameterisation for the original input values of Table 2.

Change in input [%]	Δx_{\max} [%]	$\Delta \overline{f^y}_{max}$ [%]	$\Delta \sigma_y(x_{\max})$ [%]				
Convective scenarios 10, 11, 12							
h ± 5	∓0.1	±0.1	0.0				
h ± 10	∓0.1	±0.1	0.0				
h ±20	∓0.3	±0.3	0.0				
z_0 ± 5	±	±1.1	0.0				
<i>z</i> ₀ ±10	2.2	±2.2	0.0				
<i>z</i> ₀ ±20	∓4.4	±4.3	0.0				
Neutral scenarios 13	, 14, 15						
h \pm 5	∓0.2	±0.2	0.0				
h ±10	∓0.3	\pm 0.3	0.0				
h \pm 20	∓0.7	\pm 0.7	0.0				
<i>z</i> ₀ ±5	∓0.9	\pm 0.9	0.0				
<i>z</i> ₀ ±10	∓1.9	±1.9	0.0				
<i>z</i> ₀ ±20	∓3.8	±3.7	0.0				
Stable scenarios 16, 17, 18							
h \pm 5	∓0.9	±0.9	±0.1				
h \pm 10	1.8	±1.7	±0.2				
h \pm 20	∓3.7	±3.6	±0.4				
<i>z</i> ₀ ±5	∓0.7	± 0.7	0.0				
<i>z</i> ₀ ±10	∓1.4	±1.4	0.0				
<i>z</i> ₀ ±20	∓2.8	±2.8	0.0				

Table 6. Fitting parameters of the crosswind-integrated footprint parameterisation and of the crosswind footprint extent for a "universal" regime (Scenarios 1 to 9), and for specifically convective (Scenarios 1* and 1 to 3) or neutral and stable regimes (Scenarios 4 to 9). For each scenario, all measurement heights and roughness lengths were included. See Table 1 and Appendix A for a description of the scenarios.

Stability regime	a	b	С	d	a_{c}	b_{c}	c_{c}
Universal		-1.991		0.136			20.0
Convective	2.930	-2.285	2.127	-0.107	2.11	1.59	20.0
Neutral and stable	1.472	-1.996	1.480	0.169	2.22	1.70	20.0

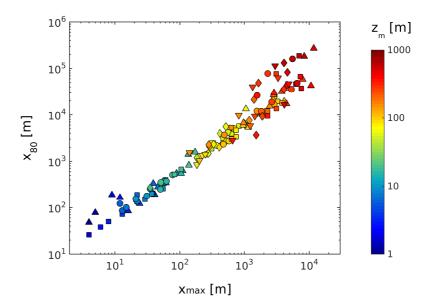


Figure 1. Range of peak locations (x_{max}) and extent of 80 % crosswind-integrated footprints (x_{80}) of LPDM-B simulations as in Table 1. The color depicts the simulated measurement heights, symbols stand for modelled roughness lengths, $z_0 = 0.01 \text{ m} (\triangle)$, $0.1 \text{ m} (\Box)$, $0.3 \text{ m} (\circ)$, $1.0 \text{ m} (\diamondsuit)$, $3.0 \text{ m} (\bigtriangledown)$. Note the use of the log scale to accommodate the full range of the simulations.

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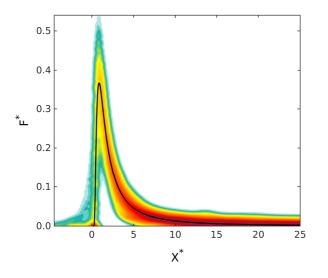


Figure 2. Density plot of scaled crosswind-integrated footprints of LPDM-B simulations as in Table 1 (low density: light blue; high density, 100 times denser than low density: dark red). The footprint parameterisation $\hat{F}^{y*}(\hat{X}^*)$ (cf. Eq. 14) is plotted as black line.

