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### **Paper:**

Bye, I., North, P., Los, S., Kljun, N., Rosette, J., Hopkinson, C., Chasmer, L. & Mahoney, C. (2017). Estimating forest canopy parameters from satellite waveform LiDAR by inversion of the FLIGHT three-dimensional radiative transfer model. *Remote Sensing of Environment*, 188, 177-189.  
<http://dx.doi.org/10.1016/j.rse.2016.10.048>

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# Estimating Forest Canopy Parameters From Satellite Waveform LiDAR by Inversion of the FLIGHT Three-Dimensional Radiative Transfer Model

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## Abstract

The Geoscience Laser Altimeter System (GLAS) has the potential to accurately map global vegetation heights and fractional cover metrics using active laser pulse emission/reception. However, large uncertainties in the derivation of data products exist, since multiple physically plausible interpretations of the data are possible. In this study a method is described and evaluated to derive vegetation height and fractional cover from GLAS waveforms by inversion of the FLIGHT radiative transfer model. A lookup-table is constructed giving expected waveforms for a comprehensive set of canopy realisations, and is used to determine the most likely set of biophysical parameters describing the forest structure, consistent with any given GLAS waveform. The parameters retrieved are canopy height, leaf area index (LAI), fractional cover and ground slope. The range of possible parameters consistent with the waveform is used to give a per-retrieval uncertainty estimate for each retrieved parameter. The retrieved estimates were evaluated first using a simulated data set and then validated against airborne laser scanning (ALS) products for three forest sites coincident with GLAS overpasses. Results for height retrieval show mean absolute error (MAE) of 3.71 m for a mixed temperate forest site within Forest of Dean (UK), 3.35 m for the Southern Old Aspen Site, Saskatchewan, Canada, and 5.13 m for a boreal coniferous site in Norunda, Sweden. Fractional cover showed MAE of 0.10 for Forest of Dean and 0.23 for Norunda. Coefficient of determination between ALS and GLAS estimates over the combined dataset gave  $R^2$  values of 0.71 for height and 0.48 for fractional cover, with biases of -3.4 m and 0.02 respectively. Smallest errors were found where overpass dates for ALS data collection closely matched GLAS overpasses. Explicit instrument parameterisation means the method is readily adapted to future planned spaceborne LiDAR instruments such as GEDI.

*Keywords:*

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## 1. Introduction

Satellite laser altimeters have the capacity to provide global estimates of vegetation height and structure (Lefsky, 2010; Simard et al., 2011; Los et al., 2012). This can provide an important baseline for future assessment and comparison of forest structural changes, including biomass. Such estimates are needed to inform and test models of carbon sequestration (Ciais et al., 2013), and to monitor changes in carbon stocks due to climatic change and both natural and human disturbance (Goetz and Dubayah, 2011).

7 While passive optical systems have been used extensively to observe vegetation covered land by measuring the  
8 spectral properties of the surfaces, such systems are limited in their ability to measure vertical structure below the  
9 upper surface of the canopy. Active light detection and ranging (LiDAR) systems have addressed this, providing  
10 information about the vertical profile of a forest canopy. Waveform LiDAR has been in use since the early 1980s,  
11 when the Wallops Flight Facility's AOL airborne laser scanner was used to profile a 14 km flight line near Doubling  
12 Gap, Pennsylvania (Nelson et al., 1984). Height and density metrics were compared with photogrammetry derived  
13 values and the results were encouraging; height means were within 0.6 m of their respective photointerpreted values.  
14 Aldred et al. (1985) also demonstrated that waveform recording LiDAR had the potential to mitigate one of the  
15 problems arising from the use of discrete-return LiDAR, which was the systematic underestimation of stand height.  
16 In the 1990s, first Scanning LiDAR Imager of Canopies by Echo Recovery (SLICER) (Means et al., 1999; Lefsky  
17 et al., 1999a,b; Harding et al., 2001) and then Laser Vegetation Imaging Sensor (LVIS) (Blair et al., 1999; Drake et al.,  
18 2002) were developed by NASA as demonstrators for potential spaceborne LiDAR.

19 In the decade following, the Geoscience Laser Altimeter System (GLAS), a space-borne waveform instrument,  
20 was carried on the ICESat mission (Brenner et al., 2003). While GLAS was primarily designed to measure ice sheet  
21 topography, secondary objectives included measurements of vegetation height and land surface elevation. Launched in  
22 January 2003, the mission lasted until October 2009 when its instrument failed. The mission platform was placed in a  
23 183 day ground track repeat cycle, to provide a 15 km spacing between tracks at the equator and 2.5 km at 80° latitude.  
24 Using GLAS data, canopy height has been estimated directly from the Gaussian wave components of a decomposed  
25 LiDAR waveform (Harding and Carabajal, 2005; Lefsky et al., 2005, 2007; Rosette et al., 2009; Duncanson et al.,  
26 2010), and volume has also been successfully derived (Rosette et al., 2008a; Nelson et al., 2009; Popescu et al., 2011).  
27 More recently, near global datasets of height for forest (Lefsky, 2010; Simard et al., 2011) and total vegetation (Los  
28 et al., 2012) have demonstrated the importance of the near-global coverage of GLAS. Los et al. (2012) conclude that  
29 the GLAS height product appears to be better suited as an input to ecological and climate models than existing data  
30 sets based on land cover alone.

31 For the previous two decades, the use of LiDAR to map biomass has increased dramatically. It is likely that over the  
32 next decade, in combination with other forms of remote sensing, LiDAR will become increasingly central to mapping  
33 biomass at regional, national or continental scales (Goetz and Dubayah, 2011; Wulder et al., 2012; Neigh et al.,  
34 2013). In particular, upcoming space borne LiDAR missions, such as the Global Ecosystems Dynamics Investigation  
35 (GEDI) LiDAR (Dubayah et al., 2014; Coyle et al., 2015) and the second generation ICESat-2 (Abdalati et al., 2010;  
36 Montesano et al., 2015) will have the potential to improve and update a definitive baseline for global biomass stocks.

37 The complex structure of a vegetation canopy in combination with uncertainties arising from instrument, suggest  
38 that remote sensing of vegetation biophysical parameters is an ill-posed problem; that is, multiple interpretations of  
39 the measured radiative signal are possible. A physically based radiative transfer model (RTM) (e.g. (Sun and Ranson,  
40 2000; Ni-Meister et al., 2001b; Disney et al., 2006; North et al., 2010)) can be used to describe the interaction of  
41 radiation with canopy elements and explicitly relate canopy parameters, observation and illumination variables and

42 remote sensing signature.

43 Model inversion may be considered a multi parameter optimisation problem. However iterative numerical opti-  
44 misation methods tend to be computationally intensive, and may not be appropriate for applications on a per-pixel  
45 basis for regional and global data (Kimes et al., 2002). An efficient approach to model inversion is the lookup table  
46 (LUT) method. It involves: generating of a table of reflectance signatures by varying the values of a set of reflectance  
47 model input parameters, comparing an observed signal against all signatures in the LUT to determine the best fit and  
48 corresponding set of parameters. Unlike iterative optimisation based approaches, LUTs can be applied to computa-  
49 tionally expensive and complex models without any modifications, and so are particularly suitable for Monte Carlo  
50 or ray tracing models such as the 3D radiative transfer model, FLIGHT, we have used in this study (Weiss et al.,  
51 2000; Leonenko et al., 2013). Also, unlike iterative methods, LUTs do not require a set of initial values, preventing  
52 the chance of poor values leading to non-global minima. The effectiveness of the LUT approach to model inversion  
53 is sensitive to the accuracy of the RT model, but also to assumptions concerning choice of LUT generation param-  
54 eters and crown macro-structure and shape. Turbid medium geometric primitives are typically used to model LUT  
55 canopy realisations due to their simplicity. However, studies (Calders et al., 2013; Widlowski et al., 2014) suggest  
56 that biophysical parameter retrieval may be sensitive to choice of crown shape or internal structure, and further work  
57 is recommended to improve understanding of this.

58 Several studies have applied model inversion to airborne LiDAR waveform (Koetz et al., 2006, 2007; Ma et al.,  
59 2015). In particular LUTs have been used previously to invert LiDAR data with some success by Koetz et al. (2006),  
60 who inverted a 3D LiDAR waveform model (Sun and Ranson, 2000). Subsequently, Koetz et al. (2007) investigated  
61 the fusion of imaging spectrometer and LiDAR data, demonstrating greater constraint on LAI. The inversion was  
62 tested on both simulated data and waveform data synthesised from small-footprint data acquired in the Swiss National  
63 Park, showing good correlation with retrieved parameters.

