

# A Smart Card-based Authentication Scheme Using User Identify Cryptography

Chin-Chen Chang<sup>1,2</sup> and Chia-Yin Lee<sup>3</sup>  
(Corresponding author: Chin-Chen Chang)

Department of Information Engineering and Computer Science, Feng Chia University<sup>1</sup>  
No. 100, Wenhwa Rd., Seatwen, Taichung 407, Taiwan

Department of Computer Science and Information Engineering, Asia University<sup>2</sup>  
No. 500, Lioufeng Rd., Wufeng, Taichung 413, Taiwan

Information & Communication Technology Laboratories, National Chiao Tung University<sup>3</sup>  
No. 1001, Tahsueh Rd., Hsinchu 300, Taiwan  
(Email: ccc@cs.ccu.edu.tw)

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## Abstract

The user authentication scheme is a useful mechanism for verifying the legitimacy of a remote user over insecure network environments. Recently, smart card-based user authentication schemes have been used in a wide range of applications, such as Internet commerce, electronic mail system, and voice over Internet protocol. However, most existing authentication schemes cannot protect the privacy of the user's identity. Therefore, the dynamic ID-based user authentication scheme is proposed to overcome this drawback. In this article, we analyze some security properties for recent dynamic ID-based user authentications. In addition, we propose an enhanced authentication scheme that can withstand the possible attacks and reduce the overhead of the system implementation.

*Keywords:* Authentication, dynamic identity, one-way hash function, smart card

## 1 Introduction

With the rapid growth of computer networks, the user client can access services or download data from remote servers. The user authentication scheme has become a simple and useful mechanism for verifying the legitimacy of the user's login request. In the general solution, such as Lamport's scheme [23], users must register with the server and keep identity/password pairs for login into the server; at the same time, the server must maintain a registration table to record the password for each registered user. However, when the server must keep so much secret information, security problems can occur and increase the overhead for verifying legal users. To overcome this drawback, Hwang and Li [14] proposed a new user authentication scheme using smart cards. Due to the fact that the smart card can store the verifier securely, there is no need for the remote server to maintain the password table for registered users. Subsequent to Hwang and Li's scheme, many user

authentication schemes based on smart cards have been proposed in the literature [3, 4, 5, 8, 10, 11, 13, 15, 17, 19, 20, 21, 22, 24, 25, 26, 28, 34, 36, 38, 40].

In a unidirectional authentication scheme, an entity can authenticate the other one by challenging some secret information. In addition, a mutual authentication protocol can allow two communicating parties to verify each other. As we know, there are four important security problems that an ideal user authentication scheme must solve, i.e., 1) it must determine whether users are legitimate or not; 2) the server must be authenticated; 3) a common session key can be established; and 4) the privacy of legal users must be ensured. To protect users' privacy, Das et al. [6] were the first to propose a dynamic, ID-based user authentication scheme. This scheme uses dynamic identity for each login session, thus, this scheme can reduce the threat of exposing a user's real identity. However, some researchers [1, 9, 18, 27, 29, 30, 33] have pointed out that Das et al.'s scheme might suffer from possible attacks. In 2009, Wang et al. [39] argued that Das et al.'s scheme does not provide mutual authentication and does not protect the user's password. By this security flaw, an adversary can use a random password to login into the server. To overcome this weakness, Wang et al. also proposed an improvement based on Das et al.'s scheme. Recently, Khan et al. [16] pointed out that Wang et al.'s scheme cannot protect the privacy of the user's identity and cannot construct a common session key between the user and the server. Khan et al. also proposed an enhanced version to overcome these drawbacks. In this article, we demonstrate that Wang et al.'s scheme suffers from the impersonation attack. In addition, both Wang et al.'s and Khan et al.'s schemes use the timestamp to prevent the replay attacks [37]. Actually, it is difficult to verify the timestamp when the user and the server are located in different time zones or when there is a congested network environment that has unstable latency. Therefore, additional time-synchronized mechanisms [31, 32] are needed to adjust the clock between these two parties.

Moreover, Khan et al.'s scheme uses a registration table to record the status of each registered user. This method not only resists the objective of using the smart card, but it also increases the overhead of the server to maintain the registration table. To overcome the above drawbacks, we propose a novel, user authentication scheme using a smart card. In addition, we proved the correctness of our scheme by using logical rules, and we demonstrated that our scheme can withstand possible attacks.

