

1 Flow and Transport in regions with Aquatic Vegetation

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9 Running Title: Flow near Aquatic Vegetation

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1 **Key Words:**

2 Aquatic Vegetation

3 Canopy

4 Canopy Shear-Layer

5 Monami

6 Turbulence

7 Turbulent Transport

8

9 **Key Terms/Definitions**

10 Emergent Vegetation = rooted vegetation that penetrates the free surface and thus occupies the

11 full water depth

12 Submerged Vegetation = rooted vegetation with a vertical extent less than the water depth

13 Canopy Shear Layer = the region of velocity shear generated by the drag discontinuity at top

14 of submerged canopy

15 Canopy-Scale Turbulence = vortices generated within canopy-shear-layer by Kelvin-Helmholtz

16 instability.

17 Stem-Scale Turbulence = turbulence generated in the wakes of individual stems and branches

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## 1 **Sidebar: Waves over Submerged Canopies**

2 Because the flow beneath waves is unsteady, inertial forces can be comparable to or larger than  
3 canopy drag at high wave frequencies, including typical wind-wave frequencies. For these  
4 conditions, the wave velocity is not significantly damped within the canopy, in contrast to the large  
5 degree of damping observed for dense canopies in uni-directional flow (Figure 3). Further, in  
6 analogy to viscous boundary streaming, canopy drag induces a non-zero wave stress, which in turn  
7 generates a mean mass-drift within the canopy. Steady currents with magnitudes up to 40% of the  
8 near-bed orbital velocity have been measured in model canopies.

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1 **Abstract:**

2 This paper describes mean and turbulent flow and mass transport in the presence of aquatic  
3 vegetation. Within emergent canopies, the turbulent length-scales are set by the stem diameter and  
4 spacing, and the mean flow is determined by the distribution of canopy frontal area. Sparse  
5 submerged canopies enhance bed roughness and near-bed turbulence, but the velocity profile  
6 remains logarithmic. For dense submerged canopies, the drag-discontinuity at the top of the canopy  
7 generates a shear-layer, which contains canopy-scale vortices that control the exchange of mass and  
8 momentum between the canopy and the overflow. The canopy-scale vortices penetrate a finite  
9 distance into the canopy,  $\delta_e$ , set by the canopy drag. This length-scale segregates the canopy into  
10 two regions: the upper canopy experiences energetic turbulent transport, controlled by canopy-scale  
11 vortices, while the lower canopy experiences diminished transport, associated with the smaller stem-  
12 scale turbulence. Flexible blades move in response to the canopy-scale vortices, called *monami*.



## 1 **Introduction**

2           Fresh- and saltwater vegetation provide a wide range of ecosystem services. Seagrasses are  
3 essential primary producers, forming the foundation for many food webs (Green & Short 2003).  
4 Seagrass meadows also damp waves, stabilize the seabed, shelter economically important fish, and  
5 enhance local water quality by filtering nutrients from the water. Based on nutrient cycling services  
6 alone, the global economic value of seagrass was estimated to be 3.8 trillion dollars per year by  
7 *Costanza et al.* (1997). Aquatic vegetation is also abundant in lowland rivers, where it provides  
8 habitat, alters light availability and temperature, and mediates concentrations of oxygen, carbon, and  
9 nutrients (Carpenter & Lodge 1986). Fresh- and saltwater wetlands provide habitat, improve water  
10 quality, and reduce coastal erosion (Mitsch & Gosselink 1986, Brampton 1992). Most of the  
11 services mentioned above are influenced by the flow within the vegetated regions.

12           The presence of vegetation alters the velocity field across several scales, ranging from  
13 individual branches and blades on a single plant, to the community of plants, called the meadow or  
14 canopy. The flow structure at the different scales is relevant to different processes. For example, the  
15 uptake of nutrients by an individual blade depends on the boundary layer on that blade, *i.e.* on the  
16 blade-scale flow (*e.g.* Koch 1994, Hurd 2000). Similarly, the capture of pollen is mediated by the  
17 flow structure generated around individual stigma (*e.g.* Ackerman 1997, 2000). In contrast, the  
18 flushing of larvae and pollen from a seagrass meadow or kelp forest depends on the flow structure at  
19 the canopy-scale (*e.g.* Jackson & Winant 1983, Gaylord et al. 2004).

20           Some aspects of canopy flow have been described in recent reviews. Monismith (2007)  
21 describes flow at branch- and canopy-scales in and around coral. Canopy-scale flow structure for  
22 terrestrial plant and urban canopies is described in Finnigan (2000) and Belcher (2012, this volume),  
23 and the mechanical interactions between wind and terrestrial plants are described by de Langre

1 (2008). To complement this rich literature, this review emphasizes conditions unique to aquatic  
 2 vegetation. Specifically, unlike terrestrial canopies, aquatic canopies can occupy all or a large  
 3 fraction of the flow depth, such that the dynamic impact of the canopy is felt over the entire flow  
 4 domain. This review will focus on fully developed flow structure over and through long canopies.  
 5 The adjustment of flow at the leading edge of a canopy is described in Belcher *et al.* (2003),  
 6 Rominger & Nepf (2011), and Belcher (2012, this volume).

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### 8 **Geometric scales and momentum balance -**

9 The canopy geometry is defined by the scale of individual stems and blades, and the number of these  
 10 elements per bed area. If the canopy elements have a characteristic diameter or width,  $d$ , and the  
 11 average spacing between elements is  $\Delta S$ , then the frontal area per canopy volume is  $a = d/\Delta S^2$ . In  
 12 terrestrial canopy literature, this is called the leaf area index (*e.g.* Kaimal & Finnegan 1994, p.79). A  
 13 non-dimensional measure of the canopy density is the frontal area per bed area,  $\lambda_f$ , known as the  
 14 roughness density (Wooding, Bradley & Marshall 1973). For canopy height  $h$ , and  $z = 0$  at the bed,

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$$16 \quad \lambda_f = \int_{z=0}^h a dz = ah, \quad (1)$$

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18 with the right-most expression valid for vertically uniform  $a$ . The canopy density can also be  
 19 described by the solid volume fraction occupied by the canopy elements,  $\phi$ . If the individual  
 20 elements approximate a circular cylinder, *e.g.* reed stems, then  $\phi \approx (\pi/4) ad$ . If the morphology is  
 21 strap-like, *e.g.* seagrasses, with blade width  $d$  and thickness  $b$ , then  $\phi = db/\Delta S^2 = ab$

22 Aquatic canopies exhibit a wide range of geometry. Marsh grasses are relatively sparse with

1  $d = 0.1$  cm to 1 cm,  $\phi = 0.001$  to 0.01,  $a = 0.01$  to  $0.07 \text{ cm}^{-1}$  (based on Valiela et al. 1978; Leonard &  
 2 Luther 1995, Lightbody & Nepf 2006). Mangroves are among the densest canopies, with  $\phi$  as high  
 3 as 0.45, mean trunk diameters of 4 to 9 cm, and  $a$  up to  $0.2 \text{ cm}^{-1}$  (Mazda et al. 1997; Furukawa et al.  
 4 1997). Seagrasses have  $a = 0.01$  to  $1 \text{ cm}^{-1}$ ,  $\phi = 0.01$  to 0.1 (Chandler et al. 1996, Luhar et al. 2010).  
 5 Emergent plants tend to have rounded stems for higher stiffness, and submerged grasses tend to have  
 6 a blade geometry in which the width (0.3 to 1 cm) is larger than the thickness ( $\approx 0.1$  cm), in which  
 7 case  $d$  is the blade width.

8           Within a canopy, flow is forced to move around each branch or blade, so that the velocity  
 9 field is spatially heterogeneous at the scale of these elements. A double-averaging method is used to  
 10 remove the element-scale spatial heterogeneity, in addition to the more common temporal averaging  
 11 (Gray & Lee 1977; Raupach & Shaw 1982, and references therein). Let the coordinates  $x$  and  $z$  be  
 12 parallel and normal to the local mean bed-slope, with  $z = 0$  at the bed and positive away from the  
 13 bed. The velocity vector  $\vec{u} = (u, v, w)$  corresponds to the coordinates  $(x, y, z)$ , respectively. The  
 14 instantaneous velocity and pressure ( $p$ ) fields are first decomposed into a time average (overbar) and  
 15 deviations from the time-average (single prime). The time-averaged quantities are further  
 16 decomposed into a spatial mean (angle bracket) and deviations from the spatial mean (double  
 17 prime). The spatial averaging volume is thin in the vertical, to preserve vertical variation in canopy  
 18 density, and large enough in the horizontal plane to include several stems ( $> \Delta S$ ).