64 Existing datasets of height derived from GLAS show higher disagreement for regions of dense forest cover and  
65 higher ground slopes (Los et al., 2012; Xing et al., 2010); a physically-based joint retrieval of slope, cover and  
66 height has potential to improve accuracy over such regions. Fractional cover has previously been estimated (Los  
67 et al., 2012) over wider regions by statistical sampling, assuming each footprint represents either zero or complete  
68 vegetation cover, rather than per-footprint. This study aims to develop and evaluate a model inversion method suitable  
69 for satellite LiDAR waveform observations, to retrieve simultaneously parameters such as maximum canopy height  
70 ( $H_{top}$ ), fractional cover ( $F_c$ ), underlying topography and estimates of their error. In the following sections we will  
71 describe a lookup table (LUT) based inversion of the three-dimensional radiative transfer model FLIGHT (North,  
72 1996; North et al., 2010) and evaluate the retrieval using GLAS waveform data, validated against airborne laser  
73 scanning data.

## 74 2. Method

75 In this section we first describe the FLIGHT (North, 1996; North et al., 2010) radiative transfer model applied to  
76 simulation of GLAS waveforms. We next outline generation of a lookup table for performing model inversion. Finally  
77 we describe the method for determining the most likely set of biophysical parameters describing the forest structure  
78 for a given waveform, and error estimates associated with these parameters.

### 79 2.1. FLIGHT Radiative Transfer Model

80 The FLIGHT radiative transfer model simulates vegetation bidirectional reflectance and LiDAR return by applying  
81 Monte Carlo simulation of photon transport within a three dimensional representation of vegetation structure. In the  
82 original radiative transfer mode of operation of FLIGHT (North, 1996), photon trajectories are traced forwards from  
83 the source, through a sequence of interactions between and within crown boundaries. At each interaction a photon  
84 may be absorbed, reflected or transmitted and this process is modelled with a continuous probability density function.  
85 On leaving the canopy boundary, energy is accumulated in bins defined for each solid angle of exit. The LiDAR  
86 mode of the model (North et al., 2010) samples the paths of individual photons received within the field of view of a  
87 given sensor position, accumulating path length and energy from both laser and solar sources and including multiple  
88 scattering events.

89 Large-scale forest structure is modelled by a set of geometric primitives, either ellipsoidal or conical, giving  
90 approximate extent of foliage vertical and horizontal extent. The representation is widely used to allow modelling  
91 of the main characteristics of three-dimensional forest canopies, but which remains computationally tractable by  
92 allowing a semi-analytic radiative transfer approach (Ni-Meister et al., 2001a; Duursma et al., 2012; North, 1996). A  
93 simple growth model is used to limit the degree of overlap between neighbouring crowns. Inside each crown, foliage  
94 is modelled using the parameters of leaf area density, leaf angle distribution (LAD), size and the optical parameters  
95 of reflectance and transmittance. The parameters are set to be homogeneous within a crown but are allowed to vary  
96 between crowns. The effect of slope is incorporated into the model using a planar surface with defined slope angle.

97 For LiDAR simulation, the model calculates the probability distribution of return of a photon emitted from the  
98 laser as a function of time, and has been compared with field and satellite observations (North et al., 2010; Rosette  
99 et al., 2010; Morton et al., 2014).

### 100 2.2. LUT-Based Inversion

101 Inverting the LiDAR waveform model was performed using a LUT approach to allow an efficient retrieval of the  
102 range of parameters possible for a given waveform. The LUT inversion requires two stages. Firstly, prior to inversion,  
103 we use the FLIGHT model to generate the LUT. Each entry in the LUT contains a waveform, and the corresponding  
104 biophysical parameter set which gave rise to that waveform. Secondly, during operation of the inversion, we automat-  
105 ically select from the LUT the solution or solutions whose simulated waveform in the LUT best matches to a given  
106 observed waveform.

107 The LUT was generated by modelling LiDAR waveforms, representing a total of 107100 unique canopy represen-  
108 tations. For each: a combination of LUT parameter values was selected from within a defined range, a corresponding  
109 3D representation of a forest stand was simulated and photon paths modelled. Values for leaf reflectance and trans-  
110 mittance were derived from the LIBERTY model (Dawson et al., 1998, 2003) based on field measurements of leaf  
111 structure and pigmentation from the BOREAS campaign (Hall, 1999; Plummer and Curran, 1998), while understory  
112 reflectance was based on field measurements from this campaign (Hall et al., 2000). Sensor configuration and location  
113 were fixed to appropriate GLAS specifications. The set of parameters defining the LiDAR sensor are listed in Table  
114 1, along with example values for GLAS (Brenner et al., 2003).

115

Table 1: FLIGHT LiDAR sensor model and GLAS specific values.

Parameter	Description	Unit	Value
$(P_x, P_y, P_z)$	Sensor position relative relative to scene	$m$	(0, 0, 600000)
$\theta_o$	Sensor zenith angle	$deg$	0
$\phi_o$	Sensor azimuth angle	$deg$	0
$s_l$	RMS pulse width	$ns$	5
$q_T$	Half width angle of beam divergence	$rad$	0.00011
$IFOV$	Detector IFOV	$rad$	0.0004
$A_T$	Detector telescope area	$m^2$	0.709
$T_{RTsm}$	Roundtrip atmosphere transmittance	–	0.8 (532 nm) 0.9 (1024 nm)
$E_{trans}$	Total pulse energy	$mJ$	32 (532 nm) 72 (1024 nm)
$\Delta_t$	Recording bin width	$ns$	1

116 Tree crowns were modelled as ellipsoidal. Horizontal tree positioning within a scene was random and tree heights  
117 were uniformly distributed between a specified minimum and maximum height range. The LUT was designed to  
118 contain a wide range of possible tree height arrangements, including stands with highly variable heights (i.e. the  
119 maximum range  $H_{min}-H_{max}$  is large) and stands with a single height canopy (i.e. the maximum range  $H_{min}-H_{max}$  is 1  
120 m). While a single layer canopy is used here, more complex structures, for example to include an understory layer,  
121 are possible with the same methodology.

122 A subset of FLIGHT parameters, comprising leaf area index  $LAI$ , fractional cover  $F_c$ , lower limit height of first  
123 branch  $H_{min}$ , upper limit height of first branch ( $H_{max}$ ), slope ( $S_y$ ), canopy radius ( $E_{xy}$ ) and for the ellipsoidal crowns  
124 used in this study, canopy radius in the vertical axis ( $E_z$ ), was chosen for the LUT variables to ensure that a sufficiently  
125 broad range of stand height and coverage could be simulated. Slope referred to the angle from horizontal, of a flat

Table 2: FLIGHT parameters and ranges treated as variables for the generation of the LUT. Additional parameters (e.g. leaf optical properties and angular distribution) were fixed to default, broadleaf canopy, settings.

Parameter	Description	Unit	Min	Max	Step
$LAI$	Mean one-sided foliage area per unit area	$m^2m^{-2}$	0.4	6.1	0.1
$H_{max}$	Maximum height to first branch	$m$	1	17	2
$H_{min}$	Minimum height to first branch	$m$	0	16	2
$F_c$	Fraction of ground covered by vegetation	%	20	80	10
$S_y$	Ground slope	$deg.$	0	20	5
$E_{xy}$	Crown horizontal radius	$m$	1	4	1
$E_z$	Crown vertical radius	$m$	2	8	2

126 plane, and is assumed to mean ‘equivalent slope’, and relates to the average change in elevation within a GLAS foot-  
 127 print. It is not possible to differentiate between localised surface roughness and footprint scale changes in elevation.  
 128 The parameter ranges used are listed in Table 2. The remaining FLIGHT parameters were fixed to default values. The  
 129 LUT generated using these parameters reflects a simplified representation of natural forest structures and as such the  
 130 robustness and accuracy of this investigation can only be considered as an indication of the ability of this approach to  
 131 retrieve accurate forest biophysical parameters.