The rest of this article is organized as follows. In Section 2, we review Wang et al.'s scheme briefly. In Section 3, we demonstrate that Wang et al.'s scheme suffers from impersonation attacks. In addition, we discuss some drawbacks of related works. In Section 4, we propose an enhanced, dynamic ID-based user authentication scheme based on random nonces and one-way hash functions [35]. We present our analysis of the proposed scheme and compare the security properties with related works in Section 5. Some conclusions are summarized in Section 6.

## 2 Review of Wang et al.'s Scheme

In this section, we review Wang et al.'s scheme briefly. Their scheme is composed of four phases, i.e., the registration phase, the login phase, the verification phase, and the password change phase. The detailed processes of each phase are described below.

### Registration phase

When the user  $U_i$  wants to register with the remote server  $S$ ,  $U_i$  must choose an identity  $id_i$  and send the identity to  $S$  in a secure channel. After receiving the registration request, the server  $S$  performs the following processes.

- 1) Compute  $N_i = h(pw_i) \oplus h(x) \oplus id_i$ , where  $x$  is the secret key of  $S$ , and  $pw_i$  is the password of  $U_i$ , assigned by  $S$ .
- 2)  $S$  issues a smart card and then stores the parameters  $h(\cdot)$ ,  $N_i$ , and  $y$  into the smart card. Note that the parameter  $y$  is the secret code of  $S$ , shared with each registered user.
- 3) Deliver the smart card with corresponding password  $pw_i$  to  $U_i$  through a secure channel.

### Login phase

When the user  $U_i$  wants to login into the server  $S$ ,  $U_i$  inserts the smart card to the terminal device and keys in the identity  $id_i$  and the corresponding password  $pw_i$ . Afterward, the smart card performs the following processes.

- 1) Computes the dynamic identity  $CID_i$  as  $CID_i = h(pw_i) \oplus h(N_i \oplus y \oplus T) \oplus id_i$ , where  $T$  is the current timestamp.

- 2)  $U_i$  sends the login message  $m_1 = \{id_i, CID_i, N_i, T\}$  to the remote server  $S$  for verification.

### Verification phase

Upon receiving the message  $m_1 = \{id_i, CID_i, N_i, T\}$ , the server  $S$  performs the following processes.

- 1) Verify the timestamp by checking whether  $T' - T \leq \Delta T$ , where  $T'$  is current timestamp. If the result holds,  $S$  accepts the login request of  $U_i$ ; otherwise, the login request will be terminated.
- 2) Compute  $h(pw_i)^* = CID_i \oplus h(N_i \oplus y \oplus T) \oplus id_i$ .
- 3) Compute  $id_i^*$  as  $id_i^* = N_i \oplus h(x) \oplus h(pw_i)^*$  and verify whether it is equal to the received  $id_i$ . If the result is correct,  $S$  accepts the login request; otherwise, the login request is refused.
- 4) Compute  $a' = h(h(pw_i)^* \oplus y \oplus T')$  and then send the message  $m_2 = \{a', T'\}$  to the user  $U_i$ .

Upon receiving the response message  $m_2 = \{a', T'\}$  from  $S$  at time  $T''$ ,  $U_i$  checks the validity of timestamp  $T'' - T' \leq \Delta T$ ; if the timestamp is valid,  $U_i$  computes  $a = h(h(pw_i) \oplus y \oplus T')$  and then compares it with the received  $a'$ . If the result is equivalent, it means that the server  $S$  is authenticated.

### Password change phase

When the user  $U_i$  wants to change the current password,  $U_i$  inserts the smart card to the terminal device and keys in the current password  $pw_i$ ; next,  $U_i$  requests to change the password to a new one, i.e.,  $pw_i'$ . The smart card computes  $N_i' = N_i \oplus h(pw_i) \oplus h(pw_i')$  and replaces the original parameter  $N_i$  stored in the smart card with the new parameter  $N_i'$ .

## 3 Comments on Related Works

First of all, we point out that Wang et al.'s scheme might suffer from the impersonation attack. Then, we discuss some drawbacks of related works.

