

Abstract

 To spatially co-exist and differentially specify fates within developing tissues, morphogenetic cues must be correctly positioned and interpreted. Here, we investigate mouse hair follicle development to understand how morphogens operate within closely spaced, fate-diverging progenitors. Coupling transcriptomics with genetics, we show that emerging hair progenitors produce both WNTs and WNT inhibitors. Surprisingly, however, instead of generating a negative feedback loop, the signals oppositely polarize, establishing sharp boundaries and consequently a short-range morphogen gradient that we show is essential for three-dimensional pattern formation. By establishing a morphogen gradient at the cellular level, signals become constrained. The progenitor preserves its WNT signaling identity and maintains WNT signaling with underlying mesenchymal neighbors, while its overlying epithelial cells become WNT-restricted. The outcome guarantees emergence of adjacent distinct cell types to pattern the tissue.

INTRODUCTION

 Embryonic development has long fascinated generations of scientists. Despite years of research, developmental biologists are still puzzled by the remarkable emergence of complex multicellular organisms from single cells. Central to understanding metazoan phenotypic reproducibility is the problem of pattern formation.

 ln the early $20th$ century, biologists began providing a new conceptual framework for understanding how cellular fates are specified during morphogenesis. Initially, it was proposed that depending upon their local concentration, "materials" form gradients that dictate distinct patterning of otherwise uniform cellular sheets (Boveri 1901; T. H. Morgan 1901; Dalcq 1938; Rogers and Schier 2011). This notion began to crystallize in 1952, when Alan Turing applied mathematical modeling to explain how diffusion of two interacting chemical substances could spontaneously produce a pattern from an homogeneous field of cells (A M Turing 1952; Heller and Fuchs 2015).

 Some years later, Lewis Wolpert posited the 'French Flag Problem' to describe a cell's differential gene expression according to its position within a morphogen gradient (Wolpert 1968). He suggested that thresholds of morphogen gradients would establish boundaries that result in distinct cell fates. The 'positional information' model was then proposed to describe how complex patterns emerge from prior asymmetries (Green and Sharpe 2015; Wolpert 1969). The premise is that each cell has a positional value that specifies its position, and it is the interpretation of positional information that dictates cell fate (Wolpert 1989).

 Overall, these early studies popularized the view that morphogens and positional information function centrally in generating the symmetry-breaking events that differentiate cellular fates and drive morphogenesis. Despite these important advances on the establishment of two-dimensional patterns, comparatively little is known about the molecular nature of the positional information needed to generate three-dimensional tissue patterns, or how closely juxtaposed cells within a developing tissue and organ adopt and maintain distinct cellular fates. Here, we tackle this problem by using the emergence of hair follicles in developing mammalian skin as a classical example of three-dimensional patterning in morphogenesis.

 During embryonic development, the first of three spatially positioned arrays of hair placodes emerges when some cells within an epithelial monolayer begin to experience a higher level of WNT signal than their neighbors (DasGupta and Fuchs 1999). Similar to *Drosophila* development, these WNTs act as short-range inducers and long-range organizers. Thus, through either rapid reaction-diffusion (Sick et al. 2006; Glover et al. 2017) or mechanotransduction-mediated mesenchymal self-organization (Shyer 70 et al. 2017), the WNT^{hi} cells within the plane of homogeneous epidermal cells cluster into an array of evenly spaced placodes (Ahtiainen et al., 2014). As placodes form, they produce inhibitory signals such as bone morphogenic proteins (BMPs) that limit placode size and distance placodes from each other (Närhi et al. 2008; Noramly and Morgan 1998a)

 Three dimensional pattern formation begins when WNT signaling reaches a threshold in placode cells, stimulating them to divide perpendicularly relative to the epidermal plane and generating differentially fated progenitor daughters (Ouspenskaia et al. 2016). Intriguingly, these early basal daughters both produce WNTs and respond to WNTs, as exemplified by WNT-reporter activity and nuclear LEF1, a positive-acting downstream DNA binding effector of WNT-stabilized β-catenin (Figure 1A) (Ouspenskaia et al. 2016). Interestingly, the overlying suprabasal daughter displays a paucity of WNT signaling and adopts a new fate, while the dermal condensate beneath the hair bud shows robust WNT signaling. How this positional information is locally and directionally partitioned and how sharp boundaries in WNT signaling are established between neighboring cells has remained elusive.

83 Here, we use mouse genetics to mosaically alter WNT signaling within basal progenitors of embryonic epidermis. By coupling transcriptome analyses with gain and loss of function studies, we unveil a cohort of WNT antagonists whose transcripts are WNT-sensitive and specifically activated in the WNT signaling basal progenitors. While morphogen inhibitors have been typically associated with negative feedback loops that either dampen or impair signaling, we find that even though they produce these inhibitors, basal progenitors still signal through WNTs. Moreover, they appear to do so by differentially polarizing activators and inhibitors to establish a spatially confined gradient within the placode. By perturbing it, we learn that this single-cell length morphogen gradient endows basal progenitors with the ability to orchestrate directional signaling. Progenitors generate a WNT-restricted

microenvironment for their apical daughters, while fueling a basal basement membrane niche that is rich

93 in WNT signaling at the epithelial-mesenchymal border.

RESULTS

Sustained activation of WNT disrupts embryonic skin hexagonal patterning

 In the skin, it is well-established that nuclear LEF1 co-localizes not only with nuclear β-catenin (Fuchs et al. 2001) but also with both *TOPGAL*, a WNT-reporter driven by an enhancer composed of multimerized LEF1 DNA binding sites (DasGupta and Fuchs 1999), and as shown in Figure 1A, *Axin2- LacZ,* a WNT-reporter driven by the endogenous WNT target *Axin2* (Lustig et al. 2002). Thus, in this research, we often used nuclear LEF1 as a proxy for WNT signaling.

 To begin to understand how WNT signaling promotes the symmetry-braking events during skin development, we turned to our powerful *in utero* delivery method (Beronja et al. 2010). This method was superior over prior transgenic methods in that it allowed us to first, manipulate WNT signaling early, while the skin was still a single-layered epithelium, and second, generate mosaic perturbations in the signals that dictate hair follicle patterning (Andl et al. 2002).

 To gain initial insights, we accentuated the WNT signaling response in skin patches by transducing a lentivirus (LV) harboring Cre recombinase into E9.5 mouse embryos floxed for 109 Adenomatous Polyposis Coli (Apc^{t//fl}). As expected from prior Apc loss of function studies on E14.5 embryos (Kuraguchi et al. 2006), mosaic loss of *Apc* resulted in overactivation of β-catenin/WNT signaling in patches of transduced skin (Figure 1B).

112 In contrast to wild-type and/or *Apc^{-/+}* skin, where waves of LEF1+ placodes were patterned equidistantly in hexagonal arrays (Zhou et al. 1995; Cheng et al. 2014), hair follicle patterning was severely perturbed upon mosaic, autonomous over-stabilization of β-catenin (Figure 1C -E). While immunostaining revealed intense nuclear β-catenin as well as nuclear LEF1, *Apc-*null clusters were of random sizes and organization and the clusters never developed into bona fide hair buds. Instead, 117 clusters remained uniform for the natural markers of WNT^{hi} placode cells LEF1, β-catenin and Lhx2, but 118 they failed to generate the WNT^{to} suprabasal cells that characterize the placode to hair bud transition

 (Figure 1 - figure supplement 1A-C). No signs of DNA damage were observed in *Apc-*null clusters as 120 judged by the absence of γ H2AX signal (Figure 1 - figure supplement 2A-B).

https://example.org/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magnitics/magniti clusters appeared to be altogether non-proliferative (Figure 1 - figure supplement 3A-B). Moreover, as illuminated by co-transducing E9.5 embryos with GFP- and RFP-tagged Cre recombinase-expressing lentiviruses, both wild-type placodes and *Apc-*null clusters were multiclonal (Figure 1 - figure supplement 3C), in agreement with the notion that WNT drives the organization of non-dividing cells into placodes within the epidermal plane (Ahtiainen et al. 2014). The distinct morphology of *Apc-*null clusters within the epidermis was characterized by a loss of E-cadherin but not P-cadherin (Figure 1 - figure supplement 4A- B), suggestive of a collective cell sorting mechanism dependent on sustained WNT activation. Integrin β4 was also markedly reduced, consistent with an overall loss of polarity in these clusters (Figure 1 - figure 130 supplement 5A-B). Finally, the WNT^{to} (LEF1-negative) regions surrounding *Apc-*null clusters occupied a much greater than normal radius (Figure 1C). Taken together, our mosaic data revealed that when WNT signaling becomes too high, neighboring cells become too low for WNT signaling, sharpening the 133 boundary between WNT^{hi} and WNT^{\circ} cells and disrupting hair follicle patterning.

Sustained WNT activation is characterized by a gene expression signature rich in WNT inhibitors

 The results so far were suggestive of the existence of an opposing morphogen gradient within the developing skin. To search for these putative morphogenic cues, we added a fluorescent eGFP WNT- reporter to our LV-Cre lentiviral construct, so that we could use fluorescence activated cell sorting 139 (FACS) to isolate and transcriptionally profile independent replicates of WNT-reporter^{hi} and WNT-140 reporter^{lo} cells from transduced *Apc-*null, *R26tdTomato* embryos (Figure 2A; Figure 2 - figure supplement 1A and B).

 When compared to their heterozygous counterparts, WNT-reporter^{hi} epidermal progenitors (α6 integrin⁺) that were null for *Apc,* displayed robust upregulation (Log2 Fold Change ≥1.5, p<0.05) of established WNT-target genes, e.g. *Axin2, Twist1/2* and *Bmp4*, as well as transcripts associated with WNT signaling, cell-cell signaling, cancer, epithelial-mesenchymal transition and cell adhesion (Figure

146 2B-D and Figure 2 - figure supplement 2). Similar analysis of WNT-reporter^{lo} progenitors revealed that expression of these genes was highly sensitive to cellular WNT-reporter levels, and therefore levels of WNT signaling. Intriguingly, WNT signaling sensitive genes encoded not only WNT-activators but also WNT-inhibitors, including NOTUM, WIF1, DKK4 and APCDD1.