132 The solution of the model inversion was then found by ranking the distance using a Chi-Square metric ( $\chi^2$ ) between  
 133 a reference waveform ( $\omega_{ref}$ ) provided by GLAS and a simulated waveform ( $\omega_{sim}$ ) from the LUT as modelled by  
 134 FLIGHT. To ensure equivalence, both waveforms were normalised by total waveform energy. A merit function was  
 135 adopted:

$$\chi^2 = \sum_{i=1}^{n_{bin}} \left( \frac{\omega_{ref}[i] - \omega_{sim}[i]}{\sigma_n} \right)^2 \quad (1)$$

136 where  $n_{bin}$  is the number of bins of the waveform. The estimated total uncertainty for each bin  $\sigma_n$  is the total sum  
 137 of uncertainties arising from errors ( $\sigma_{model}$ ) such as those in the model physics and real world representation (e.g. a  
 138 turbid medium approximation, vertical distribution of LAI), deviation from values of default parameters (e.g. leaf  
 139 reflectance, soil reflectance), combined with the estimated measurement errors ( $\sigma_{measure}$ ) associated with the data.  
 140 The measurement and model errors are described in further detail in the following section.

$$\sigma_n^2 = \sigma_{measure}^2 + \sigma_{model}^2 \quad (2)$$

### 141 2.3. Error Estimates

142 A practical estimate of model error  $\sigma_{model}$  under real conditions was made empirically, derived from the error in  
143 model fit for a set of 66 GLAS waveforms over Forest of Dean, UK, which comprises a range of mixed broadleaf  
144 and coniferous forest species on sloping ground (Rosette et al., 2008b). A full description of the Forest of Dean site  
145 is given in Section 3. Errors were approximated as following a Gaussian distribution, and explaining the deviation  
146 between GLAS waveform and FLIGHT model waveform as the combination of model and measurement error, after  
147 finding of the best model fit to each waveform. An estimated measurement error  $\sigma_{measure}$ , for each waveform was  
148 calculated as the standard deviation of the ‘noise’ from a non-signal portion of the waveform. Considering the reduced  
149 Chi-Square ( $\chi_{red}^2$ ):

$$\chi_{red}^2 = \frac{\chi^2}{\nu} \quad (3)$$

150 where  $\nu$  is Degrees of Freedom given by  $N - n - 1$ , where  $N$  is total number of observations, and  $n$  is the number  
151 of fitted parameters. If  $\chi_{red}^2 \approx 1$  indicates a good model fit, then  $\chi^2 \approx \nu$ .

152 If  $\sigma_n$  is assumed to be constant for all samples then an estimate for  $\sigma_n = \sigma$  can be determined empirically for each  
153 waveform of a set of data from (1). Using:

$$\sigma^2 = \frac{1}{\nu} \sum_{i=1}^{n_{bin}} (\omega_{ref}[i] - \omega_{sim}[i])^2 \quad (4)$$

154 Consequently, an estimate for  $\sigma_{model}^2$  was obtained from each waveform fit of the reference data set by (2). The  
155 underlying assumption is that the closest model fit to the ‘true’ forest structure has been found by the inversion, and  
156 (2) gives an approximation of the total remaining (non-parameter) error  $\sigma_{model}^2$  including model physics, errors in  
157 unknown/default variables such as ground reflectance, and quantisation in the LUT.

158 Using the Forest of Dean data as a reference data set an estimate for  $\sigma_{model}$  was found to be  $\approx 0.001$  Normalised  
159 Intensity ( $I_N$ ). Subsequent analysis on all data sets: simulated, Forest of Dean (FOD), Southern Old Aspen (SOA)  
160 and Norunda (NOR) data sets included this previously determined  $\sigma_{model}$  alongside a measurement error  $\sigma_{measure}$   
161 estimated from the non-signal region of the waveform being analysed.

162 To account for the ill-posed nature of the model inversion, where a number of possible solutions may exist due  
163 to measurement or model uncertainties, the LUT was ranked according to a metric  $\chi^2$ . The first  $n = 1, 10, 100$   
164 simulated waveforms were accepted to be candidate solutions and the mean of each of the parameters was considered  
165 the solution.

## 166 3. Validation Data

### 167 3.1. Forest Sites

168 Three sites were selected for validation of the method: a mixed temperate forest site within Forest of Dean (FOD),  
169 UK, the Southern Old Aspen Site (SOA), Saskatchewan (Canada) and a boreal coniferous site in Norunda (NOR),



170 Sweden. These sites were chosen to provide a range of temperate and boreal forest types, and as they have been well  
171 characterised using coincident ALS data and field survey for regions overlapping with GLAS tracks. Key characteris-  
172 tics for the three study sites are summarised in Table 3.

173 Sources of uncertainty to consider include errors in the reference ALS data. Andersen et al. (2006) aimed to  
174 quantify the accuracy of tree height measurements made using ALS over conifer study sites and found that accuracy  
175 was influenced by point density as determined by beam divergence. For a nominal 6 p/m<sup>1</sup> the negative bias in height  
176 retrieval was found to be -0.73 m (SD = 0.43 m) for the narrow beam (0.33 m diameter footprint) LiDAR and -1.12  
177 m (SD = 0.56 m) for wider beam (0.8 m). In a previous study Gaveau and Hill (2003) attempted a similar study, this  
178 time for broadleaf woodland. They reported a negative bias of 1.12 m for tree height but also note that converting  
179 point data into grid format CHM data further propagated error, resulting in a negative bias of 2.12 m (RMSE = 1.89  
180 m). Canopy cover reference data was also derived from ALS data. However, Rosette et al. (2009) showed that a good  
181 relationship with field based estimates was possible, despite a relatively small data range. Testing ALS estimates  
182 of fractional cover with hemispherical photography they found  $R^2 = 0.77$  and RMSE = 0.02. A second source of  
183 error pertaining to the reference data may be attributed to the use of a slightly different approach for the derivation of  
184 parameters from FOD data to that used for the SOA and NOR reference data. At the time of the investigation only  
185 these derived parameters were available.

186 It should be noted that the Norunda site was subject to a considerable difference in time between the acquisition  
187 of the GLAS data (2003) and the airborne LiDAR data (2011). Many of the Norunda height parameter estimates  
188 were affected by vegetation growth occurring between the two data set acquisition dates. In the case of the fractional  
189 cover, land cover differences through forestry activities such as harvesting or thinning may also explain a number of  
190 overestimated outlier points.

### 191 3.1.1. Forest of Dean

192 The first study site was located in The Forest of Dean (FOD), Gloucestershire, UK. The forest covers an area of  
193 approximately 11,000 ha and is managed by the Forestry Commission of Great Britain. The site comprises mixed tem-  
194 perate species, mainly: Norway spruce (*Picea abies*), oak (*Quercus spp.*), Corsican pine (*Pinus nigra var maritima*),  
195 Douglas fir (*Pseudotsuga menziesii*), Scots pine (*Pinus sylvestris*) and European larch (*Larix decidua*).

196 Airborne LiDAR data were used as a proxy for ground truth data. Airborne data for the Forest of Dean study site  
197 were acquired during August 2006, using the Optech Airborne Laser Terrain Mapper (ALTM-3033) sensor system.  
198 The aerial survey was carried out by the the Natural Environment Research Council Airborne Research and Surveying  
199 Facility (ARSF) (through the Unit for Landscape Modelling, University of Cambridge), on behalf of the Forestry  
200 Commission of Great Britain Forest Research Agency.

201 For FOD airborne LiDAR data, the log ASCII standard (LAS) format data were processed by Rosette et al. (2008b)  
202 using the method described by Streutker and Glenn (2006). Return points were classified into vegetation and ground  
203 classes and a ground surface model was interpolated using Delaunay triangulation. Mean footprint slope was derived

Table 3: Characteristics of forest sites used for validation.

	FOD	SOA	NOR
Region	Forest of Dean, Great Britain	Saskatchewan, Canada	Norunda Common, Sweden
Location	51.81° N, 2.52° W	53.63° N, 106.20° W	60.09° N, 17.48° E
Elevation above sea level (m)	50–225	524–572	34–83
Topography	Moderate relief	Low relief	Low relief
Main species	Norway spruce ( <i>Picea abies</i> ), Oak ( <i>Quercus spp.</i> ), Corsican pine ( <i>Pinus nigra</i> ), Douglas fir ( <i>Pseudotsuga menziesii</i> ), Scots pine ( <i>Pinus sylvestris</i> ), European larch ( <i>Larix decidua</i> )	Trembling aspen ( <i>Populus tremuloides</i> ), Hazelnut ( <i>Corylus cornutta</i> )	Norway spruce ( <i>Picea abies</i> ), Scots pine ( <i>Pinus sylvestris</i> )
Max canopy height (m)	30	21	28

204 from the surface model. Fractional cover ( $F_c$ ) estimates were calculated as the fraction of vegetation class point count  
 205 over the total point count. Only vegetation points over 0.5 m above the interpolated ground surface were counted such  
 206 that, only canopy and taller understory affecting GLAS waveform were included in the observed fractional cover.  
 207 Maximum canopy height within each airborne LiDAR subset was then calculated to allow a comparison to be made  
 208 with estimated ICESat/GLAS height parameter.