### 3.1 Weaknesses of Wang et al.'s Scheme

We consider a scenario when an attacker  $U_A$  wants to use an intended identity  $id_A$  to login into the server  $S$ . Suppose that  $U_A$  has collected previous login messages transmitted between a legal user  $U_i$  and the server  $S$ . Therefore,  $U_A$  can obtain the login parameters  $id_i, CID_i$ ,

and  $N_i$  and the past timestamp  $T$ . Afterward, the attacker can masquerade as a legal user to cheat the server as shown below:

- 1)  $U_A$  forges the login parameters  $id_A$ ,  $CID_A$ , and  $N_A$  such as  $id_A = id_i \oplus T \oplus T_A$ ,  $CID_A = CID_i \oplus T \oplus T_A$ , and  $N_A = N_i \oplus T \oplus T_A$ , where  $T_A$  is the current timestamp.
- 2)  $U_A$  sends the login message  $\{id_A, CID_A, N_A, T_A\}$  to  $S$  for verification.

Upon receiving the message  $\{id_A, CID_A, N_A, T_A\}$  at time  $T^*$ , the server  $S$  verifies the user by the following processes:

- 1) Check whether  $T^* - T_A \leq \Delta T$ ; actually, the result holds since the timestamp  $T_A$  is correct.

- 2)  $S$  computes the term  $h(pw_A)^*$  as  $h(pw_A)^* = CID_A \oplus h(N_A \oplus y \oplus T_A) \oplus id_A$ . Note that  $h(pw_A)^*$  can be written as:

$$h(pw_A)^* = CID_i \oplus T \oplus T_A \oplus h(N_i \oplus T \oplus T_A \oplus y \oplus T_A) \oplus id_i \oplus T \oplus T_A = CID_i \oplus h(N_i \oplus y \oplus T) \oplus id_i.$$

- 3)  $S$  computes  $id_A^*$  as  $id_A^* = N_A \oplus h(x) \oplus h(pw_A)^*$  and verifies whether  $id_A^*$  is equal to the received  $id_A$ . If  $id_A^* = id_A$ , the server  $S$  will validate that  $U_A$  is a legal user.

We show that the term  $id_A^*$  in 3) is equal to  $id_A$  as follows:

$$\begin{aligned} id_A^* &= N_i \oplus T \oplus T_A \oplus h(x) \oplus CID_i \oplus h(N_i \oplus y \oplus T) \oplus id_i \\ &= h(pw_i) \oplus h(x) \oplus id_i \oplus T \oplus T_A \oplus h(x) \oplus h(pw_i) \oplus h(N_i \oplus y \oplus T) \oplus id_i \oplus \\ &\quad h(N_i \oplus y \oplus T) \oplus id_i \\ &= id_i \oplus T \oplus T_A \\ &= id_A. \end{aligned}$$

From the above derivative result, we demonstrate that Wang et al.'s scheme suffers from the impersonation attack. On the other hand, Wang et al.'s scheme does not preserve the feature of anonymity for users, since the users must send their real identities to the server for authentication. Therefore, this scheme loses the property of dynamic identity.

### 3.2 Some Drawbacks of Related Works

In order to provide the feature of anonymity and provide session key establishment, Khan et al. proposed an improved version of Wang et al.'s scheme. Khan et al.'s scheme has many attractive features, such as user anonymity, session key establishment, and lost smart card revocation. However, the remote server must maintain a registration table to record the status of each registered user. This table may increase the system overhead on the server

side. In other words, it will spend much time to recognize the legal user when the table stores tens of thousands of records. On the other hand, both Wang et al.'s and Khan et al.'s schemes use the timestamp to withstand the replay attacks. As we know, it is difficult to verify the timestamp when participants are located in different time zones or when there is a congested network environment that has variant delay time. Thus, additional time-synchronized mechanisms are needed to adjust the clock between the client and the server.

In this article, we propose an improvement to enhance the security and performance of Wang et al.'s and Khan et al.'s schemes. Our scheme not only can achieve all security requirements presented in related works, but it can do so without using any time-synchronized mechanism. The detailed processes of our scheme are described in the next section.

## 4 Proposed Scheme

In this section, we propose an enhanced, dynamic ID-based user authentication scheme without timestamps. Our scheme consists of four phases, i.e., the registration phase, the authentication phase, the password change phase, and the lost card revocation phase.