 Notably, the levels of WNT target gene expression were always higher in *Apc-*null than in non- phenotypic *Apc-*heterozygous cells, consistent with their overall ectopically higher levels of β-catenin (Figure 2D). Thus, it was important to verify that the WNT-sensitive genes we unearthed were relevant to normal hair follicle development.

WNT signaling cells from developing hair follicles express high levels of WNT inhibitors

 Because our lentiviral transducing strategy is not specific for placodes and the whole skin epithelium becomes transduced upon lentiviral delivery (Beronja et al., 2010), we devised a precise 158 strategy to isolate a pure population of WNThi signaling cells specifically from developing hair follicles. To do so, we crossed otherwise wild-type *Lhx2-GFP* and Fucci (mKO2Cdt1) mice (Ouspenskaia et al. 2016) 160 and FACS-purified and profiled their slow-cycling, WNThi signaling basal hair bud progenitors (α 6-161 integrin^{hi}LHX2^{hi}mKO2⁺) (Figure 3A; Figure 3 - figure supplement 1A). Indeed, not only was this wild-type population WNT-reporter active (Figure 3 - figure supplement 1B), but in addition, the transcriptome 163 overlapped appreciably with that of the WNT^{hi} potent *Apc-*null cells (Figure 3B; Figure 3 - figure supplement 1C).

 Most notably, WNT signaling activators and inhibitors fell within the overlap (Figure 3 - figure supplement 2). As confirmed by *in situ* hybridization, many of these factors displayed expression 167 specificity for the WNT^{hi} and not WNT^{Io} cells of wild-type epithelial cells (Figure 3C). Overall, the 168 comparative analyses between WNT^{hi} *Apc-null and WNT^{hi} wild-type bud cells underscored the value of* comparing progenitors with different levels of WNT signaling to tease out a physiological WNT-dependent signature.

 Bmp4 was among the genes exhibiting strong WNT signaling dependency (Figure 3 - figure supplement 3A-C). As BMPs are known to inhibit follicle formation, and BMP-inhibitors are known to

 promote it (Noramly and Morgan 1998b; Lu et al. 2016), this provided a possible explanation for why the hair follicle-free zone surrounding *Apc-*null clusters was increased (Figure 1C). Indeed, nuclear pSMAD1/5/9, a proxy for BMP4 signaling, persisted multiple cell layers away from *Apc-*null clusters (Figure 3 - figure supplement 3C). Moreover, when over-expressed mosaically, BMP suppressed hair bud formation within adjacent regions of wild-type skin, accompanied by aberrant expansion of pSMAD1/5/9 (Figure 3 - figure supplement 3D-G). These findings support the notion that BMP4 acts in a long-range, negative feedback loop and is responsible for creating a bud-free environment around WNT-specified hair buds, which are driven by BMP inhibitors.

 By contrast, and as previously reported for intestine (Farin et al. 2016), WNTs seemed to function locally, since despite marked elevation of WNT10B within *Apc-*null clusters, immunostaining did not reveal signs of long-range expansion of nuclear β-catenin/LEF1 or WNT inhibitors (NOTUM and WIF1) into surrounding wild-type skin (Figure 3 – figure supplement 4A and B). Probing deeper into the possible functions of these counter-acting positive and negative WNT morphogens (Langton, Kakugawa, and Vincent 2016) under more physiological conditions, we continued our focus on WNT10B, NOTUM and WIF1.

WNT ligands and WNT inhibitors are oppositely polarized by WNT signaling cells from the developing hair follicles

 To track WNT inhibitors during hair follicle development, we investigated the cellular localization of their endogenous proteins at E15.5. At this time, there were three ongoing, staggered waves of hair follicle morphogenesis, enabling simultaneous capturing of placode, bud/germ and peg stages. Strikingly, WIF1 localized at the apical side of the basal cells of placode, bud and germs (Figure 4A and B). WIF1's apical localization in hair germs was severely impaired by Tunicamycin, suggestive of a role for N- Glycosylation in the preferential apical secretion of WNT inhibitors (Figure 4 - figure supplement 1A) (Scheiffele, Peränen, and Simons 1995). By contrast, the Golgi was organized both apically and basally (Figure 4 - figure supplement 1B).

Like WIF1, endogenous NOTUM also displayed a marked apical localization in basal bud cells

 (Figure 4C). Moreover, consistent with WIF1's role in binding and trapping WNT ligands (Malinauskas et 201 al. 2011), and NOTUM's role in inactivating secreted WNTs through removal of their palmitoleate moiety (Kakugawa et al. 2015), nuclear LEF1 was drastically reduced in the suprabasal bud cells at the interface of this high zone of WNT-inhibitor (Figure 4B and C; white arrows).

 To understand the importance of co-expressing quintessential WNT signaling ligands and inhibitors during hair follicle development, we devised a strategy that would allow us to similarly detect these antagonists: we exposed E9.5 *Krt14rtTA* embryos to lentiviruses harboring doxycycline-inducible expression vectors driving a C-terminal MYC-epitope tagged version of each target (Figure 5A). We added Doxycycline to activate *rtTA* at E13.5 and induce protein expression, and then analyzed at E15.5.

 When ectopically expressed in the interfollicular epidermis, MYC-tagged WIF1 localized uniformly 210 to epidermal cell borders, as detected by either WIF1 or MYC-tag immunofluorescence (Figure 5 - figure supplement 1A). A similar pattern of expression was observed for MYC-tagged NOTUM (Figure 5 - figure supplement 2A). By contrast, in the basal hair bud progenitors, both MYC-tagged inhibitors polarized apically (Figure 5B and C). Apical localization of WIF1-MYC and NOTUM-MYC in the developing hair 214 follicle strikingly paralleled their endogenous localization (Figure 4B and C; Figure 5B and C; Figure 5 – figure supplement 1B; Figure 5 – figure supplement 2B). A similar pattern of apical expression was also observed for APCDD1 and DKK4, inhibitors that prevent WNT receptor signaling (Figure 5 – figure supplement 3A).

 By the hair germ stage, WIF1 was no longer expressed in the dermal condensate (Figure 4B; Figure 5B; Figure 5 - supplement figure 1B), nor was NOTUM at the dermal condensate-epidermal interface (Figure 4C; Figure 5C; Figure 5 - supplement figure 2B). Thus, by polarizing WNT-inhibitors apically in basal hair bud cells, a WNT-inhibitor free zone appeared to be generated at this epithelial- mesenchymal interface (yellow arrowheads, Figure 4B and C). Moreover, the robust presence of nuclear LEF1 both in basal bud cells and in the dermal condensate suggested the presence of active WNT ligands within this inhibitor-free zone. Indeed, in contrast to WNT inhibitors, WNT10B and WNT3 were 225 both preferentially polarized at the basal membrane, as quantified by pixel intensity analyses (Figure 5D; Figure 5 - figure supplement 3).

227 In contrast to the polarization of WNT ligands and WNT inhibitors, Frizzled-10 WNT receptor 228 localized to all borders of the hair germ progenitor cells (Figure 5E). This raised the possibility that the elevation in WNT inhibitors might not be a simple negative feedback loop for WNT signaling (Brandman and Meyer 2008). Rather it appeared to generate a sharp morphogen boundary, permissive for WNT signaling within basal hair bud cells and underlying dermal condensate, but restrictive for WNT signaling in overlying suprabasal bud cells. If so, dual expression but differential localization could explain fate diversification and morphogenesis within the developing hair follicle.

Hair bud progenitors apically polarize WNT inhibitors to protect their own identity and differentially confer WNT signaling to their neighbors.

 To further probe the existence of this putative morphogen gradient across the developing hair follicles, we first devised and implemented a strategy to induce the elevation of either WIF1 or NOTUM in skin epithelial progenitors. In doing so, we observed that WNT inhibitors impaired hair follicle specification and led to a sparser hair coat (Figure 6A; Figure 6 - figure supplement 1A and B-B'). We also used LGK974, which inhibits porcupine, an enzyme necessary for WNT secretion (Liu et al. 2013). Low doses of LGK974 administered to E15.5 skin explants were sufficient to prevent nuclear LEF1 in the 243 normally WNT^{hi} basal hair bud cells. Moreover, the normally WNT^{hi} basal cells adopted the SOX9 fate of the WNT^{Io} suprabasal bud cells, underscoring the importance of the WNT morphogen gradient in fate specification (Figure 6 - figure supplement 2A-C).

246 At higher doses, LEF1 was lost not only from the basal hair bud cells, but also from the dermal condensates, consistent with the higher levels of nuclear LEF1/WNT signaling in the dermal condensate relative to the hair bud (Figure 6 - figure supplement 2D and E). Moreover, when we washed out the low dose porcupine inhibitor, nuclear LEF1 and basal bud progenitor fate was restored, illustrating not only the reversibility of the process, but also the restriction of WNT signaling to the epithelial-dermal condensate boundary (Figure 6 - figure supplement 3A and B).

 The accurate and reproducible response of LEF1 expression to the porcupine inhibitor treatment and its wash-out offered yet another validation of nuclear LEF1 as a *bona fide* proxy for WNT signaling.

 Probing deeper, we transduced embryonic wild-type skin with our WNT-reporter and evaluated the GFP and LEF1 simultaneous expression with other WNT targets. In the basal cells from the developing hair follicle LEF1 perfectly co-localized with TCF1/7, the nuclear effector of WNT signaling. Furthermore 257 WNT-reporter^{hi}, LEF1 positive progenitor cells co-expressed other key WNT signaling pathway components like FZD10 and WIF1 (Figure 6 - figure supplement 4).