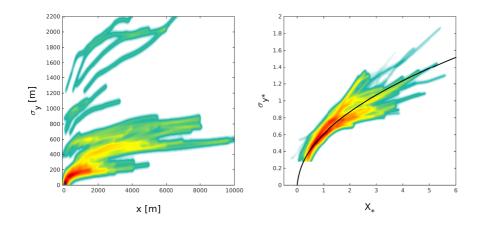


Figure 3. Density plot of real-scale (left panel) and scaled (right panel) lateral dispersion of LPDM-B simulations as in Table 1; low density: light blue, high density (100 times denser than low density): dark red. The parameterisation $\hat{\sigma}_y^*(\hat{X}^*)$ (cf. Eq. 18) is plotted as black line.

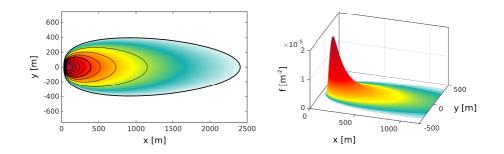


Figure 4. Example footprint estimate for the convective Scenario 1 of Table 1, a measurement height of 20 m, and a roughness length of 0.01 m. The receptor is located at (0/0) m and the *x*-axis points towards the main wind direction. Footprint contour lines (left panel) are shown in steps of 10 % from 10 to 90 %.

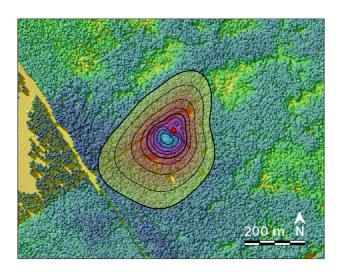


Figure 5. Example footprint climatology for the ICOS flux tower Norunda, Sweden, for 1–31 May 2011. The red dot depicts the tower location with a receptor mounted at $z_{m} = 12 z_{m} = z_{receptor} - z_{d} = 12$ m. Footprint contour lines are shown in steps of 10% from 10 to 90%. The background map is tree height derived from an airborne LiDAR survey.

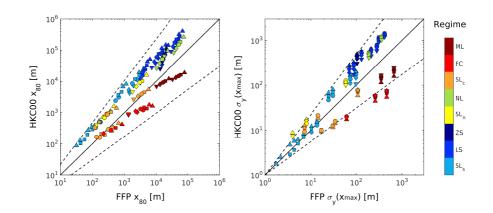


Figure 6. Comparison of FFP simulations for scenarios of Table 1 with corresponding simulations of the model (HKC00) of Hsieh et al. (2000). Plotted are the extent of 80% crosswind-integrated footprints, x_{80} (left panel), and the crosswind dispersion at the footprint peak location, $\sigma_y(x_{max})$ (right panel). The color depicts the stability regime of the simulation, ML being Mixed Layer, FC Free Convection Layer, SL the Surface Layer (c for convective, n for neutral, and s for stable), NL Neutral Layer, ZS Z-less Scaling, and LS Local Scaling (see Holtslag and Nieuwstadt, 1986, for more details). Symbols denote modelled roughness lengths, $z_0 = 0.01 \text{ m} (\Delta)$, $0.1 \text{ m} (\Box)$, $0.3 \text{ m} (\circ)$, $1.0 \text{ m} (\diamondsuit)$, $3.0 \text{ m} (\bigtriangledown)$, and dashed lines denote 2:1 and 1:2, respectively. Note the use of the log-log scale to accommodate the full range of the simulations.

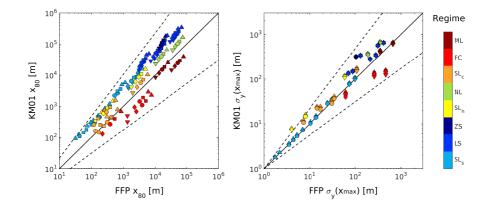


Figure 7. Same as Fig. 6 but for results of FFP compared with corresponding simulations of the model (KM01) of Kormann and Meixner (2001).

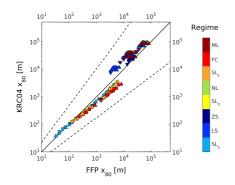


Figure 8. Comparison of FFP simulations for scenarios of Table 1 with corresponding simulations of the footprint parameterisation (KRC04) of Kljun et al. (2004b). Plotted is the extent of 80% crosswind-integrated footprints (x_{80}). The color depicts the stability regime of the simulation and symbols denote modelled roughness lengths (see Fig. 6 for details).