### Registration phase

First of all, the user  $U_i$  selects a fixed length  $id_i$  and corresponding  $pw_i$  to be her/his identity and password, respectively. Next,  $U_i$  submits  $id_i$  and  $pw_i$  to the server  $S$  for registration. Suppose that  $x$  and  $y$  are two secret keys of  $S$ ; then,  $S$  executes the following steps:

- 1) Select a 128-bit sized integer  $r_i$  randomly.
- 2) Compute  $R_1 = h(id_i \parallel x \parallel r_i)$ , where  $h(\cdot)$  is a collision-resistant, one-way hash function, such as SHA [42].
- 3) Compute  $R_2 = g^{xy} \bmod p$ , where  $g$  is a primitive element in  $Z_p^*$ , and  $p$  is a large prime number.
- 4) Compute  $R_3 = h(id_i \parallel R_2) \oplus h(pw_i)$ .
- 5) Issue a smart card with a 32-bit sized serial number  $sn_i$ , where  $sn_i$  has a specific format.
- 6) Combine the identity of the user  $U_i$  with the serial number of the smart card as  $SID_i = (id_i \parallel sn_i)$ , where the symbol  $\parallel$  denotes the concatenation operation.
- 7) Finally, store  $R_1$ ,  $R_2$ ,  $R_3$ ,  $SID_i$  and  $h(\cdot)$  on the smart card and, then, deliver the smart card to the user  $U_i$ .

All processes of the registration phase must be conducted in a secure manner. The registration phase is illustrated in Figure 1.

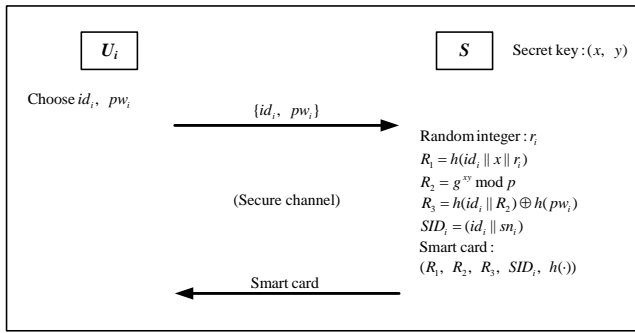


Figure 1: The registration phase of the proposed scheme

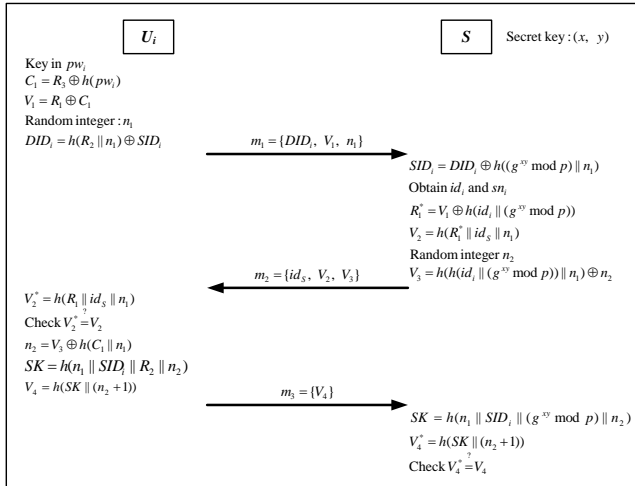


Figure 2: The authentication phase of the proposed scheme

### Authentication phase

We assume that a mobile user  $U_i$  requests to access the server  $S$ . Before providing services,  $S$  must authenticate the legitimacy of  $U_i$ . For authentication,  $U_i$  inserts the smart card to the terminal device and then inputs her/his password  $pw_i$ . Afterward, the smart card performs the following steps:

- 1) Compute  $C_1 = R_3 \oplus h(pw_i)$ .
- 2) Compute  $V_1 = R_1 \oplus C_1$ .
- 3) Generate a 160-bit sized integer  $n_1$  randomly.
- 4) Generate a dynamic identity  $DID_i$  by computing  $DID_i = h(R_2 || n_1) \oplus SID_i$ .
- 5) Finally, send the message  $m_1 = \{DID_i, V_1, n_1\}$  to  $S$  for authentication.

Upon receiving the authentication request message  $m_1$ , the server  $S$  performs the following steps:

- 1) Obtain the term  $SID_i$  by computing  $SID_i = DID_i \oplus h((g^{xy} \text{ mod } p) || n_1)$ .
- 2) Retrieve the identity  $id_i$  and the serial number  $sn_i$  from the term  $SID_i$  and then check the format of  $id_i$  and  $sn_i$ .

Note that the server  $S$  can use the serial number  $sn_i$  to determine whether the smart card is revoked.

- 3) Compute  $R_1^* = V_1 \oplus h(id_i || (g^{xy} \text{ mod } p))$ .
- 4) Generate a 160-bit sized integer  $n_2$  randomly.
- 5) Compute  $V_2 = h(R_1^* || id_i || n_1)$  and  $V_3 = h(h(id_i || (g^{xy} \text{ mod } p)) || n_1) \oplus n_2$ , and then send the message  $m_2 = \{id_i, V_2, V_3\}$  to the user  $U_i$ .