 Turning to the physiological relevance of the polarized WNT inhibitors in preventing WNT signaling suprabasally, we again employed *in utero* lentiviral delivery, this time to transduce the embryonic skin with inducible versions of NOTUM and WIF1 that were engineered to harbor the basal targeting domain of aquaporin-4 (AQP4) (Urra et al. 2008) (Figure 6 - figure supplement 5A). By E15.5, transduced (H2BGFP+) hair bud progenitors displayed pronounced basal targeting of these AQP4- tagged WNT-inhibitors (Figure 6B; Figure 6 - figure supplement 5B-E). Quantifications showed that basal targeting was more efficient with NOTUM, and this correlated with a more pronounced reduction in hair follicles. Moreover, as quantified by nuclear LEF1 fluorescence intensity, the nuclear LEF1 signal was significantly decreased in NOTUM-AQP4-induced cells compared to either NOTUM-induced or wild-type cells (Figure 6C). This was particularly clear in mosaic hair buds, where basal progenitors that did not express NOTUM-AQP4-MYC-tag (arrowheads, Figure 6C) were adjacent to their NOTUM-AQP4- 270 transduced counterparts. These manipulations also resulted in an expansion of WNT¹⁰ SOX9 cells, 271 underlying the importance of properly regulating WNT inhibitors in hair follicle morphogenesis (Figure 6D).

 Finally, we tested the functional importance of NOTUM's apical localization by asking whether its 274 depletion would lead to an increase in WNT signaling. By transducing *Notum*^{fl/fl} and *Notum*^{fl/+} R26td *Tomato* embryos with LV-Cre, we found that in the absence of NOTUM, both the proportion of LEF1+ cells and also their nuclear LEF1 signal intensity were significantly increased within developing hair buds (Figure 7A-C). Moreover, the effects of *Notum* ablation were largely confined to the apical region of the hair bud and not the underlying dermal condensate, further underscoring the short range and functional importance of apically localizing WNT inhibitors.

DISCUSSION

 Pattern formation plays near universal roles in tissue morphogenesis. The early developing skin is composed of a single layer of multipotent epithelial progenitor cells that will either stratify and develop into the skin's epidermal barrier or form epithelial placodes to launch hair follicle morphogenesis. Positional cues are important not only to specify the uniform distribution of hair follicles across the tissue, 287 but also to differentiate the cells within each of these mini-organs. In uncovering the existence of an internal WNT morphogen gradient within the earliest progenitors of the hair placode, we have begun to understand how WNT signals can be directionally distributed to neighboring cells to break symmetry and trigger the morphogenetic transition from the two-dimensional early placode to a three-dimensional mini-organ.

 WNT signaling has long been known to be important broadly for regenerative and morphogenetic processes (Petersen and Reddien 2011; Loh, van Amerongen, and Nusse 2016; Clevers, Loh, and Nusse 2014). The presence of inhibitors of the WNT signaling pathway has also long been recognized, and given the oft short-lived nature of WNT signals in development, it has always been assumed that inhibitors function in a negative feedback loop to turn off the signal for the next step in lineage specification. Although the existence of such feedback loops is well-established (Perrimon and McMahon 1999), such a mechanism did not reconcile how WNT signaling remains high in basal hair bud progenitors that also simultaneously express at least four different WNT inhibitors. An additional conundrum was how this WNT expressing, WNT signaling progenitor gives rise to only one daughter cell that retains this status, while the other daughter cell adopts a WNT-restricted state.

 Our findings show that by differentially compartmentalizing WNTs and WNT inhibitors, basal placode progenitors not only maintain both positive and negative WNT morphogens simultaneously, but also directionally target the signals, providing the requisite positional cues to transition from two to three dimensional patterning within the developing tissue. By polarizing WNTs basally, progenitors are able to retain their own WNT signaling as well as that of their underlying mesenchymal neighbors to fuel hair follicle morphogenesis at the dermal-epidermal interface. Conversely, by polarizing WNT inhibitors

 apically, the same hair bud progenitors directionally orchestrate WNT^{to} SOX9+ fate specification of their overlying neighbors to launch the diversification of the epithelial cells within the developing hair follicles (Figure 8).

 During development, the formation of precise boundaries is fundamental to the specification of different cellular compartments. Our findings best fit a model whereby developing hair follicle progenitors 313 use WNTs and WNT inhibitors to build local boundaries. By localizing WNT inhibitors apically, WNThigh 314 progenitors limit the WNT response, preserving their own WNT high signaling identify while simultaneously</sup> preventing their suprabasal daughter from responding to the WNT signal.

 A similar refining mechanism has been previously proposed in the *Drosophila* imaginal disks. In the *wingless* expressing cells of the wing margin, cells that are closer to the dorsoventral boundary are able to repress *wingless* expression in their juxtaposed neighbors through a self-refining mechanism. In this case, however, the mechanism appears to involve NOTCH, whose activity is required for *wingless* expression, which in turn appears to repress NOTCH activity (Rulifson et al. 1996). In the hair follicle, 321 NOTCH signaling has not been detected in the WNT10B+ progenitors, but rather the WNT^{low} differentiating cells (Blanpain et al. 2006). Thus, while the mechanisms seem to be evolutionarily divergent, the functional output is similar and involves the establishment of a sharp boundary that enables the emergence of juxtaposed cell fates.

 Although our current study focused on the existence of this single-cell length morphogen gradient and its functional significance, it will be interesting in the future to unravel how bidirectional targeting occurs. WNTs are known to be N-glycosylated, and studies in *Drosophila* suggest that WNTs can be secreted apically and then transported basally (Yamazaki et al. 2016). Intriguingly, however, in *Drosophila*, N-glycosylation-deficient Wingless is secreted without consequence (Tang et al. 2012), and in mammalian cells, WNTs have been found to be more potent and bind extracellular matrix more robustly in the absence of N-glycosylation (Doubravska et al. 2011). Thus, although our tunicamycin results suggest a role for N-glycosylation in WNT-inhibitor apical secretion, it may be advantageous for cells such as hair bud progenitors that adhere to a basement membrane to secrete their WNTs basally. The ability of ECM to retain growth factors (Baeg et al. 2001), including WNT regulators, makes this

hypothesis all the more attractive.

 In closing, by establishing a morphogen gradient at the cellular level, signals are constrained such that two neighboring cell populations in direct physical contact can effectively receive different signaling inputs. Overall, the ability to directionally control rapid changes in daughter fates, and to establish sharp tissue boundaries without the need for direct competition and/or elimination, offers basic advantages to 340 this mechanism that are likely to be broadly applicable in development.

MATERIAL AND METHODS

Supplementary File 1: Key Resources Table

Mouse strains, lentiviral transduction and constructs

 Mice were housed and cared for in an AAALAC-accredited facility at the Rockefeller University. All animal experiments were conducted in accordance with protocols approved by IACUC and in accordance with National Institutes of Health guidelines. All animal procedures used in this study are described in our #17020-H protocol named *Development and Differentiation in the Skin*, which had been previously reviewed and approved by the Rockefeller University Institutional Animal Care and Use Committee (IACUC). All animals used for the experiments in this manuscript were generated previously: *Axin2- LacZ* (The Jackson Laboratory) (Lustig et al., n.d.), *Krt14-rtTA* (Nguyen, Rendl, and Fuchs 2006), *Rosa26Flox-Stop-Flox-tdTom* (The Jackson Laboratory), *Apcfl/*fl was a kind gift from Kucherlapati Lab (Kuraguchi et al. 2006), *Fucci (595, Riken,*(Sakaue-Sawano et al. 2008)*), Lhx2-EGFP* (The Gene Expression Nervous System Atlas (GENSAT) Project, NINDS Contracts N01NS02331 & HHSN271200723701C to The Rockefeller University, New York, NY, USA), *Wif1-KO* was a kind gift from Igor Dawid (NIH), *Notum-KO* embryos and *Notumfl/fl* mice were kind gifts from the Jean Paul-Vincent Lab (Canal et al. 2016).

 We used ultrasound-guided *in utero* lentiviral-(LV) mediated delivery of RNAi into the amniotic cavity of living E9.5 mouse embryos. This non-invasive technique selectively infects and transduces the

 single-layer of unspecified epidermal progenitors as previously described (Beronja et al. 2010). The construct for lentiviral *Pgk-NLS-Cre-mRFP* has been described (Williams et al. 2011). *Pgk-NLS-Cre- EGFP* was generated by replacing the mRFP coding region with EGFP. For our LV-WNT reporter (*pLKO- TK-12xTOP-EGFP-Pgk-Cre*), *Cre* was amplified by polymerase chain reaction (PCR) from *pLKO.1-Pgk- Cre* (Williams et al. 2011) and inserted into pLenti-12xTOP-EGFP, in which EGFP is driven by a minimal herpes virus thymidine kinase promoter downstream of an enhancer containing multimerized LEF1 DNA binding sites (Beronja et al. 2013). Lentiviral doxycycline-inducible constructs were cloned using a tetracycline regulatory element (TRE) sensitive to the binding and activation by the doxycycline-inducible rtTA transcription factor. This TRE system (*LV-TRE-Gene-Pgk-H2BGFP*) has been previously described (Hsu, Li, and Fuchs 2014). The cDNAs, *Bmp4* (MG50439-G, Sino Biological, (Lu et al. 2016)), *Notum- Myc-tagged* (MR217230, Origene), *WIF1-Myc-tagged*, (MR202510, Origen) *Wnt10b-Myc-tagged* (MR224739, Origen), *Dkk4-Myc-tagged* (MR202533, Origene), *Apcdd1-Myc-tagged* (MR225129, Origene), *Wnt3-Myc-tagged* (MR222492, Origene) were purchased from Origen, and then cloned by PCR to insert the gene of interest (GOI) in the *LV-TRE-GOI-Pgk-H2BGFP*. *Notum-Aqp4-Myc-*tagged, and *Wif1-Aqp4-Myc*-tagged were designed by adding the coding sequence of the last 42 amino acids of the rat Aquaporin-4 (Madrid et al. 2001) (Urra et al. 2008), upstream of *Myc-tag* and synthesized by Genewiz. *Notum-Aqp4-Myc-tagged* and *Wif1-Aqp4-Myc-tagged* further cloned by PCR and inserted into the *LV-TRE-GOI-Pgk-H2BGFP*. *Krt14rtTA* was activated by feeding pregnant females with doxycycline (2 mg/kg, Doxyfeed, Bio-Serv) chow at E9.5 until time of collection.