### 209 3.1.2. Saskatchewan

210 The second study site is located within the southern boreal forest of Saskatchewan, Canada. The Southern Old  
 211 Aspen (SOA) site was first established as part of the Boreal Ecosystem Research and Monitoring Site (BERMS) study  
 212 (Barr et al., 2004, 2006; Black et al., 1996; Kljun et al., 2007) and lies approximately 10 km north of the transition  
 213 zone between agriculture and forest. Located near the southern end of the Prince Albert National Park, the SOA  
 214 site (Barr et al., 2004, 2006; Black et al., 1996; Chasmer et al., 2011) is predominately uniformly aged trembling  
 215 aspen (*Populus tremuloides* Michx.) with hazelnut (*Corylus cornutta* Marsh) dominating the under storey (Barr et al.,  
 216 2006). The terrain is mainly flat, with a site mean slope of  $\approx 2^\circ$  (Mahoney et al., 2014) and the  $\approx 21$  m stand  
 217 height is relatively even due to natural regeneration after a wildfire in 1919 (Blanken et al., 1997; Amiro et al., 2006;  
 218 Kljun et al., 2007). Airborne LiDAR data covering the SOA site were acquired on behalf of the authors in August  
 219 2008, by the Applied Geomatics Research Group (AGRG) and the Canadian Consortium for LiDAR Environmental  
 220 Applications Research (C-CLEAR), using an Optech ALTM-3100 system.

### 221 3.1.3. Norunda

222 A third study site is located at Norunda (NOR) (Lindroth et al., 1998; Feigenwinter et al., 2010; Lagergren et al.,  
223 2005), situated 30 km north of Uppsala, Sweden. The site is at the southern part of the boreal forest zone and  
224 is part of the integrated carbon observation system (ICOS Sweden) research infrastructure. Norway spruce (*Picea*  
225 *abies*) and Scots pine (*Pinus sylvestris*) dominate the site, while there is a smaller fraction of deciduous vegetation  
226 (approximately 15%), predominately birch (*Betula sp.*) (Lindroth et al., 1998). The area is generally flat with some  
227 localised variations in elevation less than 10 m. Corresponding airborne data were acquired in June 2011 by the ARSF  
228 on behalf of the authors. A Leica ALS50-II LiDAR instrument was used.

229 For both the Southern Old Aspen and Norunda sites, airborne LiDAR data were processed by Chasmer et al.  
230 (2011); Mahoney et al. (2014); Kljun et al. (2013). Canopy height was derived using the IDW algorithm within a 2.5  
231 m search radius of classified canopy reflections greater than 0.5 m above the ground (Hopkinson et al., 2005). Canopy  
232 fractional cover was calculated using the Beer's Law laser intensity method (Hopkinson and Chasmer, 2009).

### 233 3.2. GLAS Data

234 Waveform data in this study were acquired by the Geoscience Laser Altimeter System (GLAS) (Brenner et al.,  
235 2003; NSIDC, 2014). The GLAS instrument employed three Nd:YAG lasers (designated Laser 1, 2 and 3), to operate  
236 one at a time, at 1064 nm and 532 nm wavelengths. The 1064 nm pulse was used for measuring surface and dense  
237 cloud elevations, and , and the 532 nm pulse was used to measure the vertical distribution of clouds and aerosols. For  
238 this study, only the 1064 nm pulse was used. The instrument was required to operate at a nominal 600 km altitude  
239 and with a 375 microradian field of view to illuminate a footprint size of  $70 \pm 10$  m (Brenner et al., 2003), however  
240 footprints were found to be elliptical and averaged  $48 \text{ m} \times 102 \text{ m}$  for Laser periods 1A through to 2C and  $47 \text{ m} \times$   
241  $57 \text{ m}$  for the Laser periods 3A through to 3K (NSIDC, 2014). A pulse frequency of 40 Hz resulted in a distance of  
242 approximately 175 m between the spots measured centre-to-centre.

243  $4,500,000 \times 1 \text{ ns}$  samples were collected for each transmitted 1064 nm pulse and on-board processing reduced  
244 this to 544 and 200 samples to be telemetered over ice sheet or land, and sea ice or water surface respectively. For  
245 the Laser 1a and 2a periods, this was designed to yield a range window of 81.6 m for land and ice sheet or 30 m for  
246 water surface (Schutz et al., 2005). However, the on-board software truncated the signal from the upper part of tall  
247 vegetation or particularly steep slopes and so for later operational periods a compression scheme was introduced to  
248 increase the overall land height range to 150 m (lower 392 bins at 1 ns = 58.8 m, upper 152 bins at 4 ns = 91.2 m)  
249 (Harding and Carabajal, 2005).

250 All waveform data used in the study were from the level one (L1A) GLA01 product (Zwally et al., 2011) which  
251 comprise the raw altimetry data as transmitted from the space vehicle, and includes the long (544 or 1000 bin) and  
252 short (200 bin) waveforms. Waveform footprint geolocation data were taken from the GLA14 product (Zwally et al.,  
253 2014). Footprint geolocation accuracy was known to be  $< 1 \text{ m}$  for data releases V026 and onwards.

254 Forest of Dean data were taken from release V026, and were acquired on 22nd October 2005 (laser 3D, Id:  
 255 885917496, 885917506, 885917516). The original dataset included 86 overpass footprints, but filtered to a set of 66  
 256 to avoid artificial objects such as buildings and roads (Rosette et al., 2008b). For the Southern Old Aspen site, 22  
 257 footprints of GLAS data were available from release V031, acquired 21st February 2003. The laser period was laser  
 258 1A. Historical weather data records from Environment Canada indicate that there was approximately 23 cm snow  
 259 cover on the date of the GLAS data acquisition (Environment Canada, Government of Canada, 2014). A total of 99  
 260 GLAS footprints for the Norunda study site data were acquired over two dates: 49 footprints on 22nd February 2003  
 261 (laser 1A, Id: 22494495) and 50 footprints on 25th September 2003 (laser 2A, Id: 115682811), both from release  
 262 V033.

### 263 3.3. Converting Fractional Cover to Projected Cover

264 The standard FLIGHT model output within the LUT of *fractional cover* ( $F_c$ ) is defined as vertically projected total  
 265 crown cover. A further LUT entry  $P_c$  is derived to approximate fractional cover compatible with airborne LiDAR, of  
 266 vertically projected foliage area for tree crowns. This is calculated using the conversion formula:

$$P_c = F_c \left( 1 - e^{-k \left( \frac{LAI}{F_c} \right)} \right) \quad (5)$$

267 was used, where  $k$  was chosen to be 0.5.

## 268 4. Results

### 269 4.1. Sensitivity analysis

270 The model inversion was applied first to a simulated data set to determine the ability to retrieve parameters from  
 271 individual waveforms and assess likely error. A set of 1000 waveforms representing a range of forest canopy re-  
 272 alisations were created by running FLIGHT. Canopy parameters were sampled randomly within a subset of ranges  
 273 specified in Table 4.

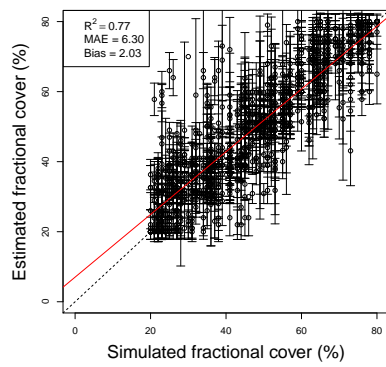
274  $R^2$ , MAE and bias for all solution-set sizes are summarised in Table 5. For the simulated data set, fractional cover  
 275 and height were well estimated with high  $R^2$  (0.77 and 0.91, respectively) and low mean absolute errors (MAE) (6.30  
 276 % and 1.30 m, respectively). Scatterplots with the distribution of results are shown in Figures 1a and 1b. Furthermore,  
 277 close proximity to the 1:1 line demonstrate the potential of this method to retrieve height. For the retrieval of canopy  
 278 vertical radius,  $R^2$  and MAE (0.77 and 0.96 m, respectively) are reasonable (Figure 1c). However, relatively large  
 279 standard deviations in individual estimates indicate a higher degree of uncertainty in estimates for this parameter. A  
 280 very high  $R^2 = 0.93$  for slope estimation (see Figure 1d) provides further evidence to suggest that the LUT method  
 281 might be suitable for estimating topography simultaneously with other forest parameters. Low variability within the  
 282 solution sets is evident from the low standard deviation.

Table 4: FLIGHT parameters and ranges treated as variables for the generation of waveforms representing the forest canopy realisations belonging to the simulated data set. Additional parameters were fixed to the same default settings as with the generation of the LUT.