Upon receiving the message  $m_2$ , the user  $U_i$  executes the following steps:

- 1) Compute  $V_2^* = h(R_1 || id_i || n_1)$ .
- 2) Check whether  $V_2^* = V_2$ . If the result holds, the server  $S$  is authenticated; otherwise, the connection with the server is terminated.
- 3) Obtain the random nonce  $n_2$  by computing  $n_2 = V_3 \oplus h(C_1 || n_1)$ .
- 4) Generate the session key  $SK$  shared with  $S$  by computing  $SK = h(n_1 || SID_i || R_2 || n_2)$ .
- 5) Compute  $V_4 = h(SK || (n_2 + 1))$  and send the message  $m_3 = \{V_4\}$  to  $S$ .

After receiving the message  $m_3$ , the server  $S$  performs the following processes:

- 1) Generate the session key  $SK$  shared with the user  $U_i$  by computing  $SK = h(n_1 || SID_i || (g^{xy} \text{ mod } p) || n_2)$ .
- 2) Compute  $V_4^*$  as  $V_4^* = h(SK || (n_2 + 1))$  and check whether  $V_4^* = V_4$ . If they are equivalent, the user  $U_i$  is authenticated, and the session key  $SK$  shared with  $U_i$  is authenticated. After that, the server  $S$  can provide service or send messages securely by using the session key  $SK$  to encrypt the content.

The authentication processes between the user  $U_i$  and the server  $S$  are illustrated in Figure 2.

Note: To prevent on-line password guessing attacks, if the verifying result of the equation  $V_4^* = V_4$  is invalid more than three times continuously for the same  $id_i$ , the server  $S$  will revoke the smart card with the serial number  $sn_i$ .

### Password change phase

When the user  $U_i$  wants to change the current password  $pw_i$  to a new password  $pw'_i$ ,  $U_i$  must insert the smart card to the terminal device and key in the identity  $id_i$  with corresponding password  $pw_i$ . Then, the smart card will perform the following processes without interacting with the server  $S$ .

- 1) Compute  $Q_1 = h(id_i || R_2)$  and  $Q_1^* = R_3 \oplus h(pw_i)$ .

- 2) Compare  $Q_1$  with  $Q_1^*$ ; if  $Q_1 = Q_1^*$ ,  $U_i$  is allowed to change the password. Otherwise, the password change procedure is terminated.
- 3) Compute the new term  $R_3'$  as  $R_3' = h(id_i \| R_2) \oplus h(pw_i) \oplus h(pw_i') \oplus h(pw_i')$  and replace the original  $R_3$  with the new  $R_3'$ .

### Lost card revocation phase

When the user  $U_i$  loses her/his smart card,  $U_i$  must notify the server  $S$  to revoke the smart card. When receiving the revocation request,  $S$  first validates the  $U_i$  by checking her/his secret personal information. All procedures in this phase are executed through a secure channel. After validating the revocation request,  $S$  records the serial number  $sn_i$  of the revoked smart card in the database and issues a new smart card with new serial number  $sn_i'$  for  $U_i$ . Afterward,  $U_i$  can choose a new password for the new smart card by executing the procedure similar to the registration phase.

## 5 Security Analysis

In 1990, Burrows et al. [2] proposed useful logical rules to prove the validity of authentication protocols. We used the BAN logic proposed by Burrows et al. to analyze the authentication procedures of the proposed scheme. Then, we show that our scheme can withstand some possible attacks.

### 5.1 Authentication Proof based on BAN Logic

We used BAN logic to verify that our user identification protocol can achieve mutual authentication. The main goal of our protocol is to establish a common session key  $SK$  between the user  $U_i$  and the remote server  $S$ . We used the following logical postulates to show that  $U_i$  and  $S$  can mutually authenticate and share a session key  $SK$ .

$U_i$  believes  $id_S$ ,

$S$  believes  $id_i$ ,

$U_i$  believes  $S$  believes  $U_i \xleftrightarrow{SK} S$ ,

$U_i$  believes  $U_i \xleftrightarrow{SK} S$ ,

$S$  believes  $U_i$  believes  $U_i \xleftrightarrow{SK} S$ , and

$S$  believes  $U \xleftrightarrow{SK} S$ .