Flow Cytometry

 Methods for preparing embryonic mouse back and head skin for fluorescence activated cell sorting (FACS) and purification of α6-high epidermal and hair bud progenitors have been previously described (Williams et al. 2011). Briefly, the skin of E14.5 and E17.5 embryos was dissected and either (E14.5) placed directly into a trypsin-EDTA solution at 37ºC for 5 minutes on an orbital shaker, or (E17.5) first treated with the enzyme dispase (Gibco, 1:1 in PBS) overnight at 4ºC prior to making the single cell suspension. Sorting buffer (PBS 5% FBS) was added to the suspension to neutralize trypsin. Single-cell

 suspensions were obtained by filtering through a 70µM strainer and collected by centrifugation at 300g for 5 minutes. Cell suspensions were washed 3 times and incubated with the appropriate antibodies for 30 minutes on ice. For FACS, we used the following antibodies (along with epifluorescent markers): α6- integrin (eBiosciences) to select for basal progenitors, CD140a (PDGFRA) (eBiosciences) to select against mesenchymal cells, CD31 (PECAM1) (eBiosciences) to select against platelets. DAPI was used to exclude dead cells. Cell isolations were performed on FACS Aria sorters running FACS Diva software (BD Biosciences).

RNA-seq and analysis

 FACS isolated keratinocytes, pooled from 3 embryos for each condition, were sorted directly into TrizolLS (Invitrogen). RNA was purified using Direct-zol RNA MiniPrep kit (Zymo Research) per manufacturer's instructions and 2-pooled samples were sequenced for each condition. The quality of the RNA for sequencing was determined using an Agilent 2100 Bioanalyzer and all samples analyzed had RNA integrity numbers (RIN) > 8. Library preparation was performed by the Weill Cornell Medical College Genomic Core facility, which uses the Illumina TrueSeq mRNA sample preparation kit. RNAs were sequenced on their Illumina HiSeq 2500 machines. The reads were aligned with Tophat using mouse genome build mm9 build and the transcript assembly and differential expression was performed using Cufflinks with Ensembl mRNAs to guide assembly. Analysis of RNA-seq data was done using the cummeRbund package in R (Trapnell et al. 2012)*.*

 The genes known to be sensitive to WNT signaling (http://web.stanford.edu/group/nusselab/cgi-408 bin/wnt/) are marked as green dots in the volcano plots that compare WNT^{hi} and WNT^{to} transcriptomes of embryonic skin progenitors on *Apc-*null and *Apc-*het mice. Selected genes relevant for this study are 410 highlighted in both volcano plots (WNT^{hi} and WNT^{Io} transcriptomes of embryonic skin progenitors on *Apc-* null and *Apc-*het and in WT backgrounds - Lhx2GFP+ mKO2Cdt1+ vs mKO2Cdt1+). Differentially regulated transcripts were analyzed with Gene Set Enrichment Analysis (GSEA) to find enriched gene sets (Subramanian et al. 2005).

The overlap between *Apc-*null WNThi and wild-type WNThi (Lhx2GFP+ mKO2Cdt1+) signature genes was defined by intersecting significantly differentially expressed genes (those with a q-value of < 0.05 and with Log2 fold change -FC- of 1.5 fold up) in the two populations. The significance of the overlap was evaluated with a *P-value* derived using the hypergeometric distribution using R software.

In Situ **Hybridization**

 Two different protocols were used to perform *in situ* hybridization depending on the probes hybridized. Whereas protocol 1 was used for *Wnt10b*, *Apcdd1* and *Dkk4* hybridization, protocol 2 was used for the *Notum* and *Wif1* hybridizations. The Wnt10b anti-sense probe was synthesized using the cDNA region 1493-2008bp from the mRNA annotated as NM_011718.2 (PCRII-*Wnt10b*). The cDNA was linearized with the restriction enzyme XhoI and transcribed with Sp6 polymerase. The cDNA used to synthesize the *Apcdd1* anti-sense probe (pCR4-*mApcdd1*) was a generous gift from Angela Cristiano. The cDNA was linearized with the restriction enzyme SpeI and transcribed with T3 polymerase. The cDNA used to synthesize *Dkk4* anti-sense probe (pGEMT-*mDkk4*) was a generous gift from David Schlessinger. The cDNA was linearized using the restriction enzyme NcoI and was further transcribed with the SP6 polymerase. The *Notum* anti-sense probe was synthesized using the cDNA region 385-1495bp from the mRNA annotated as NM_175263.4. The cDNA was linearized with Notl and transcribed with SP6 polymerase. The *Wif1* anti-sense probe was synthesized using the cDNA region 1289-2037bp from the mRNA annotated as NM 011915.2 (pCRII-*mWif1_3*). The cDNA was linearized with NotI and transcribed with SP6 polymerase.

 Protocol 1: 10 to 14 μm cryosections were fixed for 10 minutes in 4% paraformaldehyde (PFA, from 16% PFA solution Electron Microscopy Sciences) in Diethyl pyrocarbonate-PBS (DEPC-PBS), and washed with DEPC-PBS (two times, 5 minutes each). Sections were incubated in TEA buffer with 0.25% acetic anhydride (10 minutes) and washed with DEPC-PBS (three times, 5 minutes each). Pre-hybridization of tissue sections was performed at 68°C for 2 hours with hybridization buffer (50% deionized formamide, 5X saline-sodium citrate, SCC, 0.5 mg/ml salmon sperm DNA, 0.5 mg/ml yeast tRNA and 8.5X

 Denhardt's solution). Hybridization with 1 ug/ml of probe was preformed overnight at 68°C (for 18 hours). To remove the unbound probe, sequential stringent washes were performed at 68°C (5 minutes with 5X SSC, followed by three times 30 minutes with 0.2X SSC), and at room temperature (RT, 5 minutes with 0.2X SSC followed by 10 minutes with B1 buffer - 100 mM Tris-HCl pH 7.5, 0.15 M NaCl). Tissue was blocked with 10% Normal Goat Serum (NGS) in B1 buffer (1 hour at RT) before Digoxigenin detection. Sections were incubated overnight at 4ºC with Anti-Digoxigenin-AP, Fab fragments (from sheep, Roche, 1:2000 in B1 buffer with 1% NGS) and washed with B1 buffer (three times, 10 minutes each). Finally, slides were protected from light and developed at RT with BM purple containing 0.24 mg/ml levamisole and 0.1% Tween-20 until satisfactory signal was achieved.

 Protocol 2: 10 to 14 μm cryosections were prepared one day prior to the procedure, stored at –80° C or 452 kept on dry ice until ready for fixation. Sections were fixed for 30 minutes in cold (4% PFA at 4° C) and 453 washed three times (5 minutes each) at RT with DEPC-PBS. Slides were treated with 3% H₂O₂ (30 minutes) and washed with DEPC-PBS (three times, 5 minutes each). Slides were equilibrated with TEA buffer (5 minutes), treated with TEA buffer containing 0.25% acetic anhydride (10 minutes), and washed three times with DEPC-PBS (5 minutes each). Tissue pre-hybridazion was performed for 2 hours at 68°C with hybridization buffer (50% deionized formamide, 2X SSC, 10% dextran sulfate, 0.5 mg/ml yeast tRNA, 0.5 mg/ml heat-denatured salmon sperm DNA) and hybridization was performed with 1 μg/ml of probe overnight at 68°C (for 18 hours). Post-hybridization washes were performed at 68°C (10 minutes with 5X SSC, and three times 30 minutes with 0.2X SSC). Slides were then washed at RT with 0.2X SSC (for 5 minutes) before incubation with blocking solution for 1 hour at RT (0.5% Roche Blocking reagent in B1 buffer, 100 mM Tris-HCl pH 7.5, 0.15 M NaCl). A second block was performed (1 hour at RT) with B1-BTx buffer (100 mM Tris-HCl pH 7.5, 0.15 M NaCl, 1% BSA, 0.3% Triton-X 100). Sections were incubated overnight at 4° C with anti-Digoxigenin-AP, Fab fragments (1:2000 in B1-BTx buffer), and washed at RT with sequential washes; 1) four times, 20 minutes each, with B1-BTx buffer; 2) 5 minutes with B1 buffer and finally 3) 5 minutes with B3 buffer (100 mM Tris-HCl pH 9.5, 0.1 M NaCl, 50 mM

 MgCl2). Signal was developed protected from light and incubating sections with BM purple (with 0.24 mg/ml levamisole, 0.1% Tween-20).