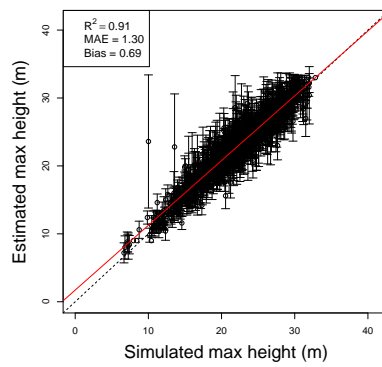
Parameter	Description	Unit	Min	Max
$LAI$	Mean one-sided foliage area per unit area	$m^2m^{-2}$	2.0	6.0
$H_{min}$	Min height to first branch	$m$	0.0	16.0
$H_{max}$	Max height to first branch	$m$	0.0	17.0
$F_c$	Fraction of ground covered by vegetation	%	20	80
$S_y$	Ground slope	$deg.$	0	20
$E_{xy}$	Crown horizontal radius	$m$	2.0	4.0
$E_z$	Crown vertical radius	$m$	2.0	6.0

Table 5: Chi-Square summary statistics on simulated dataset, for solution sizes  $n = 1, 10, 100$ .

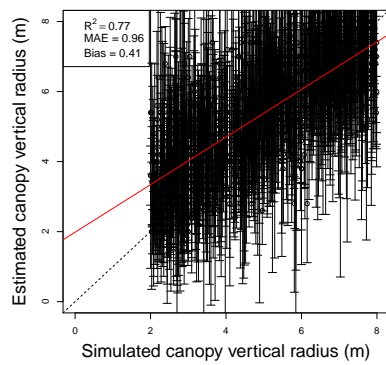
Parameter	Chi-Square			
	$n = 1$	$n = 10$	$n = 100$	
$R^2$	0.81	0.91	0.91	
$H_{top}$	MAE	1.66	1.30	1.43
	Bias (m)	0.54	0.69	0.94
$R^2$	0.70	0.77	0.79	
$F_c$	MAE	7.42	6.30	5.84
	Bias	2.01	2.03	2.15
$R^2$	0.70	0.77	0.79	
$E_z$	MAE	1.26	0.96	1.00
	Bias (m)	0.38	0.41	0.55
$R^2$	0.91	0.93	0.94	
$S_y$	MAE	1.44	1.23	1.11
	Bias (deg.)	0.01	-0.02	0.00



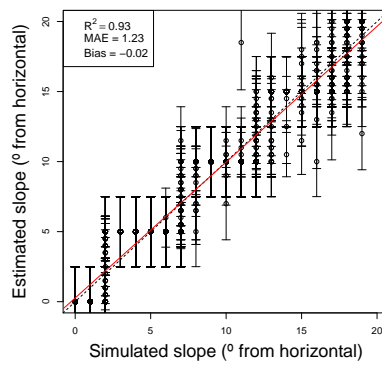
(a)



(b)



(c)



(d)

Figure 1: Chi-Square parameter estimates against FLIGHT model input parameters for simulated dataset with  $n = 10$ : a) Fractional cover, b) Maximum height, c) Canopy vertical radius, d) Slope. Circles represent the mean of possible set of size  $n$  solutions, and error bars represent the uncertainties related to the model inversion and are given by the standard deviation of the set of  $n$  possible solutions.

283 4.1.1. Response to Signal and Model Parameter Error

284 To investigate the effect of signal noise and error in assumed model parameters on the robustness of parameter  
 285 estimation, a subset of FLIGHT parameter values were modified individually, and in combination, and the resulting  
 286 simulated waveforms were compared against the LUT using the method described previously. Leaf and soil reflectance  
 287 parameter values were perturbed by  $\pm 10\%$ , and leaf diameter was set randomly to a value between 0.01–0.1 m. Wave-  
 288 forms simulated with combined leaf and soil noise perturbations were generated by varying randomly the reflectance  
 289 parameters between  $\pm 10\%$ . Two further LAD functions representing erectophile and planar foliage structures were  
 290 specified and simulated waveform data sets were modelled accordingly; all other parameters were fixed between the  
 291 three LAD types.  $R^2$ , MAE and bias for solution-set size  $n = 10$  are summarised in Tables 6 and 7.

292 As was expected, noise added to the leaf and soil reflectance FLIGHT parameters had a greater effect on the  
 293 estimation of  $F_c$  and  $E_z$  than on parameters concerning the vertical dimension e.g.  $H_{top}$  and  $S_y$ . In particular, negative  
 294 bias for  $F_c$  was found to occur when leaf reflectance was decreased or when soil reflectance was increased. Conversely,  
 295 bias moved in a positive direction when leaf reflectance was increased or when soil reflectance was decreased. Noise  
 296 from the soil reflectance perturbation had the greatest effect on the estimation of the parameters, particularly when  
 297 soil reflectance was increased. In this case,  $R^2$  was degraded for both  $F_c$  and  $H_{top}$ . Leaf diameter noise was found to  
 298 have minimal effect on forest parameter retrieval, due to the compensatory effect of the  $F_c$  and  $LAI$  parameters.

Table 6: Simulated: Chi-Square summary statistics of the simulated data set with added noise for leaf and soil reflectance and for leaf size, for solution size  $n = 10$ .

Parameter	Default	Noise					
		Leaf Spec. (-10%)	Leaf Spec. (+10%)	Soil Spec. (-10%)	Soil Spec. (+10%)	Leaf Dia. (0.01–0.1 m)	Combined
$R^2$	0.77	0.74	0.78	0.76	0.66	0.77	0.68
$E_z$ MAE	0.96	0.99	0.96	0.84	1.26	0.96	1.03
$E_z$ Bias (m)	0.41	0.37	0.49	0.13	0.87	0.42	0.51
$F_c$ $R^2$	0.77	0.74	0.78	0.76	0.66	0.77	0.68
$F_c$ MAE	6.30	6.52	7.16	10.45	8.75	6.34	7.64
$F_c$ Bias	2.03	-0.42	4.65	9.52	-5.23	1.94	0.47
$H_{top}$ $R^2$	0.91	0.89	0.91	0.92	0.81	0.91	0.88
$H_{top}$ MAE	1.30	1.38	1.30	1.11	2.08	1.29	1.49
$H_{top}$ Bias (m)	0.69	0.79	0.68	0.12	1.55	0.71	0.92
$S_y$ $R^2$	0.93	0.94	0.93	0.93	0.94	0.94	0.93
$S_y$ MAE	1.23	1.20	1.26	1.25	1.24	1.20	1.26
$S_y$ Bias (deg.)	-0.02	-0.19	0.21	-0.10	0.34	-0.03	0.10

Table 7: Simulated: Chi-Square summary statistics of the simulated data set for the three LAD classes, for solution sizes  $n = 10$ .

Parameter		Spherical (Default)	Erectophile	Planar
$H_{top}$	$R^2$	0.91	0.90	0.92
	MAE	1.30	1.39	1.15
	Bias (m)	0.69	0.84	0.41
$F_c$	$R^2$	0.77	0.72	0.80
	MAE	6.30	6.79	9.77
	Bias	2.03	-0.80	9.10
$E_z$	$R^2$	0.77	0.72	0.80
	MAE	0.96	1.02	0.88
	Bias (m)	0.41	0.52	0.02
$S_y$	$R^2$	0.93	0.94	0.93
	MAE	1.23	1.21	1.21
	Bias (deg.)	-0.02	0.00	0.07

## 299 4.2. Validation of GLAS Retrievals Over Forest Sites

300 The model inversion was validated using spatially consistent GLAS and airborne LiDAR data from the three  
301 forest sites. A  $\chi^2$  metric was applied to every canopy realisation within the LUT and sets of various sizes of possible  
302 solutions were then selected. Estimates for canopy maximum height ( $H_{top}$ ) and fractional cover ( $F_c$ ) parameters were  
303 compared for all sites, while slope was additionally compared for the Forest of Dean study site. These parameters  
304 were derived from the mean of the given set of possible solutions for each waveform. Associated uncertainties were  
305 indicated by the standard deviations of the solution sets. Where the uncertainty was found to be less than the LUT  
306 parameter increment, the LUT parameter increment was used instead as the minimum uncertainty.

307 Representative examples of waveform fitting over the simulated and three real forest datasets are shown in Figures  
308 2, 3, 4 and 5 and show a close agreement between the GLAS and simulated (LUT) waveforms. The typical bimodal  
309 waveform is apparent in most of the examples, however Figures 2b and 3c also show the effect of coincident vegetation  
310 and ground portions of the waveform due to the combination of topographic slope and low lying vegetation.