According to the analytical procedures of BAN logic, each round of the protocol must be transformed into an idealized form. First, we illustrate some notations of BAN logic as follows.

$(X, Y)$ : formula  $X$  or formula  $Y$  is one part of formula  $(X, Y)$ .

$\langle X \rangle_S$ : formula  $X$  combined with a secret parameter  $S$ .

$\{X\}_K$ : formula  $X$  encrypted by the secret key  $K$ .

$P \xleftrightarrow{K} Q$ :  $P$  and  $Q$  may use the shared key  $K$  to communicate. Note that  $K$  will never be discovered by anyone except  $P$  and  $Q$ .

$P \xleftrightarrow{S} Q$ : The secret formula  $S$  is known only to  $P$  and  $Q$ . Only  $P$  and  $Q$  can use  $S$  to prove their identities to each other.

We use BAN logic to transform our protocol, illustrated in Figure 2, into the idealized form. We show the messages in idealized form as follows:

$m_1. U_i \rightarrow S : \{SID_i, n_1\}_{R_2}$ .

$m_2. S \rightarrow U_i :$

$\langle id_S, n_1 \rangle_{R_1}, \{S \xleftrightarrow{U_i, n_1}\}_{h(id_i \| R_2)}, \{S \xleftrightarrow{SK} U_i, n_1\}_{n_2}$ .

$m_3. U_i \rightarrow S : \{U_i \xleftrightarrow{SID_i} S, n_2\}_{R_2}, \{S \xleftrightarrow{SK} U_i, n_2\}_{SID_i}$ .

Since the server  $S$  shares secrets, such as  $R_1 = h(id_i \| x \| r_i)$ ,  $R_2 = g^{xy} \bmod p$ , and  $h(id_i \| R_2)$ , with the user  $U_i$  via the smart card, we can make some assumptions without loss of generality as follows:

A1.  $U_i$  believes fresh  $n_1$ .

A2.  $S$  believes fresh  $n_2$ .

A3.  $U_i$  believes  $U_i \xleftrightarrow{R_1} S$ .

A4.  $U_i$  believes  $U_i \xleftrightarrow{h(id_i \| R_2)} S$ .

A5.  $S$  believes  $U_i \xleftrightarrow{R_2} S$ .

A6.  $S$  believes  $U_i \xleftrightarrow{h(id_i \| R_2)} S$ .

A7.  $U_i$  believes ( $S$  controls  $id_S$ ).

A8.  $U_i$  believes ( $S$  controls  $U_i \xleftrightarrow{n_2} S$ ).

A9.  $U_i$  believes ( $S$  controls  $U_i \xleftrightarrow{SK} S$ ).

A10.  $S$  believes ( $U_i$  controls  $U_i \xleftrightarrow{SID_i} S$ ).

A11.  $S$  believes ( $U_i$  controls  $U_i \xleftrightarrow{SK} S$ ).

Actually, assumptions A1 and A2 are basic assumptions

of BAN logic. We analyzed the idealized form of the proposed authentication protocol using the assumptions above and the rules of BAN logic. We show the main steps of the proof as follows:

By  $m_1$  and A5, we apply the message-meaning rule to derive  
 $S$  believes  $U_i$  said  $(SID_i, n_1)$ . (Statement 1)

By  $m_2$ , we break conjunctions and produce the following:  
 $U_i$  sees  $\langle id_S, n_1 \rangle_{R_1}$ , (Statement 2)

$U_i$  sees  $\{S \leftrightarrow U_i, n_1\}_{h(id_i || R_2)}$ , (Statement 3)

and

$U_i$  sees  $\{S \leftrightarrow U_i, n_1\}_{SK}$ . (Statement 4)

By A3 and Statement 2, we apply the message-meaning rule to derive

$U_i$  believes  $S$  said  $(id_S, n_1)$ . (Statement 5)

By A1 and Statement 5, we apply the nonce-verification rule to deduce

$U_i$  believes  $S$  believes  $(id_S, n_1)$ . (Statement 6)

By Statement 5, we break the conjunction to obtain

$U_i$  believes  $S$  believes  $id_S$ . (Statement 7)

By A7 and Statement 7, we apply the jurisdiction rule to obtain

$U_i$  believes  $id_S$ . (Statement 8)

By A4 and Statement 3, we apply the message-meaning rule to derive

$U_i$  believes  $S$  said  $(S \leftrightarrow U_i, n_1)$ . (Statement 9)