Whole-Mount immunofluorescence and histological analyses

 5-ethynyl-2′-deoxyuridine (EdU, 500 μg/g, Life Technologies) was injected intraperitonally into pregnant females 4h prior to processing embryos at the desired stage of development. Typically >3 embryos from independent experiments were analyzed per condition. For whole-mount immunofluorescence, embryos were fixed in 4% PFA in phosphate buffered saline (PBS) for one hour, followed by extensive washing in PBS. Samples were then permeabilized for 3 hours in 0.3% Triton X-100 in PBS and treated with Gelatin Block (2.5% fish gelatin, 5% normal donkey serum, 3% BSA, 0.3% Triton, 1X PBS). For immunolabeling with mouse antibodies, sections were first incubated with the M.O.M. blocking kit according to manufacturer's instructions (Vector Laboratories). The following primary antibodies were used: P- Cadherin (goat, 1:300; R&D AF761), LEF1 (guinea pig, 1:2000 and rabbit 1:300, Fuchs Lab; rabbit, 1:300, Cell Signaling C12A5), SOX9 (guinea pig, 1:2000; Fuchs Lab), LHX2 (rabbit, 1:2000; Fuchs Lab), anti-GFP/YFP (chicken, 1:1200; Abcam), anti-RFP (rat 1:200; Chromotek 5F8) β-catenin (mouse, 1:200, BD 610154), pSMAD 1/5/9 (rabbit, 1:200; Cell Signaling), NOTUM (rabbit 1:100; Sigma HPA023041), WIF1 (goat 1:300; R&D AF7135), MYC-tag (rabbit, 1:300; Cell Signaling 71D10), SOX2 (rabbit, 1:200; Abcam EPR3131), Trans-Golgi (rabbit 1:200; abcam TGN46 16059), Frizzled10 (rabbit 1:200; MyBioSource MBS9606335), SHH (goat 1:50; R&D AF445), E-Cadherin (rabbit 1:500; Cell Signaling, 24E10), P-Histone H2AX S139 (rabbit 1:200; Cell Signaling), β4-Integrin (rat 1:500; CD104 346-11A BD), TCF1/TCF7 (rabbit 1:500; Cell Signaling C63D9). Primary antibodies were incubated at 4ºC for 36h. After washing with 0.1% Triton X-100 in PBS, samples were incubated overnight at 4ºC with secondary antibodies conjugated with Alexa 488, RRX, or 647 (respectively, 1:1000, 1:500, and 1:200, Life Technologies). Samples were washed, counterstained with 4'6'-diamidino-2-phenilindole (DAPI) and 491 mounted in SlowFade™ Diamond Antifade Mountant (Invitrogen), and EdU incorporation was detected by Click-It EdU AlexaFluor 647 Imaging Kit (Life Technologies).

Immunohistochemistry and LacZ-derived β-galactosidase activity

 For sagittal analyses of tissues, pre-fixed (4% PFA in PBS), paraffin-embedded embryos were sectioned at 10μm. Immunohistochemistry was performed by incubating sections at 4°C overnight with primary antibodies against mouse anti-β-catenin (mouse, 1:1000; Sigma, 15B8) and APC (rabbit 1:500; Sigma HPA013349). For brightfield immunohistochemistry, biotinylated species-specific secondary antibodies followed by detection using (ImmPRESS reagent kit peroxidase Universal - Vector Laboratories) and DAB kit (ImmPACT DAB Peroxidase (HRP) Substrate Vector Laboratories) were used according to the manufacturer's instructions.

 LacZ-derived β-galactosidase activity was assayed on frozen sections (10μm), fixed with 0.5% glutaraldehyde in PBS for 2 minutes, washed with PBS, and then incubated with 1 mg/ml Xgal substrates 504 in PBS with 1.3 mM MgCl₂, 3 mM K3Fe(CN)6, and 3 mM K4Fe(CN)6 for 1 hr at 37° C.

Skin explants and pharmacological treatment

 Head and back skins were excised from E15.5 embryos and placed into sterile PBS. Explants were cut in half to compare morphogenesis of pharmacologically-treated *vs* vehicle control skin. Each explant half was covered with Nucleopore TrackEtch filters (Whatman) dermis side down. Filters with skin samples were placed in lummox teflon-bottom dishes (Sarstedt). Pre-warmed keratinocyte culture medium with 0.3mM calcium was added to the culture. Each corresponding half skin received one treatment: either Tunicamycin (0.15mM, 1mM and 2mM; Milipore Sigma) or DMSO control. Explants were cultured at 513 37°C, 5% CO2 for 10 hours and fixed with 4% PFA for 45 minutes before immunostaining and confocal microscopy analysis.

 For the porcupine inhibitor experiment, each half skin was treated with either porcupine inhibitor LGK974 (1mM or 10mM; Cayman Chemical), or DMSO control. Explants were kept at 37ºC, 5% CO2. Media with treatment was changed after 12 hours. After culturing for 24h or 36h at 37ºC, samples were fixed and processed for confocal immunofluorescence microscopy.

 Porcupine inhibitor washout experiment was performed by treating each half skin with 1mM LGK974. After 12 hours one of the samples was fixed (PFA 4%) while the media was changed every 5

 minutes (total of 20 minutes) for the corresponding other sample. Washout sample was kept at 37ºC, 5% CO2 for additional 24 hours and fixed with 4% PFA before immunostaining and confocal microscopy analysis.

Confocal microscopy

 Confocal images were acquired using a spinning disk confocal system (Andor Technology Ltd) equipped with an Andor Zyla 4.2 and a Yokogawa CSU-W1 (Yokogawa Electric, Tokyo) unit based on a Nikon TE2000-E inverted microscope. Four laser lines (405, 488, 561 and 625 nm) were used for near simultaneous excitation of DAPI, Alexa448, RRX and Alexa647 fluorophores. The system was driven by 529 Andor IQ3 software. Tiled imaging was performed to sample $2mm²$ areas of skin. Stacks of 1mm steps were collected with a 20x/0.75 CFI Plan-Apochromat air objective. Zen 2.3 software (blue edition, Carl Zeiss Micrsocopy GmbH, 2011) was used to stitch the acquired images. 40x oil objective was used to acquire z stacks of 0.5-1 mm steps.

Developing hair-follicle density, and immunofluorescence quantitative analysis

 Developing hair follicle density was measured from tiled images using Fiji software (NIH). Briefly: placode 536 and cluster densities were quantified from 10-30 mm² regions of 14.5 back skins (*Apc-*null or *Apc-het*). For all the *Krt14rtTA* experiments, developing hair follicle densities were quantified across a total area of $538 \geq 8$ mm² of E15.5 head skin, i.e. peak LV transduction. For each explant (n=5 LGK1µM), we quantified the 539 developing hair follicle density over a total area of 10mm².

 Placode and clusters morphological analysis was performed using the shape descriptors tool from Fiji (NIH). Area and circularity (*4pi(area/perimeter^2)*) were measured and recorded. A circularity (cir) value of 1.0 indicates a perfect circle. As the value approaches 0.0, it indicates an increasingly elongated shape.

 Intensity plots were generated like in (Messal et al. 2019) using the plot profile tool from Fiji (NIH) and measuring intensities of a minimum of 3 basal cells per developing follicle (from a minimum of developing skin from 3 embryos). Briefly, optical sections of whole-mount 40x confocal images were converted into composite images in which MYC-tag (or FZD10) was in the red (or green) channel and

 DAPI (which labels the DNA) in the blue. Basal–apical intensities were measured along a straight line for each cell (and each channel) along the middle axis of the cell and normalized for intensity by subtracting the minimum value from each intensity profile and dividing by its average value. All measurements were aligned for the basal side of the cell having the same starting point of the measurement.

 Transduction, ectopic and mispolarization expression efficiency were quantified using Fiji. Briefly, 40x optical sections of spinning disk confocal images were converte into composite images in which DAPI was in blue channel, H2BGFP in the green channel and MYC-tag in the red channel. From each optical section of a developing hair follicle, a minimum of 9 basal cells were quantified. The numbers of transduced cells (H2BGFP positive), ectopic expression (MYC-tag apical polarization) and mispolarization (basolateral expression of AQP4-MYC-tag) were recorded and the proportions calculated either relative to the total of basal cells analyzed (transduction) or the total number of MYC-tag expressing cells (ectopic and mispolarization experiment).

 LEF1 immunofluorescence quantifications were performed using Fiji. Briefly, using spinning disk Z-stacks of whole-mount 40x confocal images, we sum the intensity across the follicle. The integrated density of LEF1 immuolabeling across a region of interest (e.g. dermal condensate or basal hair bud progenitors) was normalized at the cellular level by DAPI. Background was then measured and subtracted for each channel.

 The relative population size of LEF1 or SOX9 was determined using Fiji. Briefly, using spinning disk Z-stacks of whole-mount 40x confocal images, we measured the area occupied by each specific cell population (LEF1 from dermal condensate, LEF1 from developing hair follicle and SOX9 hair follicle) and divided by the total epithelial area of the developing follicle, using the area tool.

Statistics

 To reduce any bias in data collection, all data from each group were not analyzed until all images were collected. No statistical method was used to predetermined sample size, randomization and experiment blinding was not used. Each experiment was repeated with at least two replicates and data presented is from three or more embryos, same age. Distributions were tested for normality using D'Agostino and

 Pearson test. To test significance, unpaired or paired two-tailed Student's *t*-tests were used for normal distribution and nonparametric Mann-Whitney test when the distribution did not follow a normal distribution. Basal to apical fluorescence intensity profile plots represent means and error bars SEM. Violin plots show the distribution of all measured data points. Median and quartiles are represented. All the other graphs represent means and error bars SD in all plots. Significance of *P* value was set at < 0.05. Statistical details for each experiment, including the statistical test used, the sample size for each experiment, the n and *P* value can be found in the corresponding figure legend. All graphs and statistics were produced using GraphPad Prism 8.2 for MAC, GraphPad Software, San Diego, California USA, www.graphpad.com.

Data and materials availability

 All reagents engineered for this study are available from jdelacruz@rockefeller.edu under a materials transfer agreement with the Rockefeller University. RNAseq data are deposited in the Gene Expression Omnibus under accession number GSE108745 [\(www.ncbi.nlm.nih.gov/geo\)](http://www.ncbi.nlm.nih.gov/geo).