19           Using the double-average method, the stream-wise momentum equation becomes

$$21 \quad \frac{D\langle \bar{u} \rangle}{Dt} = g \sin \theta - \frac{1}{\rho} \frac{\partial \langle \bar{p} \rangle}{\partial x} - \frac{\partial}{\partial z} \underbrace{\langle \overline{u' w'} \rangle}_{(i)} - \frac{\partial}{\partial z} \underbrace{\langle \overline{u'' w''} \rangle}_{(ii)} + \nu \frac{\partial^2 \langle \bar{u} \rangle}{\partial z^2} - D_x \quad (2)$$

(i)           (ii)           (iii)

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1 Here,  $\rho$  is the water density,  $\nu$  is the kinematic viscosity,  $\theta$  is the bed slope, and  $g$  is the gravitational  
 2 acceleration. Term (i) is the spatial-average of the Reynolds' stress. Term (ii), called the dispersive  
 3 stress, is the momentum flux associated with spatial correlations in the time-averaged velocity field.  
 4 Poggi et al. (2004b) have shown that the dispersive stress is less than 10% of the Reynolds stress (i)  
 5 for  $\lambda_f = ah > 0.1$ . Term (iii) is the viscous stress associated with the spatial variation in  $\langle \bar{u} \rangle$ . The  
 6 final term,  $D_x$ , is the spatially-averaged drag associated with the canopy elements, which is often  
 7 represented by a quadratic drag law (*e.g.* Kaimal & Finnegan 1994, p. 95).

$$8$$

$$9 \quad D_x = \frac{1}{2} \frac{C_D a}{1 - \phi} \langle \bar{u} \rangle \langle \bar{u} \rangle \quad (3)$$

10

11  $C_D$  is the canopy drag coefficient. Since the drag acts upon the fluid within the canopy, which  
 12 occupies only  $(1 - \phi)$  of the total volume, the drag is divided by the factor  $(1 - \phi)$ . The canopy-drag  
 13 length-scale,  $L_c$ , is defined from the quadratic drag law, *i.e.* based on dimensional reasoning  
 14  $D_x = \langle \bar{u} \rangle^2 / L_c$  (Belcher et al. 2003). From (3)

$$15$$

$$16 \quad L_c = \frac{2(1 - \phi)}{C_D a}. \quad (4)$$

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18 This represents the length-scale over which the mean and turbulent flow components adjust to  
 19 canopy drag. Since, most aquatic canopies have high porosity ( $\phi < 0.1$ ), this scale is commonly  
 20 approximated by  $(C_D a)^{-1}$ .

1           The drag coefficient,  $C_D$ , is affected by the canopy density,  $a$ , the element-Reynolds'  
 2 number,  $Re_d = \langle \bar{u} \rangle d / \nu$ , and the morphology of the individual canopy elements. A review of  $C_D$ 's  
 3 dependence on Reynolds' number and canopy density can be found in Tanino and Nepf (2008a) and  
 4 Nepf (2011). A linear drag law provides a better fit for rigid vegetation under low element Reynolds  
 5 number ( $Re_d < 50$ , Tanino et al. 2005). The Darcy-Forscheimer equation (e.g. Whitaker 1996) has  
 6 also been used to describe drag in wetlands (Oldham & Sturman 2001) and coral canopies (Lowe et  
 7 al. 2008). For flexible vegetation, the posture of the blade is affected by the flow speed, a  
 8 phenomenon called reconfiguration. As velocity increases, the blades are pushed over into more  
 9 streamlined positions, so that the drag force increases more slowly with increasing velocity than  
 10 predicted by the quadratic drag law. The impact of a changing plant shape on drag force has been  
 11 represented by altering the exponent in the drag law, while holding  $a$ , the frontal area, constant at the  
 12 undisturbed (no flow) value,  $a_o$ . Specifically, the square power in (3) is replaced with a variable  
 13 power  $2+E$ . The exponent  $E$  assumes values between 0 (rigid blade) and -2 (extremely flexible)  
 14 depending on the type of vegetation (see e.g. Vogel, Ch.6, 1994, Alben et al. 2002, O'Hare et al.  
 15 2007, Sand-Jensen 2008, Gosselin *et al.* 2010, Green 2005). In practice, it is difficult to characterize  
 16 the frontal area  $a$  for real plants, which has lead to contradictory results in the dependency of drag on  
 17 velocity (e.g. see discussion of Sand-Jensen 2003 by Sukhodolov 2005, Green 2005, Statzner et al.  
 18 2006).

19

## 20 **Emergent Canopies**

21           An emergent canopy fills the entire water depth,  $H$ , and typically penetrates through the  
 22 water surface. This type of canopy occurs in tidal marshes, kelp forests, and seagrass meadows  
 23 during periods of low tide. Emergent canopies impose structure on both the mean and turbulent flow

1 over the entire water column. The canopy dissipates eddies with scales greater than the stem-scales  
 2 of  $\Delta S$  and  $d$ , while contributing additional turbulent energy at these stem scales (Figure 1). As a  
 3 result, the dominant turbulent length-scale within a canopy is shifted downward from analogous  
 4 conditions without vegetation. In an open channel (no vegetation) eddies scale with the water depth,  
 5  $H$ . In a channel with rigid vegetation, the integral length-scale of the turbulence,  $\ell$ , is set by the  
 6 smaller of the stem diameter,  $d$ , or the average distance to the nearest neighboring stem,  $S_n$ ,  
 7 regardless of water depth (Tanino & Nepf 2008b). In a square array of stems the average spacing  
 8 and the average nearest neighbor spacing are the same,  $\Delta S = S_n$ , but in a random array,  $S_n < \Delta S$ . For  
 9  $d \leq S_n$ , turbulence is generated within stem wakes (if the Reynolds number is sufficient), so that  $\ell =$   
 10  $d$ . For  $d > S_n$ , turbulence is generated within the pore channels, so that  $\ell = S_n$ . These two regimes are  
 11 depicted in Figure 2a. Even for solid volume fractions as low as 0.6% ( $a = 0.01 \text{ cm}^{-1}$ ) the production  
 12 of turbulence by the canopy exceeds the production by bed shear over most of the flow depth (Nepf  
 13 *et al.* 1997, Burke & Stolzenbach 1983, Lopez & Garcia 1998). Therefore, turbulence level *cannot*  
 14 be predicted from the bed-friction velocity, as it is for open-channel flow. Instead, it is a function of  
 15 the canopy drag, as described below.

16 Vortex generation by stem wakes and/or in pore channels drains energy from the mean flow  
 17 (expressed as canopy drag) and feeds it into the turbulent kinetic energy. If this conversion is 100%  
 18 efficient, then the rate at which turbulent energy is produced,  $P_w$ , is equal to the rate at which mean  
 19 flow energy is extracted, *i.e.* the rate of work done by the flow against canopy drag (*e.g.* Raupach  
 20 and Shaw 1982).

$$22 \quad P_w = \frac{1}{2} C_D a \langle \bar{u} \rangle^3 \quad (5)$$

23

1 In fact, only the form drag is converted into turbulent kinetic energy. The viscous drag component is  
 2 immediately dissipated to heat. For stiff canopies, *i.e.* most emergent canopies, and  $Re_d > \approx 200$ , the  
 3 majority of the drag is form drag, and (5) is a reasonable approximation (Tanino & Nepf 2008 a, b).  
 4 In contrast, Nikora & Nikora (2007) suggest that for flexible canopies, which are typically  
 5 submerged, the drag is predominantly viscous, and (5) would be an overestimate of stem-scale  
 6 turbulence production. The relative contributions of viscous drag and form drag depend on the  
 7 morphology and alignment (streamlined vs. bluff) of the blades and stems within the canopy.

8 Within a homogenous emergent canopy, transport terms are negligible, and the wake  
 9 production (5) is balanced by viscous dissipation,  $\varepsilon$ , *i.e.*  $P_W = \varepsilon$ . In addition, for turbulence kinetic  
 10 energy,  $k$ , the dissipation rate within the canopy has the scale (Tennekes & Lumley 1972),

$$12 \quad \varepsilon \sim \langle \bar{k} \rangle^{3/2} \ell^{-1} \quad (6)$$

13  
 14 Equating (5) and (6), the turbulence intensity in the canopy is,

$$16 \quad \frac{\sqrt{\langle \bar{k} \rangle}}{\langle \bar{u} \rangle} \sim (C_D a \ell)^{1/3}. \quad (7)$$

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 18 As describe above, the turbulence length scale,  $\ell$ , is set by the smaller of the stem diameter,  $d$ , and  
 19 nearest-neighbor stem spacing,  $S_n$ . In a canopy of low solid volume fraction, or specifically  $S_n > d$ ,  
 20 the turbulence intensity increases rapidly with increasing canopy density (Figure 2b), because  $\ell = d$ ,  
 21 and thus  $a \ell \approx d^2/S_n^2$  in (7). In a canopy of high solid volume fraction,  $S_n < d$ , the turbulence intensity  
 22 increases more slowly, because  $\ell = S_n$ , and thus  $a \ell \approx d/S_n$  in (7).