### 311 4.2.1. Forest of Dean

312 Retrieved fractional cover and height from GLAS for the Forest of Dean site are shown plotted against corre-  
313 sponding measurements from ALS in Figures 6a and 6b respectively, and Table 8 shows the Forest of Dean site  $R^2$ ,  
314 MAE and Bias for three values of  $n$ . Fractional cover is estimated with  $R^2$  of 0.52 and low MAE of approximately



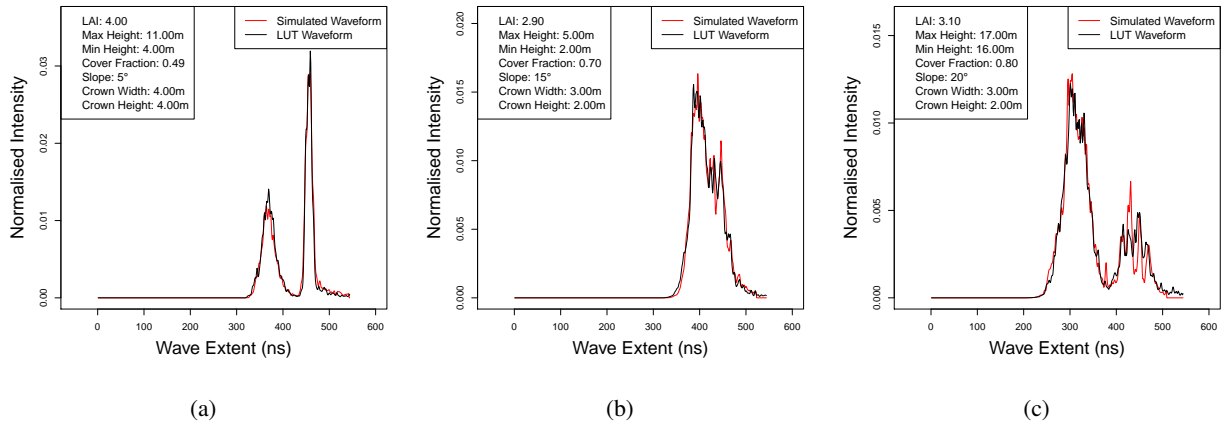


Figure 2: Simulated: Chi-Square metric waveform fit examples, showing best LUT fit against examples of simulated GLAS waveforms.

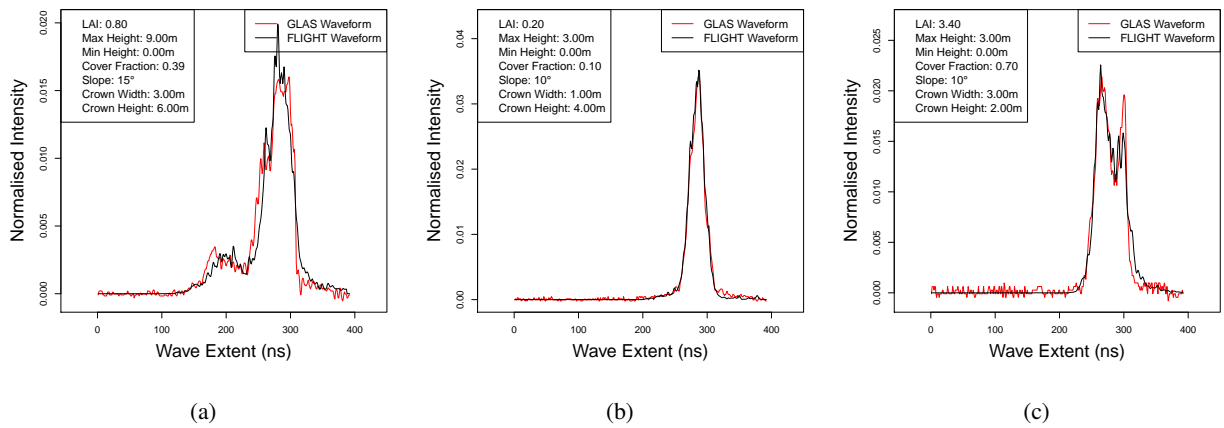


Figure 3: Forest of Dean: Chi-Square waveform fit examples, showing best LUT fit against Forest of Dean GLAS waveform examples.

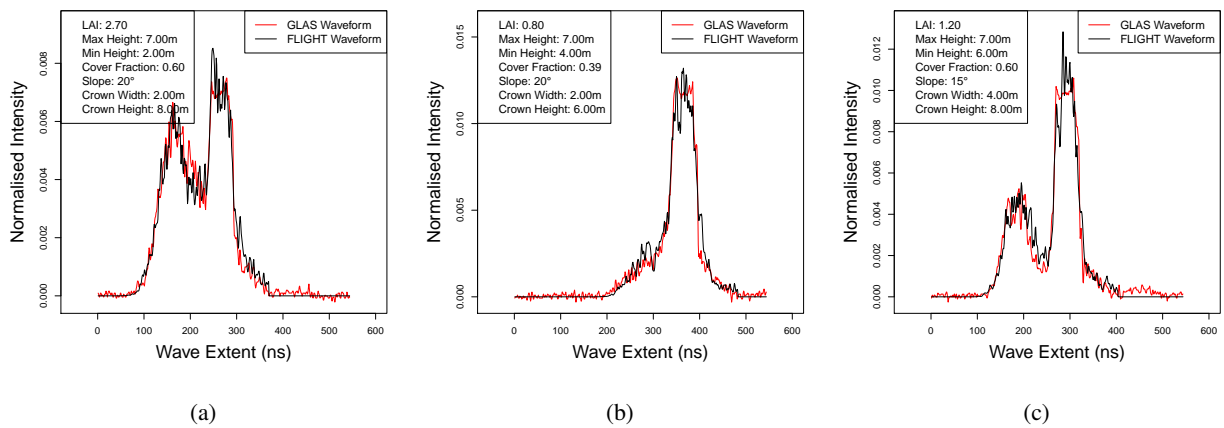


Figure 4: Southern Old Aspen: Chi-Square waveform fit examples, showing best LUT fit against Southern Old Aspen GLAS waveform examples.

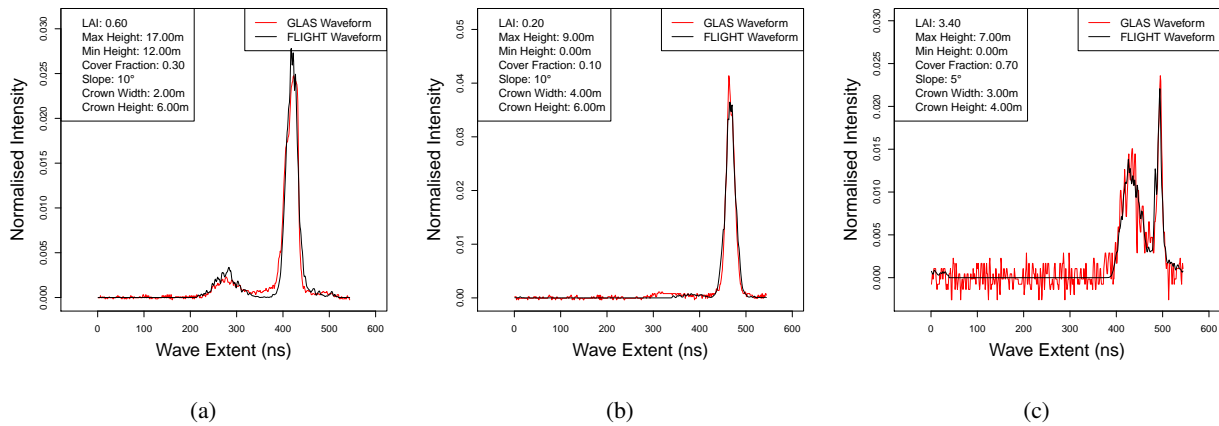


Figure 5: Norunda: Chi-Square waveform fit examples, showing best LUT fit against Norunda GLAS waveform examples.