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DECLARATION OF INTERESTS

- The authors declare no competing financial interests.
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FIGURE LEGENDS

 Figure 1. Two-dimensional patterning of hair placodes is severely affected upon sustained autonomous WNT activation. (**A**) Sagittal views and schematic of skin section depicting a basal hair bud progenitor and underlying dermal condensate (DC, encased by blue dotted lines). Labeling is for *LacZ* expression knocked into the *Axin2* locus and nuclear LEF1, two faithful proxies of WNT signaling. Additionally, 829 nuclear SOX9 marks the overlying WNT^{\circ} bud cells, and P-cadherin marks the basal epithelial 830 progenitors. Dashed lines denote the basement membrane (BM) rich in extracellular matrix (ECM) and growth factors at the epidermal-dermal border. Scale bars, 10μm. (**B**) (top left and bottom) *In utero* lentiviral delivery strategy to generate sparse epidermal patches lacking APC, and therefore super-833 activating WNT signaling. Visual and epifluorescence imaging of mosaically transduced (R26dtTomato+) E14.5 *Apc* heterozygous and null embryos. Scale bar, 2mm. (top right) Schematic of whole mount imaging. (**C**) Planar views of the skin surface of E14.5 embryos. Scale bar, 100μm. (**D**) Quantifications showing *Apc* null clusters of broader size and shape than *Apc* heterozygous (het) placodes, which were 837 analogous to wild-type in this assay (Circularity =1 perfect circle). (Placodes and clusters density plot 838 n>10mm² skin area; *****P* < 0.0001; Mann-Whitney test; Area and Circularity plots n=130 placodes and 216 clusters; *****P* < 0.0001; Mann-Whitney test; All n≥3 embryos.). (**E**). Whole mount (planar) images showing atypically strong nuclear β-Catenin and LEF1 in *Apc-*null cell clusters. Scale bar, 20μm.

Figure 2. Teasing out a WNT-sensitive molecular signature based upon transcriptome profiling of skin

 progenitors possessing different WNT signaling levels*.* (**A**) LV construct, epifluorescence imaging and 844 FACS strategy for isolating WNT signaling (GFP+) and WNT^{\circ} skin progenitors from LV-transduced E14.5 *Apc*^{$\#$ +} and *Apc*^{$\#$ *fl*, *R26fl-stop-fl-tdTOM* embryos. (**B**) Gene set enrichment analysis (GSEA) of gene sets} showing marked differential expression in WNT signaling progenitors from *Apc-*null vs *Apc-*het embyros. False discovery rate (FDR) q-values of enrichment are shown for each gene set. (**C**) Waterfall plot depicting genes markedly influenced (Log2 Fold Change ≥1.5, p<0.05) by APC status (color-coding according to B). (**D**) Volcano plot showing differentially regulated transcripts and WNT-reporter status.

 Figure 3. Wild-type WNT signaling progenitor cells express high levels of WNT inhibitors. (**A**) Strategy used to isolate and profile slow-cycling basal progenitors from the epidermal fraction of dispase-treated, 853 wild-type E17.5 skin, which contains epidermis and early hair placodes/buds. Note: LEF⁺ progenitors are 854 simultaneously LHX2GFP⁺ and mKO2⁺. (B) Volcano plot and comparative expression profiling reveals that relative to their epidermal counterparts, wild-type basal placode/bud progenitors share strong signature similarities with *Apc-*null progenitors. Green dots denote previously reported WNT target genes. (**C**) *In situ* hybridizations showing that WNT signaling progenitor cells simultaneously express mRNAs for WNT activators and WNT inhibitors. Black dashed lines, epidermal-dermal boundary; white dashed lines demarcate the dermal condensate (DC). Scale bars, 10μm.

 Figure 4. Progenitor cells apically polarize WNT inhibitors. (**A**) Schematic of whole-mount analysis from embryonic skin with examples of optical sections showing interfollicular epidermis (IFE), bud and germ; position of pixel intensity measurement. Z, plane of imaging from the Z-stack. (**B**) Anti-WIF1 and (**C**) anti- NOTUM immunofluorescence in placode, bud and germs reveal an apical accumulation of WIF1 and NOTUM. Pixel intensity profiles of basal hair bud progenitors (n = ≥40 WNT signaling progenitors; mean \pm SEM; a.u., arbitrary units). Note also absence of WNT inhibitors in upper region of the dermal condensate (encased by yellow dotted line) at this stage of morphogenesis, leaving a WNT inhibitor free zone (yellow arrowheads) for nuclear LEF1 and WNT signaling at the epidermal-dermal boundary (white dashed line) and a WNT inhibitor high zone in suprabasal hair bud cells (arrows). Blue circular dashed

 lines outline placodes. White dotted lines demarcate epithelial-mesenchymal boundaries. *Denotes magnified cells, shown at right of each frame. Scale bars: 5 μm magnified cells; all others, 20μm.

Figure 5. Evidence of oppositely polarized and short-range action of WNTs and WNT inhibitors in hair bud progenitors that are actively signaling through WNTs. (**A**) LV-constructs and strategy to monitor WNT inhibitors and WNTs. M, myc-tag. TRE, tetracycline regulatory element. *Krt14rtTA* is a transgenic mouse line expressing a doxycycline (DOX)-inducible transcriptional activator for TRE. (**B, C**) Similar to endogenous expression, anti-WIF1 and anti-NOTUM immunofluorescence on MYC-tag transduced skin show apical localization in hair bud progenitors. (**D**) Anti-MYC-tag immunofluorescence of transduced 879 skins revealing apical polarization of NOTUM and WIF1, but basal polarization of WNT10B. At right are basal-apical MYC-Tag/DAPI pixel intensity profiles of basal hair bud progenitors (n = ≥40 WNT signaling progenitors; mean ± SEM; a.u., arbitrary units). (**E**) Pixel intensity profile and immunolocalization of endogenous WNT-receptor FRIZZLED 10 shows uniform localization at borders of hair bud and germ 883 WNT signaling cells (n=37 cells; mean ± SEM; a.u., arbitrary units). *Denotes magnified cells, shown at 884 right of each frame. Scale bars: 5um magnified cells; all the others, 20um.

 Figure 6. Hair bud progenitors apically polarize WNT inhibitors to protect their own identity and differentially confer WNT signaling to their neighbors. (**A**) Whole-mount immunofluorescence and 888 quantifications reveal that elevating NOTUM across the epidermal plane results in significantly fewer hair 889 follicles (Mean ± SD; n>10mm² skin analyzed from ≥ 3 embryos; $*P < 0.05$; $**P < 0.005$; Mann-Whitney 890 test). Scale Bar, 100um. OE, overexpression. Insets verify transduced regions. All scale bars for immunofluorescence images are 20μm. (**B**) Adding an aquaporin4-tag mispolarizes NOTUM to the basal 892 side of hair bud progenitors. Quantifications reveal that mis-polarizing a WNT inhibitor poses a significant 893 impediment to hair follicle morphogenesis (Mean ± SD; n= 8mm² skin analyzed from ≥ 3 embryos; **P* < 0.05; ***P* < 0.005; ****P* < 0.0005; unpaired Student *t* test). White dotted lines demarcate epithelial- mesenchymal borders throughout. (**C**) Whole-mount immunofluorescence and quantifications of normalized LEF1 pixel intensities reveals that NOTUM mis-polarization leads to a significant decrease of

 LEF1 intensity in WNT signaling cells from both the dermal condensate and the hair bud (n≥48 hair follicles from ≥ 3 embryos each; Mann-Whitney test *** *P*=0.0002 and unpaired t test ***P* < 0.005; n.s. non-significant; red lines represent the distributions' median). Yellow boxes show regions magnified at right. Arrowheads show two cells not expressing NOTUM-AQP4-MYC-Tag, which have higher LEF1 signal than their expressing neighbors. (**D**) Violin Plots show that increasing levels of NOTUM and NOTUM-AQP4 lead to an increase of SOX9 expressing cells (n≥30 developing hair follicle from at least 3 different embryos; Mann-Whitney test TRE-NOTUM **P=*0.0389 and TRE-NOTUM-AQP4 **P* = 0.0461 n.s. non-significant; red lines represent the distributions' median).

 Figure 7. Notum regulates the formation of sharp boundaries between neighboring cell fates (**A**) *In utero* lentiviral delivery strategy to conditionally ablate *Notum* in *R26dtTomato* embryos. (**B-C**) Representative 907 whole-mount immunofluorescence showing LEF1 intensity profile and population size in *Notum*^{-/+} and 908 Notum^{-/-} skin. Red boxes denote regions magnified below each image. Note that *Notum* ablation (but not 909 heterozygous) leads to an increase in LEF1 signal and LEF1+ cell populations in the WNT signaling progenitor cells (n≥75 hair follicles from ≥3 different litters analyzed; Mann-Whitney test * *P*=0.0332 and 911 *** *P*=0.0002; n.s. non-significant; red lines represent the distributions' median).

 Figure 8 - Summarizing model. WNT signaling basal progenitors form opposing intracellular morphogen 913 gradients of WNT inhibitors and WNT ligands/activators. In so doing, they preserve their own WNT signaling and identity and directionally permit (dermal condensate) or restrict (suprabasal hair bud cells) WNT signaling in surrounding neighbors.

SUPPLEMENTAL FIGURES

 Figure 1 – supplement 1. *Apc-*null clusters show properties of hair follicles arrested at the placode stage. (A) Sagittal sections of embryonic skin subjected to immunohistochemistry with antibodies against β-Catenin and APC. Note that reduced APC immunostaining coincides with broadened elevated β- Catenin, reflective of enhanced WNT signaling throughout the cluster. (**B**) Schematic of whole-mount 921 analysis from embryonic skin with two examples of sampling of optical sections. (C) Apc^{f//f} and Apc^{f//+}: *Rosa26-lox-stop-lox-YFP* or *tdTomato* embryos were transduced with LV-Cre and subjected to whole-

923 mount immunofluorescence microscopy. Note that when cells form a distinct cluster, they strongly 924 immunolabel for nuclear β -catenin and LEF1, as well as WNT^{hi} progenitor marker LHX2, features of hair 925 placodes, but they are negative for WNT^{to} hair bud marker SOX9. The absence of WNT^{to}SOX9⁺ cells within the cluster indicates its failure to progress to the hair follicles bud stage. By contrast, the wild-type 927 cells surrounding these clusters were SOX9⁺, reflective of the impact of WNT^{hi}LHX2⁺ surrounding the clusters. This is most likely due to the high level of WNT-inhibitors expressed by neighboring *Apc*-null cells as shown in Fig 2. Scale bar, 20μm for all frames.

