

# Image-based recommendations on styles and substitutes

**Julian McAuley, UCSD**

& Chris Targett, Qinfeng ('Javen') Shi, Anton van den Hengel, University of Adelaide

# Relationships between products



## Calvin Klein Men's Relaxed Straight Leg Jean In Cove

★★★★☆ 20 customer reviews

Price: \$48.16 - \$69.99 & FREE Returns. Details

Size:

Select [Sizing info](#) | [Fit: As expected \(55%\)](#)

Color: Cove

- 98% Cotton/2% Elastane
- Imported
- Button closure
- Machine Wash
- Relaxed straight-leg jean in light-tone denim featuring whiskering and five-pocket styling
- Zip fly with button
- 10.25-inch front rise, 19-inch knee, 17.5-inch leg opening

### Frequently Bought Together



Calvin Klein Jeans  
\$57.94 - \$69.50



Calvin Klein Jeans  
\$49.92



Calvin Klein Jeans  
\$50.67 - \$69.99



Levi's  
\$23.99 - \$68.00

### Customers Who Viewed This Item Also Viewed



### Customers Who Bought This Item Also Bought



# Relationships between products



↔ **browsed** together  
↔ **bought** together

# Modeling networks of images

## Understanding product networks with **images**

**Prediction:** Can we estimate whether two products are likely to be purchased/browsed together?

**Understanding:** Can we understand which products have compatible visual “styles”, and use this to recommend baskets of products to people?

# Relationships between products – why?

## 1. To understand the notions of **substitute** and **complement goods**



is substitutable for



complements



# Relationships between products – why?

## 2. To **recommend** baskets of related items

Query:



Suggested outfit:



Query:



Suggested outfit:





Amazon product network:

- thousands of **categories**
- 9 million **products**
- 21 million **users**
- 140 million **reviews**
- 300 million **relationships**



Four types of relationship:

- 1) People who **viewed** X also **viewed** Y
- 2) People who **viewed** X eventually **bought** Y
- 3) People who **bought** X also **bought** Y
- 4) People **bought** X and Y **together**

**Substitutes** (1 and 2), and **Complements** (3 and 4)



# Why might images be useful

- Visual explanations might be useful for some categories
- The image is the most important feature for many categories
  - Cold-start problems

# Problem setting

Binary prediction task:

Given a pair of products, **x and y**, predict whether they were purchased together, or whether they were chosen randomly

$$p(x \text{ and } y \text{ are related}) \sim -d(x, y)$$

# Problem setting

But we are not **given** a distance function:  
We need to **learn** the concept of similarity from data:

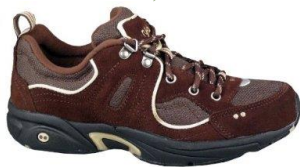
$$p_{\theta}(x \text{ and } y \text{ are related}) \sim -d_{\theta}(x, y)$$

Train  $\theta$  by maximum likelihood:

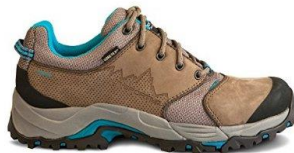
$$\theta = \arg \max_{\theta'} \prod_{\text{edges } (x,y)} p_{\theta}(x \text{ and } y \text{ are related}) \prod_{\text{non-edges } (x,y)} (1 - p_{\theta}(x \text{ and } y \text{ are related}))$$

# Problem setting

$$p(x \text{ and } y \text{ are related}) \sim -d(x, y)$$



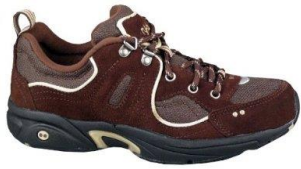
[0.723845, 0.153926, 0.757238, 0.983643, ... ]



[0.456353, 0.898354, 0.123342, 0.234253, ... ]

image features

# Problem setting



[0.723845, 0.153926, 0.757238, 0.983643, ... ]

4096-dimensional image features

We used **Caffe**, a convolutional neural net  
trained on **ImageNet**



# What are we actually learning?

How did Amazon generate their ground-truth data?

Given a product:



Let  $U_i$  be the set of users who viewed it

for every product in the corpus...



$U_1$

$U_2$

$U_3$

...

# What are we actually learning?

How did Amazon generate their ground-truth data?