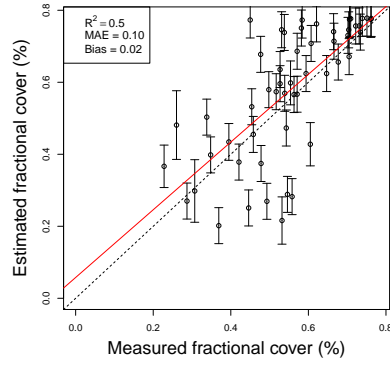
315 0.10. Height was estimated with a high coefficient of determination ( $R^2 = 0.74$ ) and low MAE of 3.71 m. The coefficients of determination give an indication of ability to distinguish within-site variability of height and fractional cover. 316 Both parameters display good adherence to the 1:1 line. The Forest of Dean ICESat/GLAS and airborne data sets 317 were acquired in closest temporal coincidence of the three datasets and the parameter regression results demonstrate 318 robust retrieval of height and vegetation cover in this case. Ground slope is estimated with good accuracy ( $MAE \leq 4^\circ$  319 degrees) but showing a positive bias of  $\approx 3.4^\circ$  degrees. 320

#### 321 4.2.2. Saskatchewan

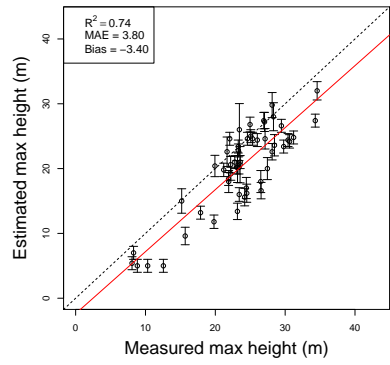
322 Canopy fractional cover and height jointly derived from GLAS footprints, compared with those from ALS for 323 the Southern Old Aspen study site are shown in figures 7a and 7b. It is important to note the model inversions 324 were performed on the available GLAS data, which were acquired during ‘leaf-off’ conditions (February), while 325 ALS fractional cover are made during a ‘leaf-on’ period (August). Quantitative comparison for fractional cover is 326 not appropriate therefore, other than to note the results show an expected lower value for leaf-off, and no significant 327 correlation. Since the conditions are very different to those assumed in the LUT (bare ground, ‘leaf-on’) this provides 328 a challenging test for model inversion for other structural parameters. It is interesting to note that canopy maximum 329 height derived from GLAS by model inversion was nevertheless estimated as close to the 1:1 line, with MAE of only 330 3.35m. The  $R^2$ , MAE and Bias for all solution-set sizes are summarised in Table 9.

#### 331 4.2.3. Norunda

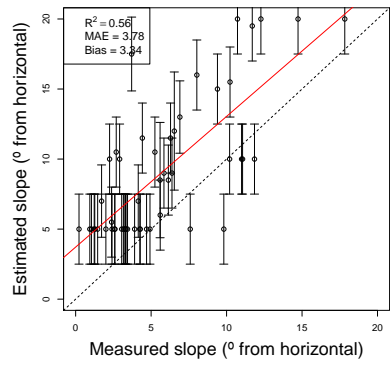
332 The final study site, Norunda, was subject to a considerable difference in time between the acquisition of the 333 GLAS data (2003) and the airborne LiDAR data (2011). Figure 8b shows most points have lower values in height 334 parameter retrieval from GLAS, compared to the later ALS data. These are likely due to growth occurring between 335 the two data set acquisition dates. Land cover differences through natural disturbance, growth or forestry activities



(a)



(b)



(c)

Figure 6: Forest of Dean: Chi-Square parameter estimates against airborne LiDAR derived parameters: a) Fractional cover, b) Maximum height, c) Slope. Circles represent the mean of possible set of size  $n$  solutions, and error bars represent the uncertainties related to the model inversion and are given by the standard deviation of the set of  $n$  possible solutions.

Table 8: Forest of Dean: Chi-Square summary statistics for solution sizes  $n = 1, 10, 100$ .

Parameter	Chi-Square		
	$n = 1$	$n = 10$	$n = 100$
$R^2$	0.71	0.74	0.70
$H_{top}$ MAE	4.00	3.80	3.71
Bias (m)	-3.53	-3.40	-3.26
$R^2$	0.51	0.50	0.52
$F_c$ MAE	0.10	0.10	0.10
Bias (m)	0.02	0.02	0.01
$R^2$	0.57	0.56	0.54
$S_y$ MAE	3.74	3.78	4.19
Bias (deg.)	3.29	3.34	3.87

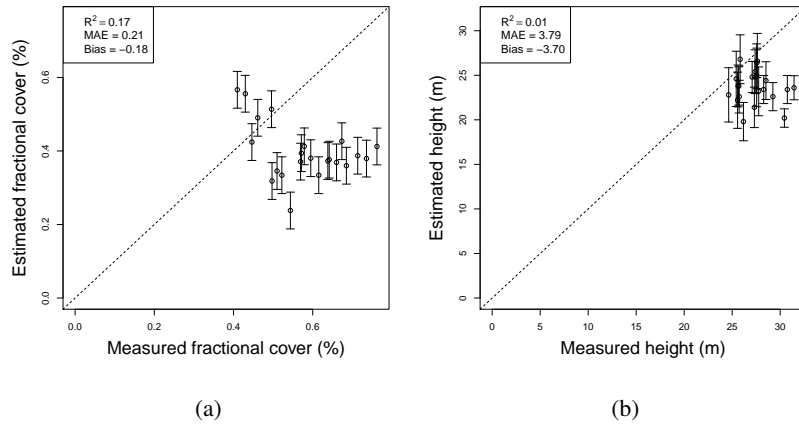


Figure 7: Southern Old Aspen: Chi-Square estimated parameters against airborne LiDAR derived parameters: a) Fractional cover, b) Maximum height. Circles represent the mean of possible set of size  $n$  solutions, and error bars represent the uncertainties related to the model inversion and are given by the standard deviation of the set of  $n$  possible solutions.

Table 9: Southern Old Aspen: Chi-Square summary statistics for solution sizes  $n = 1, 10, 100$ . Parameter  $S_y$  was left out of analysis as elevation change within the GLAS footprint was insignificant.

Parameter	Chi-Square			
	$n = 1$	$n = 10$	$n = 100$	
$R^2$	0.00	0.01	0.07	
$H_{top}$	MAE	4.36	3.97	3.35
	Bias (m)	-4.23	-3.70	-3.25
$R^2$	0.34	0.17	0.10	
$F_c$	MAE	0.22	0.21	0.20
	Bias	-0.19	-0.18	-0.18

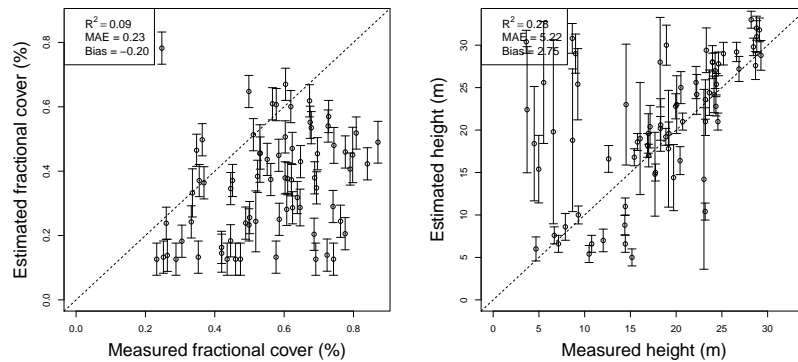
Table 10: Norunda: Chi-Square solutions summary statistics for solution sizes  $n = 1, 10, 100$ . Parameter  $S_y$  was left out of analysis as elevation change within the GLAS footprint was insignificant.

Parameter	Chi-Square			
	$n = 1$	$n = 10$	$n = 100$	
$R^2$	0.16	0.28	0.24	
$H_{top}$	MAE	6.00	5.22	5.13
	Bias	2.77	3.75	3.39
$R^2$	0.10	0.09	0.13	
$F_c$	MAE	0.23	0.23	0.24
	Bias	-0.20	-0.20	-0.22

336 such as clear felling and thinning also explain a number of overestimated outlier points for both height and fractional  
337 cover. As a result the MAE in height is somewhat higher for this comparison (5.13 m) than the first two examples.  
338 Fractional cover estimates show reasonable MAE (0.23), but low coefficient of determination, suggesting noise is high  
339 compared to within-site variability. Although making evaluation of retrieval accuracy more difficult, the large number  
340 of explained outlier points compared to other two sites, which did not experience significant growth or management,  
341 suggest the the method may be well suited to monitoring changes in height and vegetation cover over time. The  $R^2$ ,  
342 MAE and Bias for all solution-set sizes are summarised in Table 10.

## 343 5. Discussion

344 The inversion of the waveform LiDAR model using the LUT method provided estimates for the maximum canopy  
345 height for the Forest of Dean, Saskatchewan and Norunda sites. MAE was determined to be: 3.80 m, 3.35 m, 5.13  
346 m, respectively. ALS derived height estimate uncertainty bounds are well within those found using this method. An



(a) Fractional cover estimated using the weighted Chi-Square metric with  $n = 10$ . (b) Maximum height estimated using the weighted Chi-Square metric with  $n = 10$ .

Figure 8: Norunda: Chi-Square estimated parameters against airborne LiDAR derived parameters: a) Fractional cover, b) Maximum height. Circles represent the mean of possible set of size  $n$  solutions, and error bars represent the uncertainties related to the model inversion and are given by the standard deviation of the set of  $n$  possible solutions.

347 ability to detect the available within-site variability is shown by the  $R^2$  values of: 0.74, 0.07, 0.30, respectively.