 Figure 1 – supplement 2. *Apc-null* clusters do not present signs of DNA double strand breaks. (**A-B**) 932 Immunofluorescence detection of γ H2AX in developing epidermis of (A) *Apc*^{#/+} and (B) *Apc*^{#/#} Rosa26- *lox-stop-lox-tdTOM* embryos were transduced at E9.5 with lentivirus harboring a Cre recombinase (*Pgk- Cre-mRFP*) and analyzed at E14.5. Circular yellow dashed line outlines a placode. Orange insets highlight transduced (tdTOM+) versus non-transduced epithelia. Yellow dashed lines contour *Apc-null* clusters. Scale bar, 20μm for all frames.

 Figure 1 – supplement 3. *Apc*-null cells aggregate into clusters and are non-proliferative. (**A**) 939 Experimental design and proliferation analysis. *Apc^{t/fl}; Rosa26-lox-stop-lox-YFP* embryos were transduced at E9.5 with LVs harboring a Cre recombinase (*Pgk-Cre-mRFP*) and analyzed at E14.5. At 4h 941 prior to analysis, a pulse of 5-Ethynyl-2'-deoxyuridine (EdU) was administered. Note the absence of EDUpositive cells within the clusters. Scale bar, 10μm. (**B**) *Apcfl/fl YFPfl/fl mKO2Cdt1* embryos were transduced with *Pgk-Cre* as shown in the schematic. Representative image of an *Apc*-null cluster is shown at right. 944 Note that YFP⁺ cells are simultaneously positive for the G0/G1 sensor mKO2Cdt1, in agreement with the non-proliferative status of these clusters. Scale bar, 20μm. (**C**) E9.5 *Apcfl/fl* embryos were transduced with LVs harboring different fluorescing Cre recombinases and analyzed 5d later. Note that like placodes, clusters are multiclonal, reflected by the presence of both RFP and GFP tagged cells. Scale bars, 20μm.

 Figure 1 – supplement 4 *Apc-null* cell clusters lose adherens junction transmembrane protein E- Cadherin. Representative E14.5 whole-mount immunofluorescence images and respective orthogonal 951 views from (A) *Apc-het* and (B) *Apc-null* transduced tdTomato⁺ embryonic skins showing endogenous E- Cadherin and P-Cadherin immunofluorescence. Note loss of E-Cadherin in *Apc-null* clusters when compared to the surrounding wild-type skin. Circular yellow dashed line outlines a heterozygous placode while remain dashed lines contour *Apc-null* cell clusters. White dotted lines demarcate epithelial- mesenchymal boundaries. The XY axis is planar to the epidermis; the XZ axis shows sagittal views perpendicular to the skin surface. Scale bars, 20μm.

 Figure 1 – supplement 5 *Apc-null* cell clusters lose the hemidesmossome integrin beta4 (ITGB4). Representative E14.5 whole-mount immunofluorescence images and respective orthogonal views from (**A**) *Apc-het* and **(B)** *Apc-null* transduced tdTomato⁺ embryonic skins showing endogenous ITGB4 and P- Cadherin staining. Note the loss of ITGB4 in *Apc-null* clusters when compared to the surrounding wild- type skin. Circular yellow dashed line outlines a heterozygous placode while remain dashed lines contour *Apc-null* cell clusters. White dotted lines demarcate epithelial-mesenchymal boundaries. The XY axis is planar to the epidermis; the XZ axis shows sagittal views perpendicular to the skin surface. Scale bars, 20μm.

967 **Figure 2 – supplement 1**. FACS purification strategy to isolate WNT^{hi} skin progenitors from *Apc* 968 embryonic skin. (A-B) FACS purification of WNT^{hi} cells from *Apc^{f//+}*; *Rosa26-lox-stop-lox-dtTomato* 969 embryos (A) and from *Apc^{f//fl}* Rosa26-lox-stop-lox-dtTomato embryos (B). Both types of embryos were 970 transduced at E9.5 with an LV harboring a WNT GFP reporter and Pgk-Cre and then harvested at E14.5. 971 WNT-reporter^{hi} (a6⁺ tdTomato⁺ GFP⁺) and WNT-reporter^{lo} (a6⁺tdTomato⁺) progenitors were purified, while 972 suprabasal (a6^{neg} tdTomato⁺ GFP^{neg}) epidermal cells and non-epidermal cells (Lin-: CD131+ and CD140a+) were eliminated.

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 Figure 2 – supplement 2. Table1. Cell adhesion transcripts upregulated in *Apc null* WNThi cells (Geneontology – PANTHER Classification System).

Figure 3 – supplement 1. FACS purification strategy to isolate WNT^{hi} placode and WNT^{Io} epidermal progenitors from wild-type embryonic skin. (**A**) FACS purification plots of single cell suspensions isolated from the dispase-selected epidermal/hair bud fraction of E17.5 skin. Pups were transgenic for *Lhx2-GFP*, active in basal hair bud progenitors, and for *mKO2Cdt1*, active in the slow-cycling basal skin progenitors of both hair buds and interfollicular epidermis. All basal progenitors are marked by α6 integrin. Non- epidermal cells (Lin-: CD131+ and CD140a+) were excluded by FACS. (**B**) *mKO2Cdt1* embryos were exposed to lentivirus at E9.5 and analyzed at E15.5 as depicted in the schematic. The LV harbored a WNT-GFP reporter (*12xTCF-TK-EGFP*) and *Pgk-Cre*. Note that the progenitor cells from the developing hair follicle are concomitantly LEF1+, mKO2+ and WNT reporter positive. Scale bar, 20μm. (**C**) Venn 988 diagram depicts the overlap between *Apc-*null WNT^{hi} signature genes and wild-type (*Lhx2GFP+* 989 mKO2Cdt1+) WNT^{hi} signature genes. P values were calculated using the hyper geometric distribution 990 formula via R. Note: While overlap was appreciable, WNT^{hi} Apc-null transcripts were pure placode 991 signature genes and in addition encoded cell cycle inhibitors, while wild-type WNThi cells included not 992 only placode but also some bud mRNAs, and although slow-cycling, these cells were still proliferative.

994 **Figure 3 – supplement 2. Table 2.** WNT^{hi} signature genes in hair follicle development. Shown is a list of 995 transcripts that are shared between the *Apc null* WNT^{hi} signature and the wild-type WNT^{hi} signature.

 Figure 3 – supplement 3. BMP4 acts long range to perturb hair follicle patterning**.** (**A-B**) Strong correlation between WNT signaling and *Bmp4* levels in both (**A**) *Apc-*null clusters and (**B**) wild-type hair buds. (**C**) Whole-mount immunohistochemistry of E14.5 mosaic *Apc-*null and *Apc-*het embryos. Note a halo (asterisks) of nuclear pSMAD1/5/9+ cells extending well beyond the borders of *Apc-*null clusters, indicative of long-range BMP signaling. Scale bar, 20μm. (**D**) Experimental setup to overexpress BMP4 in skin progenitors. BMP4 is under the regulation of a tetracycline regulatory enhancer (TRE) activated by

 doxy-induced rtTA transcription factor binding. The lentivirus was introduced at E9.5 into the amniotic 1004 cavity of Krt14rtTA⁺ and Krt14rtTA^{neg} embryos, which were then analyzed at E15.5. (E) Whole-mount 1005 images of 1mm² E15.5 skins of Doxy-treated *Krt14rtTA*⁺ and control (*Krt14rtTA^{neg}*) littermates. Note the 1006 perturbation in patterning of hair follicles (P-Cadherin⁺). Scale bar, 100μm. (F-G) Representative regions of transduced and untransduced epidermis in *Krt14rtTA* negative and positive littermates, (**F**) Note the 1008 reduced LEF1 immunostaining in GFP⁺ BMP^{hi}-signaling cells. (G) Note the presence of nuclear 1009 pSMAD1/5/9 positive cells distant from the BMP^{hi}-signaling cells (white arrows), suggestive of long-range signaling. White boxes delineate the regions that are magnified in the three images beneath each low-magnification panel. Scale bar, 20μm.

 Figure 3 – supplement 4. *Apc*-null cells express high levels of WNT inhibitors. **(A-B)** Representative immunofluorescence images and respective orthogonal views from *Apc-null* and *Apc-het* transduced 1015 tdTomato⁺ embryonic skins showing endogenous (A) WIF1 and (B) NOTUM patterns. Note strong expression of WNT inhibitors NOTUM and WIF1 in *Apc-*null clusters, despite presence of nuclear LEF1 and robust WNT signaling. Circular dashed line in *Apc-het* outlines a placode. Dotted lines demarcate epithelial-mesenchymal boundaries. The XY axis is planar to the epidermis; the XZ axis shows sagittal views perpendicular to the skin surface. Scale bars, 20μm.

 Figure 4 – supplement 1. Apical WIF1 localization is dependent on N-Glycosylation. (**A**) Strategy to test the importance of N-Glycosylation for WIF1 apical localization. E15.5 wild-type embryonic skin explants were treated with different Tunicamycin concentrations for 10 hours and fixed afterwards for whole-mount immunofluorescence analysis. Note increasingly mis-polarized endogenous WIF1, shifting from apical to basal, as the concentration of Tunicamycin is raised. Insets show higher magnifications of boxed regions. (**B**) Localization of the endogenous Trans-Golgi network in the developing hair follicles and interfollicular epidermis (IFE) and their respective basal-apical pixel intensity profile measured in 21 WNT-signaling 1028 progenitor cells and 31 IFE cells (mean ± SEM. a.u., arbitrary units). Insets show higher magnification of

 selected regions. Note that Golgi is present both basally and apically within the bud progenitors. Scale bars, 20μm. Inset scale bars, 10μm.