By A1 and Statement 9, we apply the nonce-verification rule to deduce

$U_i$  believes  $S$  believes  $(S \leftrightarrow U_i, n_1)$ . (Statement 10)

By Statement 10, we break the conjunction to derive

$U_i$  believes  $S$  believes  $S \leftrightarrow U_i$ . (Statement 11)

By A8 and Statement 11, we apply the jurisdiction rule to obtain

$U_i$  believes  $S \leftrightarrow U_i$ . (Statement 12)

By Statement 4 and Statement 12, we apply the message-meaning rule to derive

$U_i$  believes  $S$  said  $(U_i \leftrightarrow S, n_1)$ . (Statement 13)

By A1 and Statement 13, we apply the nonce-verification rule to deduce

$U_i$  believes  $S$  believes  $(U_i \leftrightarrow S, n_1)$ . (Statement 14)

By Statement 14, we break the conjunction to derive

$U_i$  believes  $S$  believes  $(U_i \leftrightarrow S)$ . (Statement 15)

By A9 and Statement 15, we apply the jurisdiction rule to obtain

$U_i$  believes  $S \leftrightarrow U_i$ . (Statement 16)

By  $m_3$ , we break conjunctions and produce the following:

$S$  sees  $\{U_i \leftrightarrow S, n_2\}_{R_2}$ , (Statement 17)

and

$S$  sees  $\{S \leftrightarrow U_i, n_2\}_{SID_i}$ . (Statement 18)

By A5 and Statement 17, we apply the message-meaning rule to derive

$S$  believes  $U_i$  said  $(U_i \leftrightarrow S, n_2)$ . (Statement 19)

By A2 and Statement 19, we apply nonce-verification rule to deduce

$S$  believes  $U_i$  believes  $(U_i \leftrightarrow S, n_2)$ . (Statement 20)

By Statement 20, we break the conjunction to obtain

$S$  believes  $U_i$  believes  $U_i \leftrightarrow S$ . (Statement 21)

By A10 and Statement 21, we apply the jurisdiction rule to deduce

$S$  believes  $U_i \leftrightarrow S$ . (Statement 22)

According to the equation  $SID_i = (id_i || sn_i)$ , we can derive

$S$  believes  $id_i$ . (Statement 23)

By Statement 18 and Statement 22, we apply the message-meaning rule to obtain

$S$  believes  $U_i$  said  $(S \leftrightarrow U_i, n_2)$ . (Statement 24)

By A2 and Statement 24, we apply nonce-verification rule to deduce

$S$  believes  $U_i$  believes  $(S \leftrightarrow U_i, n_2)$ . (Statement 25)

By Statement 25, we break the conjunction to obtain

$S$  believes  $U_i$  believes  $U_i \leftrightarrow S$ . (Statement 26)

By A11 and Statement 26, we apply the jurisdiction rule to derive

$S$  believes  $U_i \leftrightarrow S$ . (Statement 27)

Based on Statement 15, Statement 16, Statement 26, and Statement 27, we prove that the proposed protocol establishes an authenticated session key  $SK$  between the user  $U_i$  and the server  $S$ . Due to the aforementioned results of Statement 8 and Statement 23, we also prove that  $U_i$  and  $S$  are able to authenticate each other using our protocol.

## 5.2 Withstand Possible Attacks

In order to prove that the proposed scheme can withstand possible attacks, some basic security assumptions are given as follows:

Table 1: Comparison of security properties among related works

Items	Das et al.'s [6]	Wang et al.'s [39]	Khan et al.'s [16]	Ours
<b>Mutual authentication</b>	No	Yes	Yes	Yes
<b>Password chosen by users</b>	Yes	No	Yes	Yes
<b>User anonymity</b>	Yes	No	Yes	Yes
<b>Without registration table</b>	Yes	Yes	No	Yes
<b>Withstand impersonation attacks</b>	No	No	Yes	Yes
<b>Without time-synchronized mechanisms</b>	No	No	No	Yes
<b>Session key establishment</b>	No	No	Yes	Yes
<b>Perfect forward secrecy</b>	No*	No*	Yes	Yes

\* Since Das et al.'s and Wang et al.'s schemes do not provide session key establishment, these two schemes do not provide the property of perfect forward secrecy for transmitted messages.

- **Assumption 1** Security characteristic of smart cards

According to the smart card standard ISO/IEC 7816-4 [41], we assume that secret data, such as  $R_1$ ,  $R_2$ ,  $R_3$ , and  $SID_i$ , which are stored in the smart card cannot be retrieved by any outside entity.