348 Maximum height was best estimated at the Forest of Dean and Saskatchewan sites but degraded at the Norunda  
 349 site. This was likely due to the temporal difference between GLAS and ALS data sets, and forestry related activity  
 350 at this site. Using Swedish NFI data, the GLAS were filtered to only allow footprints located in stands that were at  
 351 or near maturity and had not been subject to forestry activities. The filtering resulted in only three remaining points  
 352 and so was not considered to be a robust sample. However, bias and MAE for height was found to be 0.92 m and  
 353 2.75 m, respectively — a clear improvement. Accuracy for maximum canopy height was surprisingly good at the  
 354 Saskatchewan site, considering the height retrieval was made using GLAS data acquired during ‘leaf-off’ conditions,  
 355 where a decrease in returned energy is likely to lower the estimated maximum canopy height (Wasser et al., 2013).

356 The most commonly used height metric to derive vegetation height from GLAS LiDAR data is waveform extent,  
 357 defined as the height difference between the first and last elevation at which the waveform energy exceeds a threshold,  
 358 usually set as 4.5 times background noise (Lefsky et al., 2005, 2007). Results using the method described in our study  
 359 compare well to those using the former method, presented by Los et al. (2012) and Rosette et al. (2009). Los et al.  
 360 (2012) also additionally employ a number of filters such that up to 75% of points were removed in tropical forest  
 361 study sites, and validating against aircraft derived height data to achieve  $r = 0.67$  and  $RMSE \approx 8$  m. Rosette et al.  
 362 (2009) use the same Forest of Dean GLAS and airborne LiDAR data as described in this study to obtain  $R^2 = 0.68$   
 363 and MAE = 4.4 m for maximum canopy height when using GLAS data products.

364 A number of the height overestimates were due to the tested metric fitting noise in a GLAS waveform to a compara-  
 365 bly sized vegetation peak in a FLIGHT waveform representing very low fractional cover or LAI. Alternative metrics  
 366 may increase the accuracy of the fitting of very low intensity portions of the GLAS waveform, improving vegetation

367 signal start and end point estimations. However height estimates generally agreed with field measurements acquired  
368 by Rosette et al. (2008b), with results close to the 1:1 line.

369 Fractional cover was comparably well estimated for the combined dominant cover classes Forest of Dean site, ( $R^2$   
370 = 0.50 and MAE = 0.10). Again, ALS derived uncertainty bounds are well inside those found using the presented  
371 method. For the Norunda site, the time difference between GLAS and airborne data acquisition dates prevented  
372 a more realistic parameter estimate from being obtained. When the data set was filtered, a total of three GLAS  
373 footprints remained. From these, MAE was determined to be 0.13. For the deciduous Southern Old Aspen site, the  
374 availability of only 'leaf-off' winter GLAS data meant that it was not possible to assess fractional cover estimates.

375 Slope beneath canopy was retrieved for the Forest of Dean site, where within-footprint elevation changes were  
376 significant, and found to have a  $R^2$  of 0.56 compared to airborne LiDAR measurements, but with a positive bias of  
377  $3.78^\circ$ ; this overestimate of slope would be expected to lead to an underestimate of canopy height equivalent to  $\approx$   
378 3–4 m to explain the same total waveform extent. This was tested over an inland water surface in Norunda, where  
379 the FLIGHT LiDAR return shows a narrower return peak than the GLAS waveform, requiring an equivalent slope  
380 of  $3\text{--}5^\circ$  to match. The reason for the widened GLAS ground peak in real waveform returns compared to modelled  
381 is unclear. A finer granularity slope parameter range may improve the slope estimation, where quantisation in the  
382 LUT leads to a 'binning' effect (see Figure 1d) but would not correct bias. A possible reason for the systematic slope  
383 mismatch could be due to small scale surface roughness detected by GLAS but not modelled in FLIGHT. A second  
384 potential explanation for the slope underestimate is due to an apparent small but systematic underestimate in modelled  
385 waveform temporal width which is based on published instrument parameters.

386 Choice of optimum solution set size  $n$  was not clear from the sites investigated and varied between parameter and  
387 site. It was observed that solution set medians remained relatively similar as  $n$  increased. However, variances about  
388 the means of the solution sets were found to increase as  $n$  increased. For this study, a value  $n = 10$  was chosen over  
389  $n = 1$  so that an indicator of solution uncertainty could be determined, while also minimising uncertainty around the  
390 estimated parameter. Furthermore, high values of  $n$  (e.g.  $n > 1000$ ) significantly impact the speed of the calculations.

391 In addition to uncertainties due to instrument and model errors, a significant source of error was attributed to  
392 the combination of returns from both vegetation and ground elevations, that occur due to the size of the illuminated  
393 footprint and as a function of ground slope (Harding and Carabajal, 2005). Ancillary topographic information (e.g.  
394 SRTM or ASTER DEM) may provide a means to preselect LUT waveforms to significantly increase the accuracy and  
395 efficiency of retrieval (Mahoney et al., 2014). Furthermore, where this LUT used fixed values for ground and canopy  
396 reflectance, a more comprehensive LUT implementation might vary these parameters and then use methods (Armston  
397 et al., 2013; Chen et al., 2014) to derive these reflectance parameters directly from the LiDAR waveform, again for  
398 the purpose of preselecting LUT waveforms.

399 A third source of error can be directly attributed to the LUT design. Inspection of the waveform fit plots revealed  
400 that original choice of canopy parameters in some cases was not sufficient to span the full range found in the study  
401 sites, in particular where a lower canopy stratum could result in confusion with a ground return. Koetz et al. (2007)

402 also report that the good performance of their model inversion was likely due to a two strata canopy simulation within  
403 their formulation. However the approach presented here allows flexible specification of structure, allowing a wider  
404 range of parameters or easily permitting more complex structures such as row-crop or two-strata canopy structures in  
405 a LUT.

## 406 **6. Conclusion**

407 This study has developed and evaluated a new method for parameter retrieval from satellite waveform LiDAR  
408 based on inversion of the three-dimensional FLIGHT radiative transfer model. A lookup table approach is developed  
409 allowing complex canopy optical properties and multi-scale structure, instrument laser emitted signal and its return  
410 detection, to provide a physically-based simultaneous retrieval of forest structural parameters, terrain slope and their  
411 uncertainty. A sensitivity study suggested potential accuracy of retrieval of forest height from GLAS data of  $\approx 1.5$  m,  
412 and fractional cover of 8%.

413 Testing using real GLAS waveforms over three forest sites demonstrated that the method for forest canopy param-  
414 eter retrieval from satellite waveform LiDAR was robust to cover type (Table 8). For the Forest of Dean site which  
415 had the nearest fitting GLAS and ALS coverage (Oct 2005 vs Oct 2006), three parameters were estimated to a high  
416 level of accuracy with height: MAE = 3.71 m;  $R^2 = 0.74$ , fractional cover: MAE = 0.10;  $R^2 = 0.50$  and ground slope:  
417 MAE = 3.78°;  $R^2 = 0.56$ . This showed improvement over previous retrieval for this site using the same data as input  
418 (Rosette et al., 2009). Other sites showed good height retrieval (MAE = 3.3–5.1 m) but lower  $R^2$  due in part to lower  
419 within-site variability compared to retrieval errors.

420 Results are in part dependent on the use of an appropriate LUT for the canopy being measured, although the canopy  
421 height retrieval appeared relatively robust to leaf-on/ leaf off conditions and snow vs bare ground. The method could  
422 include available ancillary information such as ground slope or vegetation type in order to optimise performance where  
423 these are known. The results suggest that the method used in this study is at least comparable to existing techniques and  
424 also offers the further advantage of being able to retrieve multiple parameters simultaneously, including sub-canopy  
425 terrain, and readily adaptable to future planned spaceborne LiDAR instruments (Dubayah et al., 2014; Montesano  
426 et al., 2015).

## 427 **7. Acknowledgements**

428 This research is funded by the NERC National Centre for Earth Observation (NCEO). ICESat/GLAS data were  
429 obtained from the National Snow and Ice Data Center (NSIDC), <http://nsidc.org>. The Forestry Commission Forest  
430 Research Agency is acknowledged for use of a subset of airborne LiDAR data for the Forest of Dean. Airborne LiDAR  
431 data from the Canadian sites were obtained with support from the Natural Environment Research Council (NERC)  
432 (Grant NE/G000360/1) and the Canadian Consortium for LiDAR Environment Applications Research (C-CLEAR).  
433 Airborne LiDAR data for Norunda was acquired with support from NERC/the Applied Geomatics Research Group



434 (AGRG)/FSF (Field Spectroscopy Facility) grant EU10-01 and 669 NERC/GEF (Geophysical Equipment Facility)  
435 grant 933.

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