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### Mean Velocity Profile

Within an emergent canopy, the momentum equation (2) will generally simplify to a balance between potential forcing (associated with hydrostatic pressure or bed slope) and canopy drag. First, viscous stress,  $\nu \partial^2 \langle \bar{u} \rangle / \partial z^2$ , is negligible compared to vegetative drag over most of the depth, excluding a thin layer near the bed of a scale comparable to the stem diameter,  $d$  (Nepf & Koch 1999). Second, as discussed above, the eddy length-scale is small compared to the water depth, which limits the turbulence flux of momentum, *i.e.* the turbulence stresses are typically negligible. For example, from numerical experiments the eddy scales are 1-3% of the water depth, and turbulent stresses are only 2% of the total drag for  $ah = 0.1$  (Burke & Stolzenbach 1983). Similar ratios have been measured in model emergent canopies (Nepf & Vivoni 2000). A notable exception occurs near the surface, as wind-generated stress can sometimes play a role in the momentum balance (Jenter & Duff 1999). Third, we assume that dispersive fluxes are negligible because the canopy density is commonly above the threshold  $ah > 0.1$  suggested by Poggi et al (2004b). For steady, uniform flow, the momentum equation then reduces to

$$g \left( \frac{\partial H}{\partial x} + \sin \theta \right) = - \frac{1}{2} \frac{C_D a}{1 - \phi} \langle \bar{u} \rangle \langle \bar{u} \rangle = - \frac{\langle \bar{u} \rangle \langle \bar{u} \rangle}{L_c}. \quad (8)$$

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The hydrostatic pressure and potential gradients that drive the flow (left-hand side) are not functions of the vertical coordinate,  $z$ . The right-hand side must then also be independent of  $z$ , so that the velocity varies inversely with the frontal area,  $a$ , and in proportion to the canopy-drag length scale,  $L_c$ . For plants with a distinct basal stem, this produces a velocity maximum close to the bed, because



1  $a$  is reduced below the level at which branching begins (Figure 1). A near-bed velocity maximum is  
 2 often observed in the marsh grass *Spartina alterniflora* (Leonard & Luther 1995, Leonard & Croft  
 3 2006). In contrast, the more vine-like *Atriplex portuloides* has leaves (and thus  $C_D a$ ) that are more  
 4 evenly distributed over depth, and the resulting velocity profile is uniform over depth (Leonard &  
 5 Reed 2002).

6 Equation 8 implies that the velocity profile within an emergent canopy has a self-similar  
 7 form. When the velocity is normalized by its value at an arbitrary reference depth, denoted by  
 8 subscript  $ref$ , the normalized profiles collapse together, regardless of the absolute magnitude of the  
 9 current. The shape of the normalized profile depends on the vertical distribution of  $L_c$ .

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$$11 \frac{\langle \bar{u} \rangle}{\langle \bar{u} \rangle_{ref}} = \sqrt{\frac{L_c}{L_{c-ref}}} \approx \sqrt{\frac{(C_D a)_{ref}}{C_D a}} \quad (9)$$

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13 The right-most approximation holds in most salt- and fresh-water wetlands canopies, for which the  
 14 canopy solid volume fraction is small ( $\phi < 0.1$ ), so that  $(1-\phi) \approx 1$ . A self-similar velocity structure  
 15 was confirmed by measurements in a coastal marsh (Lightbody & Nepf 2006) and in the freshwater  
 16 wetlands of the Everglades (Huang et al 2008). The normalization in (9) provides an important tool  
 17 for extrapolating a full velocity profile from records at a single vertical position.

18 An interesting non-linear behavior emerges when we compare flow conditions under  
 19 different canopy density, but the same potential and/or pressure gradient. To include the no canopy  
 20 limit, *i.e.* bare-bed, the bed resistance must be included in the momentum balance. Figure 2c and 2d  
 21 depict the change in velocity and turbulent kinetic energy, respectively, relative to bare-bed  
 22 conditions, with the later denoted by subscript  $b$ . The details of this comparison are given in Nepf

1 (1999). Because the vegetation offers additional resistance, the velocity within the canopy is always  
2 less than that over a bare bed, and the velocity ratio,  $\langle \bar{u} \rangle / u_b$ , decreases as the vegetation density  
3 increases (Figure 2c). Changes in turbulent kinetic energy with increasing vegetation density reflect  
4 the competing effects the reduced velocity and the additional turbulence production in stem wakes  
5 (7). These opposing tendencies produce a non-linear response in which the turbulence levels  
6 initially increase with increasing canopy density, but decrease as  $a$  increases further (Figure 2d).  
7 This non-linear response was predicted numerically for flow through emergent vegetation (Burke &  
8 Stolzenbach 1983) and within submerged roughness elements (Eckman 1990). It has been observed  
9 in flume studies of flow through real stems of *Zostera Marina* (Gambi *et al.* 1990). The enhanced  
10 turbulence levels in sparse canopies have important implications for canopy ecology. An increase in  
11 turbulence, particularly element-scale turbulence, could benefit vegetation by augmenting nutrient  
12 uptake and/or gas exchange (Anderson & Charters 1982), and similarly enhance uptake by microbes  
13 living on plant surfaces (*e.g.* Gantzer *et al.* 1991). Significant contributions to the turbulence  
14 intensity from stem-scale turbulence has also been observed in beds of channel macrophytes (Naden  
15 *et al.* 2006).

16         It is commonly expected that dense patches of vegetation, because they damp flow and  
17 turbulence, are associated with muddification, an increase in fine particles and organic content of the  
18 underlying sediment relative to adjacent bare bed conditions. Recently, van Katwijk *et al.* (2010)  
19 observed that sparse patches of vegetation are associated with sandification, a decrease in fine  
20 particles and organic matter, and they attribute this to higher levels of turbulence within the sparse  
21 patch, relative to adjacent bare regions. A transition from a tendency for sandification (elevated  
22 turbulence) to a tendency for muddification (diminished turbulence intensity) with increasing canopy  
23 density is consistent with the non-linear model shown in Figure 2d.

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### Submerged Canopies

The velocity within a submerged canopy has a range of behavior depending on the relative depth of submergence, defined as the ratio of flow depth,  $H$ , to canopy height,  $h$ . The flow within the canopy is driven by the turbulent stress at the top of the canopy as well as by the gradients of pressure and gravitational potential (bed slope). The relative importance of these driving forces varies with the depth of submergence (Nepf & Vivoni 2000).

$$\frac{\text{turbulent stress}}{\text{pressure gradient}} \sim \frac{H}{h} - 1 \tag{10}$$

Three classes of canopy flow can be defined from (10): deeply submerged or unconfined ( $H/h > 10$ ); shallow submergence ( $H/h < 5$ ); and emergent ( $H/h = 1$ ). A great deal is known about unconfined canopy flow based on work in terrestrial canopies (e.g. Raupach *et al.* 1996, Finnegan 2000, Belcher 2012). When unconfined, the flow within a canopy is driven by the turbulent stress at the top of the canopy, *i.e.* by the vertical turbulent transport of momentum from the overflow, with negligible contribution from pressure gradients. The terrestrial canopy model can be applied to aquatic canopies that are deeply submerged. However, due to the limitation of light penetration, most submerged aquatic canopies occur in the range of shallow submergence  $H/h < 5$  (e.g. Duarte 1991, Chambers and Kalff 1985), for which both turbulent stress and potential gradients are important in driving flow in the canopy. For emergent conditions ( $H/h = 1$ ) flow is driven by the potential gradients, as described in the previous section.

1 For a submerged canopy, there are two limits of behavior, depending on the relative  
 2 importance of the bed shear and the canopy drag. If canopy drag is small compared to bed drag,  
 3 then the velocity follows a turbulent boundary layer profile, with the vegetation contributing to the  
 4 bed roughness (Figure 3c, sparse canopy). If the canopy drag is large compared to the bed stress, the  
 5 discontinuity in drag that occurs at the top of the canopy ( $z = h$ ) generates a region of shear  
 6 resembling a free-shear-layer with an inflection point near the top of the canopy (Figure 3de, dense  
 7 canopy). From scaling arguments, Belcher et al (2003) predict that the transition between the sparse  
 8 and dense regimes occurs at the roughness density  $\lambda_f = ah = 0.1$ . Numerical simulations in Coceal &  
 9 Belcher (2004, Figure 4 of that paper) suggest that the transition occurs at  $L_c/h = 5$ , which  
 10 corresponded to  $\lambda_f = 0.15$ , for their parameter set ( $C_D = 2$ ,  $\phi = 0.25$ ). Based on measured velocity  
 11 profiles in aquatic systems (Nepf et al 2007, and references therein), the profile exhibits a boundary-  
 12 layer form with no inflection point if  $C_D ah < 0.04$ . A pronounced inflection point appears at the top  
 13 of the canopy for  $C_D ah > 0.1$ . Since  $C_D \approx 1$  in most of the studies considered, these limits are  
 14 consistent with the scaling and numerical estimates given above.