Given a product:



Let  $U_i$  be the set of users who viewed it

Rank products according to:  $\frac{|U_i \cap U_j|}{|U_i \cup U_j|}$  ('Jaccard index')



# Attempt 1: distance between features

Features of (image of) product  $i$ :

$$\mathbf{x}_i = [0.723845, 0.153926, 0.757238, 0.983643, \dots]$$

Features of product  $j$ :

$$\mathbf{x}_j = [0.456353, 0.898354, 0.123342, 0.234253, \dots]$$

$$d(\mathbf{x}_i, \mathbf{x}_j) = \sum_k \theta_k (\mathbf{x}_{i,k} - \mathbf{x}_{j,k})^2$$



# Attempt 1: distance between features

Features of (image of) product  $i$ :

$$\mathbf{x}_i = [0.723845, 0.153926, 0.757238, 0.983643, \dots]$$

Features of product  $j$ :

$$\mathbf{x}_j = [0.456353, 0.898354, 0.123342, 0.234253, \dots]$$

At best we'll discover visual **similarity**,  
but visual relationships are more subtle

# Attempt 2: Mahalanobis distance

$$d(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i - \mathbf{x}_j)M(\mathbf{x}_i - \mathbf{x}_j)^T$$

$$M = \begin{pmatrix} 0.1 & 0.2 & \dots & 0.1 \\ 0.2 & 0.1 & & 0.6 \\ \vdots & & \ddots & \vdots \\ 0.1 & 0.6 & \dots & 0.1 \end{pmatrix}$$

texture

color

## Attempt 2: Mahalanobis distance


$$d(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i - \mathbf{x}_j)M(\mathbf{x}_i - \mathbf{x}_j)^T$$

- High-dimensional
- Prone to overfitting
- Too slow!

# Attempt 3: Low-rank Mahalanobis

$$d(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i - \mathbf{x}_j)M(\mathbf{x}_i - \mathbf{x}_j)^T$$

Replace  $M$  by an  
approximation of  
low rank



$$d(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i - \mathbf{x}_j)UU^T(\mathbf{x}_i - \mathbf{x}_j)^T$$

$$d_v(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i - \mathbf{x}_j)U\Delta_vU^T(\mathbf{x}_i - \mathbf{x}_j)^T$$

user



user-personalized transform



(see paper)

# Attempt 3: Low-rank Mahalanobis

$$\text{let } \mathbf{s}_i = \mathbf{x}_i U$$

$(1 \times K)$        $(1 \times F)$        $(F \times K)$

$$\text{then } d(\mathbf{x}_i, \mathbf{x}_j) = \|\mathbf{s}_i - \mathbf{s}_j\|_2^2$$

We call this the 'style space' embedding of  $\mathbf{x}$

# Training

$$U = \arg \max_{U'} \prod_{\text{edges } (x,y)} p_U(x \text{ and } y \text{ are related}) \prod_{\text{non-edges } (x,y)} (1 - p_U(x \text{ and } y \text{ are related}))$$

# Results

## Books

rank (K)	buy after viewing	also viewed	also bought	bought together	average
1	66.3%	66.1%	66.7%	60.7%	<b>65.0%</b>
10	72.4%	71.6%	72.1%	68.8%	<b>71.2%</b>
100	73.5%	72.4%	73.6%	69.0%	<b>72.1%</b>

## Electronics

rank (K)	buy after viewing	also viewed	also bought	bought together	average
1	68.4%	74.7%	64.5%	72.3%	<b>67.5%</b>
10	83.4%	80.4%	77.6%	78.0%	<b>79.9%</b>
100	85.7%	84.0%	82.3%	82.4%	<b>83.6%</b>

# Results

## Clothing

rank (K)	also viewed	also bought	bought together	average
1	78.7%	75.4%	78.9%	<b>77.7%</b>
10	88.2%	86.8%	90.7%	<b>88.6%</b>
100	90.0%	90.8%	93.8%	<b>91.5%</b>

## Shoes

rank (K)	also viewed	also bought	bought together	average
1	78.4%	78.9%	89.5%	<b>82.3%</b>
10	94.1%	95.3%	96.1%	<b>95.2%</b>
100	96.6%	97.6%	97.9%	<b>97.4%</b>



# Visualizing 'style space'

We've projected images into a low dimensional space encoding their style, what are the "extreme" points?



# Visualizing 'style space'



# Visualizing 'style space'



# Visualizing 'style space'

Which styles are at **opposite** ends of the spectrum?



# Generating recommendations

How can we use the system to generate recommendations?

Query:



Suggested outfit:



# Generating recommendations

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Query:



Suggested outfit:



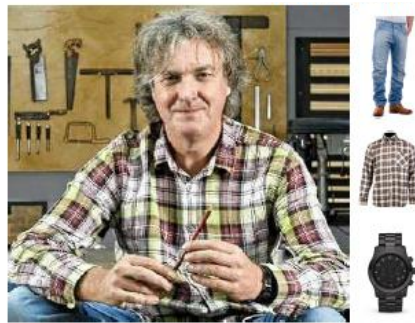


# Generating recommendations



# Outfits in the wild

## Least coordinated



## Most coordinated



# Outfits in the wild

## Old outfits



## New outfits

Change in log-likelihood

# Questions?

## Co-authors:



Christopher  
Targett



Qinfeng  
"Javen" Shi



Anton van  
den Hengel

(The University of Adelaide)