 Figure 5 – supplement 1. WIF1 expression during early hair follicle development (**A**) Strategy to monitor WIF1 expression by MYC-tagging (M). Depicted LV was introduced into the amniotic cavities of E9.5 *Krt14rtTA* embryos, and transduced genes were activated by doxycycline (DOX). Representative whole- mount and orthogonal views of WIF1-MYC-tag and WIF1 immunostaining of E15.5 embryos. Note uniform distribution of protein within the plane of the embryonic epidermis (white arrows). Dashed line demarcates the border between epidermis and dermis. Yellow lines represent the corresponding orthogonal views. Scale bar, 20μm. (**B**) Endogenous WIF1 localization is shown by whole-mount immunofluorescence of interfollicular epidermis, hair placodes, hair buds and hair germs. Note that WIF1 is increased in the hair bud and germ epidermis but is only expressed at the bud stage in the early dermal condensate (yellow dotted lines). Note also the distinct apical localization of WIF1 in hair buds and germs. *Wif1* full KO embryos were used to test the specificity of the antibody, shown here for the hair germ stage. Boxed areas in blue are magnified below each image, with WIF1 and LEF1 immunolabels. Scale bars, 20μm.

 Figure 5 – supplement 2. NOTUM expression during early hair follicle development (**A**) Strategy to monitor NOTUM by MYC-epitope tagging (M). Depicted LV was introduced into the amniotic cavities of E9.5 *Krt14rtTA* embryos and the transduced *Notum* gene was activated by doxycycline (DOX). Representative whole-mount planar (XY) and orthogonal (XZ) views of NOTUM-MYC-tag immunostaining. Note that within the plane of embryonic epidermis, NOTUM is uniformly distributed (white arrows). Dashed lines demarcate the border between epidermis and dermis. (**B**) Endogenous NOTUM immunolocalization in wild-type and *Notum*-null skin, is shown by whole-mount immunofluorescence of interfollicular epidermis, hair placode and hair germs. P-Cadherin co- immunolabeling was used to mark the skin epithelium. Dotted circles/lines encase the developing hair follicles. Boxed areas are magnified in the boxes below the relevant images. Note little or no NOTUM in

 interfollicular epidermis. However, NOTUM is expressed in developing hair placodes. At the hair germ 1057 stage, it is clear that endogenous NOTUM protein concentrates on the apical side of WNT $^{\text{hi}}$ epithelial cells (insets, red arrows). *Notum*-null skin was used as a control to show the specificity of the NOTUM antibody. All scale bars, 20μm.

 Figure 5 – supplement 3. Differential polarization of WNT inhibitors and activators**.** Strategy to monitor WNT inhibitors (DKK4 and APCDD1) and ligands (WNT3) by MYC-epitope tagging (M). LV-constructs were introduced into the amniotic cavities of E9.5 *Krt14rtTA* embryos, and transduced genes were activated by doxycycline (DOX). Whole-mount immunofluorescence and/or immunohistochemistry of representative images of hair buds are shown below. DAPI to label chromatin; anti-GFP to mark nuclei of transduced cells; Anti-MYC-tag to label the expressed inhibitor/ligand. At right are shown the basal-apical MYC-Tag pixel intensity profiles, which were measured along the lines presented in the overlying 1068 schematic of the WNThi progenitor cells of the hair follicle. A minimum of 40 WNT-signaling progenitor cells were analyzed and averaged to develop these profiles. Note the preferential apical enrichment of DKK4 and APCDD1 and opposing basal enrichment of WNT3 signal. Mean ± SEM. a.u., arbitrary units. All scale bars 20μm.

 Figure 6 – supplement 1. WNT inhibitor overexpression perturbs hair follicle formation**. (A)** Whole mount immunofluorescence and quantifications reveals that elevating WIF1 across the epidermal plane results in significantly fewer developing hair follicles beginning at the placode stage. Insets verify that the 1076 skin regions shown were transduced (GFP⁺) (Mean \pm SD; n>18mm² skin analyzed; ***P* < 0.05; ****P* < 0.005; n.s. non-significant; unpaired Student *t* test). Scale Bar, 100μm. OE, overexpression. **(B-B')** Sparser hair coat upon ectopic *Notum* expression. Example of neonatal litter, some of which overexpress NOTUM and show a sparser hair coat than their control littermates. Note also the sparser hair coat of a representative P29 adult mouse that is positive for *Notum* overexpression, when compared to its 1081 uninduced control littermate.

 Figure 6 – supplement 2. Hair bud progenitors cannot maintain their fate upon WNT inhibition. (**A**) Experimental design and results of pharmacological WNT inhibition in embryonic skin explants exposed to the porcupine inhibitor LGK974. Note that placode/bud numbers were significantly reduced after 24h treatment with 1mM LGK974, a porcupine inhibitor and established blocker of WNT signaling (n=5 1087 – embryos where each line represents the average number of placodes, germs and pegs per skin mm², on an independent explant. **P* < 0.05; paired Student *t* test). (**B**) Immunofluorescence of explants from experiment in (A). Note that upon 1mM LGK974 treatment, significant alterations appear in WNT 1090 signaling (nuclear LEF1), specifically within the normally WNT^{hi} bud progenitors that border the dermal condensate border. Note also that SHH is suppressed in these progenitors while SOX9 (normally 1092 restricted to WNT^{to} hair follicle cells) is induced, reflecting the inability of WNT^{hi} bud progenitors to maintain their fate when WNT signaling is inhibited. Note also that developing hair follicles are unable to envelope the dermal condensate. Scale bars, 20μm. (**C**) LEF1 immuno-intensity, color-coded according to pixel intensity, reveals an overall reduction in nuclear LEF1 within both hair bud progenitors and dermal condensate cells upon 1mM LGK974 treatment. Values were normalized to DAPI (DMSO n=31 and LGK974=32 developing hair follicles *****P* < 0.0001, Mann-Whitney test). Scale bar, 20μm. (**D**) Whole-mount immunofluorescence images of representative developing hair follicles from E15.5 explants treated with DMSO and 10mM LGK974. Note that LEF1 is lost from bud progenitors, which concomitantly 1100 gain SOX9 expression, normally restricted to WNT^{to} hair follicle cells. Note that at these higher concentrations of WNT-inhibitor, the effects described in (B) are now more pronounced. (**E**) Total LEF1 in the dermal condensate and basal progenitors was measured and normalized to DAPI. Note that basal hair follicle progenitors quantitatively lost nearly all of their LEF1/WNT-signal, while even at this high concentration of porcupine inhibitor, there is still some residual LEF1/WNT-signal in the dermal condensate cells (DMSO n=28 and LGK974=31 developing hair follicles; *****P* < 0.0001, Mann-Whitney test). White dotted lines demarcate the epithelial-mesenchymal boundary. Scale Bar, 20μm; a.u. arbitrary units.

 Figure 6 – supplement 3. Hair bud progenitors revert their fate after WNT inhibitor washout. (**A**) Experimental design and results of pharmacological WNT inhibition and washout in embryonic skin explants exposed to 1mM porcupine inhibitor LGK974. Immunofluorescence and quantifications of normalized LEF1 pixel intensity. Note basal progenitors and dermal condensate restore LEF1/WNT 1113 signaling and WNT^{hi} bud cells recover their original (SOX9^{neg}) fate after inhibitor washout (n=109 developing hair follicles *****P* < 0.0001; ** p=0.0024 Mann-Whitney test). (**B**) Control experiment showing the viability of E15.5 embryonic skin explants after 36h of 1mM LGK974 and DMSO vehicle treatment. Explants were plated at the bud stage and in the DMSO control, they developed to the hair peg stage by 36 hr. Scale Bar 20μm.

 Figure 6 – supplement 4. Hair follicle progenitor cells co-express WNT reporter, LEF1, TCF1/7 and WNT target gene products FZD10 and WIF1*.* E9.5 skin was transduced with lentivirus harboring the WNT-reporter-GFP (*12xTCF-TK-EGFP*) and harvested at E15.5. Representative whole-mount immunofluorescence images show WNT reporter GFP positive progenitor cells co-localizing with LEF1. Further strengthening the validity of LEF1 as a *bona fide* WNT signaling, proxy, note that progenitor cells co-express LEF1 and TCF1/7 and express FZD10 and WIF1, products of WNT target genes. Circular yellow dashed lines outline placodes. White dashed lines demarcate epithelial-mesenchymal boundaries. Scale bars, 20μm.

 Figure 6 – supplement 5. NOTUM and WIF1 mis-localization leads to impaired development of hair follicles.(**A**) Experimental setup to induce mis-localization of WNT inhibitors by targeting them to the basal membrane. Transgenes were designed to express NOTUM and WIF1 as proteins tagged with an AQP4 peptide that targets the protein to the basal membrane. The C-terminal MYC tag was added for protein detection by immunofluorescence. LV constructs were transduced into E9.5 *Krt14rtTA* positive and negative mice. Expression was induced by Doxycycline at E9.5, and embryos were analyzed at E15.5. (**B**) NOTUM-AQP4 and (**C**) WIF1-AQP4, basal-apical MYC-Tag pixel intensity profiles denote the 1135 enrichment of their basal localization (NOTUM-AQP4 n=37 cells and WIF1-AQP4 n=28 Mean ± SEM.

1136 a.u., arbitrary units). **(D)** Quantifications to test efficiency of construct transduction (H2BGFP⁺ cells) and NOTUM and WIF1 ectopic and mis-polarized expression (Myc-tag and AQP4-Myc-tag respectively). Note the shift to basal polarization once the AQP4 tag is added to the construct. n= number of cells from ≥12 1139 hair follicles. (E) Quantifications of WIF1 mis-polarization (n=8mm²; n.s. non-significant, Man-Whitney test).

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