15 In this paper we focus on the dense canopy condition ( $ah > 0.1$ ). For these canopies,  
 16 Raupach et al (1996) demonstrated a similarity between canopy-shear-layers and free-shear-layers.  
 17 In a free-shear-layer the velocity profile contains an inflection point, which triggers a flow instability  
 18 that, in turn, leads to the generation of Kelvin-Helmoltz vortices (*e.g.* Brown & Roshko 1974,  
 19 Winant & Browand 1974). These structures dominate the transfer of momentum between the high-  
 20 speed and low-speed streams, and their size sets the length-scale of the shear-layer. For dense  
 21 submerged canopies ( $ah > 0.1$ ), the momentum absorption by the canopy is sufficient to produce an  
 22 inflection point in the velocity profile, which, as in free-shear-layers, leads to the generation of K-H  
 23 vortices (Figure 3de). These vortices are called canopy-scale turbulence, to distinguish it from the

1 much-larger boundary-layer turbulence, which may form above a deeply submerged or unconfined  
 2 canopy, and the much smaller stem-scale turbulence.

3 Over a deeply submerged (or terrestrial) canopy ( $H/h > 10$ ), the canopy-scale vortices are  
 4 highly three-dimensional due to their interaction with larger boundary-layer turbulence, which  
 5 stretches the canopy-scale vortices, enhancing secondary instabilities (Fitzmaurice et al. 2004,  
 6 Finningan et al 2009). However, with shallow submergence ( $H/h \leq 5$ ), which is common in aquatic  
 7 systems, larger-scale boundary-layer turbulence is not present, and the canopy-scale vortices  
 8 dominate the turbulence field, both within and above the canopy (Ghisalberti & Nepf 2005, 2009).  
 9 For shallow submergence the canopy-scale turbulence is also more coherent (less three-dimensional)  
 10 than that observed with deeply submerged (or terrestrial) conditions. However, in both cases the  
 11 canopy-scale vortices dominate the vertical transport at the canopy interface (e.g. Gao et al. 1989,  
 12 Finnigan 2000, Ghisalberti & Nepf 2002).

13 In a free-shear-layer, the vortices grow continually downstream, predominantly through  
 14 vortex pairing (Winant & Browand 1974). In canopy-shear-layers, however, the vortices reach a  
 15 fixed scale and a fixed penetration into the canopy ( $\delta_e$  in Figure 3de) at a short distance from the  
 16 canopy's leading edge (Ghisalberti & Nepf 2004). Based on measurements with a flexible model of  
 17 the seagrass *Zostera marina* ( $a = 5.7 \text{ m}^{-1}$ ), a fixed shear-layer scale is reached at a distance of  $10h$   
 18 from the leading edge of the meadow (Ghisalberti 2000). The fixed vortex and shear-layer scale is  
 19 reached when the shear-production that feeds energy into the canopy-scale vortices is balanced by  
 20 dissipation by canopy drag. This energy balance predicts the following length-scale, which has been  
 21 verified with laboratory observations (Nepf et al. 2007).

$$23 \quad \delta_e = \frac{0.23 \pm 0.6}{C_D a} \quad (11)$$

1  
 2 Recall that  $C_{Dah} \geq 0.1$  is required to produce shear-layer vortices, so that (11) applies only to those  
 3 canopies. In the range  $C_{Dah} = 0.1$  to 0.23, the shear-layer vortices penetrate to the bed,  $\delta_e = h$ ,  
 4 creating a highly turbulent condition over the entire canopy height (Figure 3d). At higher values of  
 5  $C_{Dah}$  the canopy-scale vortices do not penetrate to the bed,  $\delta_e < h$  (Figure 3e).

6 The scaling  $\delta_e \sim a^{-1}$  has been observed in flows near porous layers over a wide range of  
 7 physical scales, spanning from granular beds to terrestrial forests and urban canopies (Ghisalberti,  
 8 2009). However, the scale relation must break down when  $(C_{Da})^{-1}$  approaches the scale of the  
 9 canopy elements,  $d$ , because  $a$  is only defined as an average over multiple elements. For rigid  
 10 cylinders, when  $(C_{Da})^{-1}$  is less than  $2d$ , the penetration scale transitions to a constant  $\delta_e \approx 2d$  (White  
 11 & Nepf 2007). The depth of submergence,  $H/h$ , can also affect the penetration length-scale. For  $H/h$   
 12  $< 2$ ,  $\delta_e$  is diminished from (11), as interaction with the water surface diminishes the strength and  
 13 scale of the vortices (Nepf & Vivoni 2000, Okamoto & Nezu 2009).

14 The penetration length,  $\delta_e$ , segregates the canopy into an upper layer of strong turbulence and  
 15 rapid renewal and a lower layer of weak turbulence and slow renewal (Nepf & Vivoni 2000).  
 16 Flushing of the upper canopy is enhanced by the canopy-scale vortices that penetrate this region  
 17 (Figure 3e). In contrast, turbulence in the lower canopy ( $z < h - \delta_e$ ) is generated in stem wakes and has  
 18 significantly smaller scale, set by the stem diameters and spacing. Canopies for which  $\delta_e/h < 1$   
 19 (Figure 3e) shield the bed from strong turbulence and turbulent stress. Because turbulence near the  
 20 bed plays a role in resuspension, these dense canopies are expected to reduce resuspension and trap  
 21 sediment. Consistent with this, Moore (2004) observed that resuspension within a seagrass meadow  
 22 was reduced, relative to bare-bed conditions, only when the above ground biomass per unit area was  
 23 greater than  $100 \text{ g/m}^2$  (dry mass). This biomass corresponds to  $ah = 0.4$  (Luhar et al. 2008). Using

1  $C_D \approx 1$ , this canopy density is consistent with the transition implied by (11). Note that the transition  
2 in near-bed turbulence and resuspension does not occur abruptly at  $C_{Dah} = 0.23$ , but gradually with  
3 increasing  $C_{Dah}$  above this value, as the canopy-scale vortices are progressively pushed further from  
4 the bed. Because of the reduced near-bed turbulence, dense canopies can promote sediment  
5 retention. In sandy regions, that tend to be nutrient poor, the preferential retention of fines and  
6 organic material, *i.e.* muddification, enhances the supply of nutrient to the canopy, so that dense  
7 canopies provide a positive feedback to canopy health in sandy regions. In contrast, in regions with  
8 muddy substrate, which is more susceptible to anoxia, sparse meadows ( $C_{Dah} \leq 0.23$ ) may be more  
9 successful, because the enhanced near-bed turbulence removes fines, leading to a sandier substrate  
10 that is less prone to anoxia.

11

### 12 *Flexible Canopies and Monami*

13 Under some conditions, the canopy-scale vortices produce sufficient instantaneous drag to  
14 overcome the buoyancy and rigidity of individual blades. The passage of the travelling vortices then  
15 causes a local depression in the canopy, which travels along the canopy interface, in synch with the  
16 travelling vortices (Figure 4a). This progressive waving of canopy blades is called *monami*  
17 (Ackerman & Okubo 1993). It has been observed to occur extensively in the field (*e.g.* Fonseca &  
18 Kenworthy 1987, Ackerman & Okubo 1993, Grizzle *et al.* 1996). The frequency of the *monami*  
19 matches the frequency of vortex passage, which is given by instability theory (Ikeda & Kanazawa  
20 1996, Ghisalberti & Nepf 2002). However, if the instantaneous drag associated with the canopy-  
21 scale vortices is not sufficient to depress individual blades, the *monami* will not occur, even though  
22 the canopy-scale vortices are present.

23 To understand the connection between the canopy-shear-layer vortices and the *monami*, it is

1 useful to consider the differences between the free-shear-layer and canopy-shear-layer. Free-shear-  
 2 layer vortices are symmetric around the inflection point ( $z_i$ ), and their translation speed,  $U_v$ , matches  
 3 the velocity at the inflection point,  $U_i$ . Because these vortices rotate faster than they translate, the  
 4 lower region of the layer experiences a negative velocity perturbation as a vortex passes (*e.g.*  
 5 Dimotakis *et al.* 1981, Ho *et al.* 1991). In a canopy-shear-layer the inflection point corresponds with  
 6 the top of the canopy ( $z_i \approx h$ ), so that the velocity at the inflection point is  $U_i = U_h = \langle \bar{u} \rangle_h$ .  
 7 However, due to the canopy drag, the vortices are displaced upward, relative to the inflection point.  
 8 As a result, the translation speed of the vortex is higher than the velocity at the inflection point, *i.e.*  
 9  $U_v > U_i = U_h$  (Ikeda and Kanazawa 1996). The velocity ratio  $U_v/U_h$  increases with increasing depth  
 10 of submergence ( $H/h$ ), up to  $U_v/U_h = 1.8$  observed at  $H/h = 4.5$  (Ghisalberti & Nepf 2002). In  
 11 terrestrial canopies  $U_v/U_h$  is also 1.8 (Finnigan 1979), suggesting that this is the asymptotic value for  
 12 unconfined canopies. Further, the canopy drag causes the vortices to rotate more slowly than  
 13 vortices formed in a free-shear-layer of comparable shear-strength. The translation speed of the  
 14 vortex is sufficiently large compared to its rotation that as the front of the vortex passes a strong  
 15 sweep ( $u > 0$ ,  $w < 0$ ) invades the canopy (Ghisalberti & Nepf 2002). The monami is generated as the  
 16 sweep deflects the canopy forward and downward. The connection between the velocity field and  
 17 the plant motion is described in Ghisalberti & Nepf (2006) and Okamoto & Nezu (2009).

18         The flexibility of the canopy and the presence of *monami* affect the turbulent exchange  
 19 between the canopy and the overflow. This can be seen in the profiles of Reynolds' stress,  
 20 normalized by the square of the velocity difference ( $\Delta U$ ) between the canopy and overflow, which is  
 21 a measure of momentum exchange efficiency. The two profiles shown in Figure 4b are measured  
 22 with the same flexible canopy ( $a \approx 0.052 \text{ cm}^{-1}$ , and  $ah = 1$  when erect, described in Ghisalberti &  
 23 Nepf 2005). The vertical axis is dimensional to emphasize the vertical shift associated with the



1 greater deflection of the canopy under the higher flow condition. In the weaker flow case ( $U_h = 1.7$   
 2  $\text{cms}^{-1}$ , orange symbols) canopy-scale vortices are produced, but are too weak to deflect the blades,  
 3 and no *monami* occurs. In the stronger flow case ( $U_h = 7.9 \text{ cms}^{-1}$ , green), the canopy deflection is  
 4 larger (smaller  $h$ ), and the canopy-scale vortices are strong enough to trigger *monami*. The *monami*  
 5 excursion amplitude is noted in the figure. The combination of deflection and *monami* allows the  
 6 turbulent flux to penetrate closer to the bed, which leads to greater in-canopy flow speed (see also  
 7 Ghisalberti & Nepf 2009).

8 While *monami* allows for a deeper penetration of stress, the momentum transfer is less  
 9 efficient. For example, the maximum normalized stress is  $\langle \overline{u'w'} \rangle / (\Delta U)^2 = 0.013$  for the stationary  
 10 canopy (orange, w/o *monami*) but only 0.008 with *monami* is present (green, Figure 4b). A rigid  
 11 canopy produces even more efficient exchange, with a peak normalized-stress of 0.017 (Ghisalberti  
 12 & Nepf 2005). The diminished exchange efficiency occurs because the vortices are smaller and  
 13 weaker in the presence of *monami*, and also weaker above a flexible canopy compared to a rigid  
 14 canopy of similar geometry (see detailed discussion in Ghisalberti & Nepf 2006).

15

### 16 *Mean Velocity Profile*

17 Sufficiently far above a submerged canopy ( $z > 2h$ ), the velocity profile is logarithmic (*see* Kaimal  
 18 & Finnigan 1994, and reference therein).

19

$$20 \quad \langle \bar{u} \rangle = \frac{u_*}{\kappa} \ln \left( \frac{z - z_m}{z_o} \right) \quad (12)$$

21

1 with  $\kappa = 0.4$  (von Karman constant). The horizontal-average (angled bracket) is not strictly needed  
 2 above the canopy, but is retained for consistency with the equations within the canopy. The friction  
 3 velocity,  $u_*$ , is related to the Reynolds' stress at the top of the canopy,  $u_*^2 = \langle \overline{u'w'} \rangle_h$ . The  
 4 parameters  $z_m$  and  $z_o$  are the displacement and roughness heights, respectively, both of which depend  
 5 on the canopy roughness density,  $ah$ . Based on studies with both model and real vegetation, a  
 6 simple estimate for friction velocity is  $u_* = (gS(H - h))^{0.5}$ , with  $S = \partial H / \partial x + \sin \theta$  (Murphy *et al.* 2007).  
 7 If the vegetation is flexible, then  $h$  is the mean deflected height of the canopy (Jarvela 2005).  
 8 However, if the depth of submergence is small, compared to the displacement height, the following  
 9 estimator is more accurate,  $u_* = (gS(H - z_m))^{0.5}$  (Nepf & Vivoni 2000).

10 Recall that the penetration length-scale,  $\delta_e$ , describes the distance over which turbulent stress  
 11 penetrates the canopy from above. Similarly, the displacement height is the centroid of momentum  
 12 penetration into the canopy (Thom 1971). This similarity suggests the physically intuitive scaling,  
 13

$$14 \quad \frac{z_m}{h} \approx 1 - \frac{1}{2} \frac{\delta_e}{h} = 1 - \frac{0.1}{C_D ah}, \quad (13)$$

15  
 16 which has been confirmed for  $ah \approx 0.2$  to 3 (Luhar *et al.* 2008). For  $ah \gg 1$ , the displacement  
 17 thickness tends towards  $z_m \approx h$ , indicating that essentially the entire canopy is cut-off from the  
 18 overflow. In addition,  $z_m$  goes to zero at  $ah = 0.1$ . When  $z_m = 0$ , the velocity profile has no inflection  
 19 point (Figure 3c), consistent with the observation  $ah > 0.1$  is required to produce an inflection point  
 20 in measured velocity profiles (Figure 3de).

21 The dependency of the roughness height,  $z_o$ , on canopy density,  $ah$ , differs significantly  
 22 above and below the threshold of  $ah = 0.1$  (*e.g.* Raupach *et al.* 1980, MacDonald *et al.* 1998,

1 Jimenez 2004, Luhar *et al.* 2008). In the sparse canopy range ( $ah < 0.1$ ), the roughness height  
 2 increases with increasing  $ah$ . In sparse canopies the flow penetrates the full canopy, so that  $z_o$  is  
 3 proportional to the drag imparted by the full canopy,  $C_D ah$ , *i.e.*  $z_o/h \sim C_D ah$ . In contrast, for dense  
 4 canopies ( $ah > 0.1$ ), the roughness height decreases with increasing  $ah$ . The effective height of the  
 5 canopy, as seen by the overflow, is the penetration scale,  $\delta_e$ . The roughness height depends on this  
 6 effective height, rather than the canopy height, so that  $z_o \sim \delta_e \sim a^{-1}$ . For example, data summarized in  
 7 Luhar et al (2008) suggest that for  $ah > 0.1$ ,  $z_o = (0.04 \pm 0.02) a^{-1}$ .

8 The logarithmic profile form is based on equilibrium turbulence, such that dissipation and  
 9 production are locally in balance (*e.g.* Tennekes & Lumley 1990). Largely because of the vertical  
 10 transport provided by the shear-layer structures, this condition is not met for some distance above the  
 11 canopy, called the roughness sub-layer. For very shallow submergence,  $H/h \leq 1.5$ , the roughness  
 12 sub-layer extends to the surface, and a logarithmic structure is not observed above the canopy.

13 The flow within a submerged canopy is driven by a combination of the turbulent, dispersive  
 14 and viscous (usually negligible) stresses generated by the overflow, as well as the potential gradient  
 15 associated with the hydrostatic pressure gradient and the bed slope. Below the penetration of  
 16 turbulent and dispersive stress ( $z < h - \delta_e$ ), conservation of linear momentum reduces to a balance  
 17 between potential gradients and the sum of the canopy and the bed drag. Assuming that the canopy  
 18 drag is much larger than bed drag, this balance yields the following mean velocity.

19

$$20 \quad \langle \bar{u} \rangle = U_1 = \sqrt{\frac{2g(\partial H / \partial x + \sin \theta)}{C_D a}} \quad (14)$$

21

22 This is the same momentum balance observed for emergent canopies. So, again, if the canopy

1 density,  $a$ , or drag coefficient  $C_D$  are functions of  $z$ , the velocity will vary inversely, *i.e.* velocity will  
 2 be highest where  $C_D a$  is lowest.

3 In the upper canopy ( $h - \delta_e < z < h$ ) flow is driven by both potential gradients and turbulent  
 4 stress. The stress-driven component is derived by simplifying the moment equation (2) to a balance  
 5 of canopy drag and turbulent stress, and modeling the turbulent stress with a mixing length model,

6  $\langle u'w' \rangle = \ell_m^2 (\partial \langle \bar{u} \rangle / \partial z)^2$  (*e.g.* Inoue 1963, Cionco 1965). This yields the exponential velocity

7 profile observed in terrestrial canopies. In aquatic canopies, the potential-driven component is also  
 8 important in the upper canopy. Combining the stress-driven and potential-driven components, the  
 9 upper canopy velocity profile is,

10

$$11 \quad \langle \bar{u} \rangle = U_1 + (U_h - U_1) \exp(-K_u(h - z)), \quad (15)$$

12

13 with  $U_h = \langle \bar{u} \rangle$  at the top of the canopy, and constant  $K_u = \beta / \ell_m$ , with  $\beta = u_* / U_h$ . It is physically-

14 intuitive that the mixing length should be related to the penetration of shear-layer vortices into the

15 canopy, *i.e.*  $\ell_m \sim \delta_e \sim (C_D a)^{-1}$ . Harmon and Finnigan (2007) suggest  $\ell_m = 2\beta^3 (C_D a)^{-1}$ , or  $K_u =$

16  $C_D a / (2\beta^2)$ . For rigid canopies in water,  $\beta = 0.24 \pm 0.02$  (S.E., data in Ghisalberti & Nepf 2005),

17 which predicts  $K_u = (8.7 \pm 1.4) C_D a$ . This predicted value agrees with the observed decay scale

18 constant,  $K_u = (9 \pm 2) C_D a$ , extracted from measured velocity profiles in Ghisalberti (2005). In the

19 dense canopy limit,  $\beta$  has no dependence on canopy density (Ghisalberti & Nepf 2005), but it

20 declines as the transition to the sparse canopy limit ( $ah < 0.1$ ) is approached, *i.e.* as the canopy-scale

21 vortices diminish and eventually disappear (Poggi et al 2004a). Flexible canopies display a lower

22 value,  $\beta = 0.17 \pm 0.01$  (Ghisalberti & Nepf 2005), consistent with the less efficient momentum

23 transfer noted in Figure 4. Belcher et al (2003) propose the alternative  $K_u = (2l_m^2 L_c)^{-1/3}$ , with the

1 approximation  $l_m \sim h$ . However, the mixing length within the canopy may be better represented by the  
 2 vortex penetration, *i.e.*  $l_m \sim L_c \sim (C_D a)^{-1}$ , which then also yields  $K_u \sim L_c^{-1} \sim C_D a$ .

3 To model the full velocity profile, *i.e.* both within and above the bed, researchers have  
 4 combined the models for above-canopy and in-canopy profiles by matching the velocity at the top of  
 5 the canopy (*e.g.* Abdelrhman 2003, Carollo *et al.* 2002). While this ignores the roughness sub-layer,  
 6 for practical purposes the resulting profile is reasonably accurate. First, the velocity profile above  
 7 the meadow ( $z > h$ ) is estimated from the logarithmic profile (12). The logarithmic profile provides  
 8 the velocity at the top of the meadow,  $U_h$ , which is used with (14) and (15) to predict the velocity  
 9 within the meadows ( $z < h$ ). An example is given in Figure 5 using data from Ghisalberti (2005).  
 10 The input parameters are the water depth ( $H = 46.7$  cm), the meadow height ( $h = 13.9$  cm), the  
 11 surface slope ( $S = 2.5 \times 10^{-5}$ ), the canopy density ( $a = 0.034$  cm<sup>-1</sup>), and the measured drag  
 12 coefficient,  $C_D = 0.77$ . The measured and predicted profiles agree within uncertainty, except  
 13 approaching the free-surface, where the measured profile tends toward  $\partial u / \partial z = 0$  to meet the no-  
 14 stress condition at the surface that is not represented in the log-profile. Other models for the  
 15 complete velocity profile in regions with submerged aquatic vegetation have utilized different  
 16 turbulence closure schemes (*e.g.* Shimizu & Tsujimoto 1994, Lopez & Garcia 2001, Poggi *et al.*  
 17 2004a, Defina & Bixio 2005), and some reflect the bending response of flexible vegetation (*e.g.*  
 18 Abdelrhman 2007, Dijkstra & Uittenbogaard 2010)

19

## 20 **Mass Transport in Vegetated Flow**

21 Conservation of mass is described by the transport equation,

22

$$23 \quad \frac{\partial C}{\partial t} + \vec{u} \cdot \nabla C = D_m \nabla^2 C, \quad (16)$$

1  
 2 with  $D_m$  the molecular diffusion. Applying the double-average method described above, and  
 3 assuming there are no sources or sinks, this becomes,

$$5 \quad \frac{\partial \langle \bar{C} \rangle}{\partial t} + \langle \bar{u}_j \rangle \frac{\partial \langle \bar{C} \rangle}{\partial x_j} = - \frac{1}{(1-\phi)} \frac{\partial}{\partial x_j} (1-\phi) \left\{ \langle \bar{u}_j' C' \rangle + \langle \bar{u}_j'' \bar{C}'' \rangle - D_m \left\langle \frac{\partial C}{\partial x_j} \right\rangle \right\}, \quad (17)$$

6  
 7 with  $(x, y, z) = (x_1, x_2, x_3)$ . The first term on the right-hand side represents dispersion associated with  
 8 turbulent fluctuations, *i.e.* turbulent diffusion. The second term on the right represents dispersion  
 9 associated with spatial-heterogeneity in the time-mean velocity field, *e.g.* the dispersion associated  
 10 with flow path tortuosity. The last term is flux due to molecular diffusion, which in general is  
 11 negligible compared to the first two. Laboratory measurements in rigid canopies indicate that, over  
 12 time-scales greater than turbulent time-scales, and spatial-scales much greater  $\Delta S$  and  $d$ , these three  
 13 terms produce Fickian transport, *i.e.* the right hand-side reduces to  $D_j (\partial^2 \langle \bar{C} \rangle / \partial x_j^2)$ , with dispersion  
 14 coefficient  $D_j$  (White & Nepf 2003, Tanino & Nepf 2008b).

### 16 *Turbulent Diffusion and Mechanical Dispersion in an Emergent Canopy*

17 For solid volume fraction  $\phi < 0.1$ , turbulent diffusion is the dominant component of  $D$  within the  
 18 canopy (Tanino & Nepf 2008b). The velocity scale controlling turbulent diffusion is the mean  
 19 velocity,  $U_I$ , given by (8) and (14). As discussed above, the turbulence length scale may be set by  
 20 the stem scale (if  $d \leq S_n$ ), or by the stem spacing  $S_n$ , for  $d > S_n$  (Figure 2a). Experimental studies  
 21 confirm  $D \sim U_I d$  for  $\phi \ll 0.1$ , and support the simple scaling,

22

$$1 \quad D = 0.2 U_1 d \quad (18)$$

2  
 3 (Lightbody & Nepf 2006, Tanino & Nepf 2008b). For denser canopies, specifically when  $S_n < d$ , the  
 4 contribution to  $D$  from turbulent diffusion declines rapidly, as the length-scale of turbulence declines  
 5 (Figure 2a). For  $\phi > \approx 0.1$ , the dispersion due to the spatial-heterogeneity in the velocity field (also  
 6 called mechanical dispersion) becomes important, and it dominates for  $\phi > 0.15$ . In addition, in the  
 7 absence of turbulence, *e.g.*  $Re_d < 100$ , mechanical dispersion is the main contributor to dispersion  
 8 across all stem densities. The following formulation is consistent with data across all stem densities  
 9 for  $Re_d < 100$ , and for  $\phi > 0.15$  for all Reynolds number (Nepf et al. 1997, Serra et al. 2004, Nepf  
 10 2004, Tanino & Nepf 2008b),

$$12 \quad \frac{D}{U_1 d} = ad \approx \phi \quad (19)$$

13  
 14 Tanino & Nepf (2008b) describe a more comprehensive model that smoothly spans the two regimes  
 15 described by (18) and (19).

16  
 17 *Turbulent Diffusion within and Above a Submerged Canopy*

18 Because the canopy drag restricts the penetration of the canopy-scale vortices, a submerged canopy  
 19 is segregated into two zones characterized by distinct turbulence scales. The canopy-scale vortices  
 20 are excluded from the lower canopy ( $z < h - \delta_e$ ), and as a result the mechanisms of dispersion  
 21 resemble those described above for emergent canopies. In contrast, transport in the upper canopy ( $z$   
 22  $> h - \delta_e$ ) is dominated by the canopy-scale turbulence, so that the turbulent diffusivity scales on the

1 size of the canopy-scale vortices and the velocity difference,  $\Delta U$ , between the canopy and the  
 2 overflow, *e.g.* shown in Figure 4. The canopy-scale vortices grow to a size comparable to the shear-  
 3 layer thickness  $t_{ml}$ . These scales also apply above a canopy with shallow submergence ( $H/h < 5$ ),  
 4 because the canopy-shear-layer extends over most of the flow depth (Ghisalberti & Nepf 2005,  
 5 Ghisalberti & Nepf 2009). Based on experiments with rigid canopies,

$$6 \quad D \approx 0.02 \Delta U t_{ml} \quad (20)$$

8  
 9 over the entire shear-layer, *i.e.* both above and within the canopy (Figure 11 in Ghisalberti & Nepf  
 10 2005). Generally,  $t_{ml} \sim h$ , so (20) can be estimated from the canopy height,  $h$ , and the velocity  
 11 difference,  $\Delta U$ . The turbulent diffusivity has a peak at the top of the canopy, with  $D(z=h) \approx$   
 12  $0.032 \Delta U t_{ml}$ . As in a free-shear layer, the turbulent diffusivity is higher than the turbulent viscosity  
 13 ( $\nu_t$ ). The turbulent Schmidt number ( $S_t = \nu_t/D_t$ ) has a mean of 0.5 within the canopy-shear layer,  
 14 similar to other free shear layers, and a minimum of 0.3 at the top of the canopy, so that mass is  
 15 mixed across the canopy–water interface three times more rapidly than is momentum (Ghisalberti &  
 16 Nepf 2005, and references therein). For reference, in a neutral boundary layer  $S_t \approx 1$  (*e.g.*, Kaimal &  
 17 Finnigan 1994, *p.* 125). The lower value of  $S_t$  within a canopy shear-layer can be explained by the  
 18 numerical results discussed in Fitzmaurice *et al* (2004). Ensemble averages of the velocity and  
 19 pressure fields show that a region of high dynamic pressure is generated when a sweep encounters  
 20 the canopy. While sweep events carry momentum and scalar downward via identical motions, the  
 21 momentum transport is offset by high pressure generated at the canopy boundary, depressing the  
 22 turbulent Schmidt number.

23



## 1 **Summary**

2           Aquatic vegetation significantly alters the mean and turbulent flow field. Within emergent  
3 canopies, the turbulent length-scales are set by the stem diameter and spacing, and the mean flow is  
4 determined by the distribution of canopy frontal area. Sparse submerged canopies ( $ah < 0.1$ )  
5 enhance bed roughness and near-bed turbulence, but the velocity profile remains logarithmic. In  
6 contrast, dense submerged canopies ( $ah > 0.1$ ) transfer the velocity profile to a mixing layer. These  
7 canopies generate two distinct scales of turbulence: canopy-scale turbulence generated by flow  
8 instability at the top of the canopy, and stem-scale turbulence generated within the canopy. The  
9 canopy-scale turbulence penetrates into the canopy only over a length-scale dependent on the canopy  
10 drag,  $\delta_e \sim (C_{Da})^{-1}$ . This length-scale determines both the displacement thickness ( $z_m$ ) for the  
11 logarithmic velocity profile above the canopy, as well as the decay of stress-driven flow within the  
12 canopy. Further,  $\delta_e$  separates a dense canopy into two regions of distinct transport. The upper  
13 canopy ( $z > h - \delta_e$ ) experiences energetic vertical transport and high levels of turbulent diffusion,  
14 controlled by canopy-scale vortices. The lower canopy ( $z < h - \delta_e$ ) experiences significantly slower  
15 transport, associated with the smaller element-scale turbulence.

16

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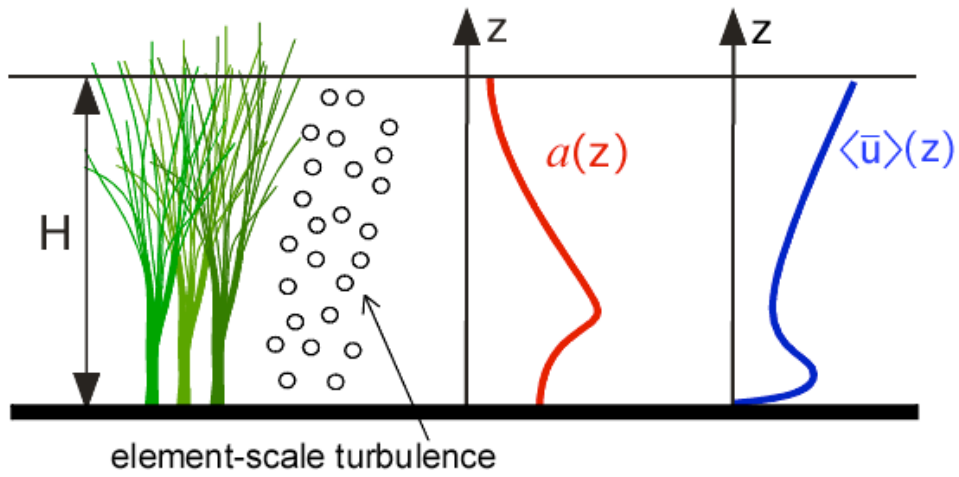
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1 **Figure 1.** Emergent canopy of marsh grass, with vertical profiles of leaf area index,  $a$ , and longitudinal velocity,  $\langle \bar{u} \rangle$ .

2 The velocity profile varies inversely with  $a$ , creating a velocity maximum close to the bed, below the level at which

3 branching begins.

4

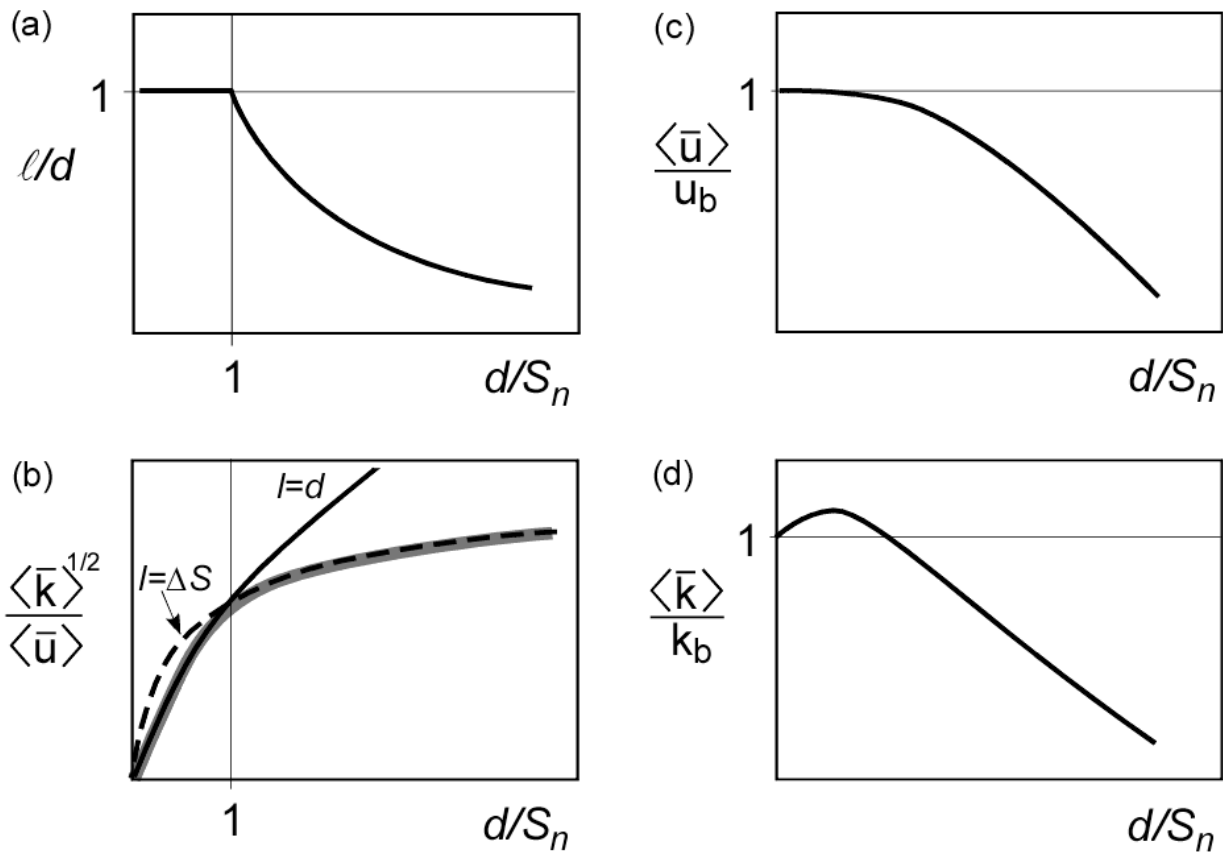


5

6

1 **Figure 2.** Changes in flow properties with increasing stem density. (a) The integral scale of  
 2 turbulence,  $\ell$ , is set by the smaller of two canopy scales: the stem diameter,  $d$ , and the nearest-  
 3 neighbor stem spacing,  $S_n$ . If  $d < S_n$ ,  $\ell = d$ . If  $d > S_n$ ,  $\ell = S_n$ . (b) The turbulence intensity, given by  
 4 (7), depends on the integral length-scale of the turbulence. If  $d < S_n$ , the turbulence intensity  
 5 increases rapidly with increasing stem density, because  $a\ell \approx d^2/S_n^2$ . If  $d > S_n$ , the turbulence intensity  
 6 increases more slowly, as  $a\ell \approx d/S_n$ . Changes in (c) velocity and (d) turbulent kinetic energy, with  
 7 increasing stem density, shown relative to values for a bare-bed (sub-script  $b$ ) with the same forcing.  
 8 Based on Fig. 10 in Nepf 2012, reproduced with the kind permission of Elsevier Press.

9

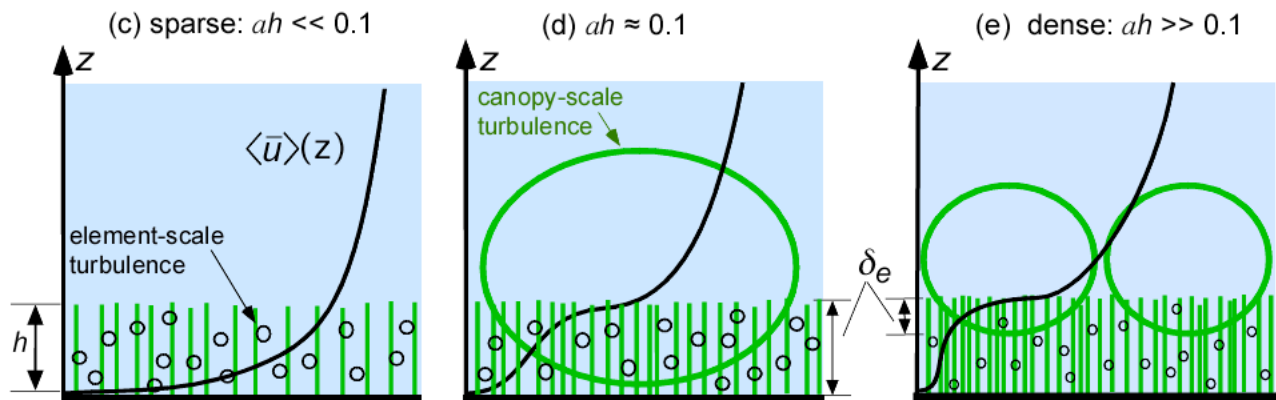
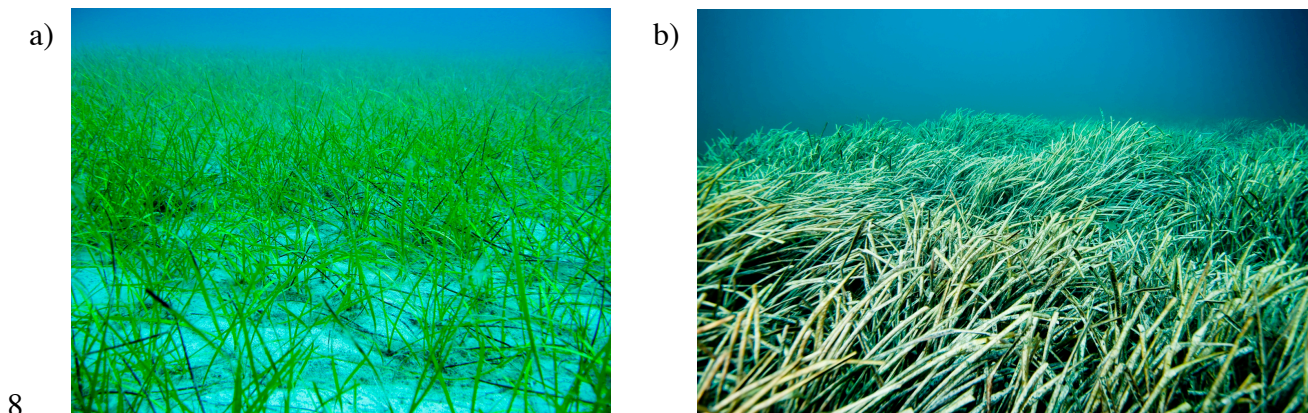


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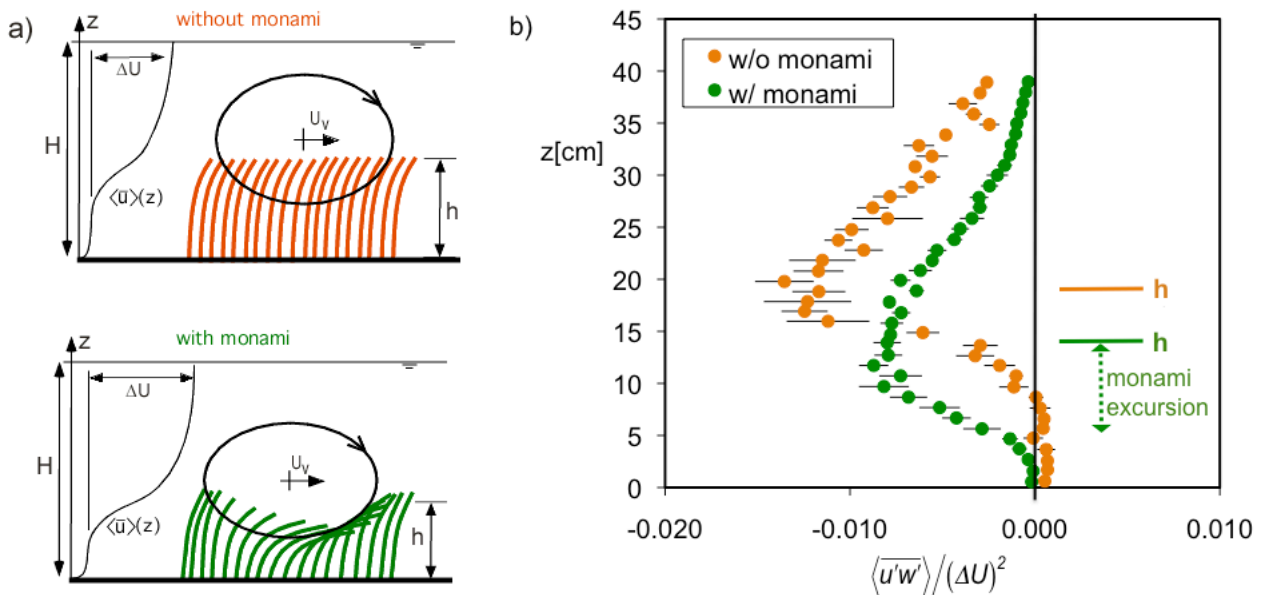
1 **Figure 3** a) seagrass *Cymodocea nodosa* at low stem density b) seagrass *Posidonia oceanica* at high  
 2 stem density. Photos by Eduardo Infantes Oanes. Vertical profiles of longitudinal velocity and  
 3 dominant turbulence scales for (c) sparse canopy ( $ah \ll 0.1$ ), (d) transitional canopy ( $ah \approx 0.1$ ) and  
 4 (e) dense canopy ( $ah > 0.1$ ).  $h$  is the submerged canopy height. For  $ah \approx > 0.1$ , a region of strong  
 5 shear at the top of the canopy generates canopy-scale turbulence. Element-scale (stem-scale)  
 6 turbulence is generated within the canopy.

7



10

1 **Figure 4.** a) For dense submerged canopies ( $ah > 0.1$ ), the drag discontinuity at the top of the  
 2 canopy generates a region of shear resembling a free-shear-layer, which in turn generates canopy-  
 3 scale vortices by Kelvin-Helmholtz instability. The passage these canopy-scale vortices over the  
 4 canopy may generate a progressive waving of the canopy that is called *monami* (green canopy). If  
 5 the shear-layer vortices are too weak, the canopy will bend, but not wave (orange canopy). b)  
 6 Profiles of normalized turbulent stress in and above a flexible canopy for two flow conditions, based  
 7 on data from Ghisalberti and Nepf (2006). With the weaker current, no *monami* occurs (orange  
 8 dots). With a stronger current, *monami* is produced (green dots). The vertical excursion of the  
 9 canopy interface associated with the *monami* is shown with the dashed double-arrow. Under the  
 10 stronger current (green dots), the individual blades are deflected further, reducing the mean canopy  
 11 height ( $h$ ), relative to the condition with the weaker current (orange dots).



12

13



1 **Figure 5.** Measured velocity (dots) from Ghisalberti (2005). Predicted velocity (solid line) with  
 2 confidence limits (dashed lines);  $H = 46.7$  cm,  $h = 13.9$  cm,  $S = 2.5 \times 10^{-5}$ ,  $a = 0.034$  cm<sup>-1</sup>,  $C_D = 0.77$   
 3 (measured). Above the meadow, the velocity is predicted from the logarithmic profile (12), with  $u^*$   
 4  $= (gS(H-h))^{1/2}$ ,  $z_m = h - (1/2)\delta_e$  (13), and  $z_o = (0.04 \pm 0.02)a^{-1}$ , as given in text. Inside the meadow the  
 5 velocity is predicted from (14) and (15), with  $U_h$  taken from logarithmic fit.  
 6