- **Assumption 2** One-way hash function assumption

Let  $h(\cdot)$  be a one-way hash function; then, 1) for any input  $x$ , it is easy to compute the hash value  $y$ , where  $y = h(x)$ ; 2) given a hash value  $y$ , it is computationally intractable to recover  $x$  satisfying the equation  $y = h(x)$ ; 3) it is difficult to find  $x_1 \neq x_2$ , such that  $h(x_1) = h(x_2)$ .

We show that the proposed scheme can resist certain possible attacks. Assume that communications are insecure and that there exists an adversary  $U_A$ . Therefore,  $U_A$  can intercept all messages communicated between  $U_i$  and  $S$ . In addition, we also assume that  $U_A$  can obtain or steal legal user  $U_i$ 's smart card. We discuss some scenarios as follows.

#### Withstand replay attacks

The adversary  $U_A$  might replay an intercepted message  $m_1 = \{DID_i, V_1, n_1\}$  to the server  $S$  for authentication. Later on,  $S$  responds by sending the message  $m_2 = \{id_s, V_2, V_3\}$  to  $U_A$ . Thus,  $U_A$  tries to recover the nonce  $n_2$  from the received  $V_3$ . First,  $U_A$  must obtain the secret parameter  $R_3$  and the correct  $h(pw_i)$ . However,  $U_A$  cannot obtain the secret parameter  $R_3$  from the stolen

smart card (**Assumption 1**). In addition,  $U_A$  cannot compute the correct  $h(pw_i)$  since the password  $pw_i$  is unknown. Therefore,  $U_A$  cannot compute a correct  $V_4 = h(h(n_1 \| id_i \| R_2 \| n_2) \| (n_2 + 1))$  to pass the authentication procedure.

#### Withstand impersonation attacks

The adversary  $U_A$  might intercept the messages  $m_1 = \{DID_i, V_1, n_1\}$  and  $m_3 = \{V_4\}$  transmitted from legal user  $U_i$  in the previous sessions.  $U_A$  sends the authentication request  $m_1$  to  $S$  and then tries to forge a message  $m'_3 = \{V'_4\}$  and sends  $m'_3$  to  $S$  for authentication. However,  $U_A$  has no capability to forge a valid  $V'_4$  as  $V'_4 = V_4^*$ , since  $U_A$  cannot obtain the correct  $n_2$ . Thus,  $U_A$  cannot masquerade a legal user to cheat the server successfully.

#### Withstand identity disclosure attacks [12]

Assume that the adversary  $U_A$  is a legal user and that  $U_A$  wants to obtain the other legal user  $U_i$ 's identity  $id_i$  from a intercepted  $DID_i$ . Due to  $DID_i = h(R_2 \| n_1) \oplus (id_i \| sn_i)$ , first,  $U_A$  must obtain the correct  $R_2$ .  $U_A$  might key in her/his correct password  $pw_A$  to obtain a correct  $DID_A$  from the smart card, and then  $U_A$  tries to retrieve the parameter  $R_2$  from this  $DID_A$ . However, it will be difficult for  $U_A$  to derive  $R_2$  as a result of the security characteristic of one-way hash functions (**Assumption 2**).

#### Perfect forward secrecy [7]

In the proposed scheme, the common session key  $SK$  between the user  $U_i$  and the server  $S$  is established when each authentication session is completed successfully. Afterward,  $U_i$  and  $S$  can use  $SK$  to execute encryption and decryption of subsequent messages. Due to the reason that the session key is constructed by a one-way hash function with random nonces, such as  $n_1$  and  $n_2$ , in each session, the subsequent messages transmitted between  $U_i$  and  $S$  are encrypted using this session key. Suppose that the adversary  $U_A$  has the ability to capture all encrypted messages from the network. Even if the server  $S$ 's long-term secret key  $(x, y)$  is exposed to the attacker, it is computationally infeasible to derive the previous encryption messages without knowing the one-time session key  $SK$ .

We summarize some major security properties of authentication schemes and compare our scheme with related works in Table 1. The results show that our scheme is the only one that is capable of achieving all security requirements.

## 6 Conclusions

In this article, we discussed some drawbacks and weaknesses of existing dynamic ID-based user authentication schemes. We also proposed an enhanced scheme to withstand possible attacks and achieve the security properties presented in related works. In addition, our scheme uses random nonces to withstand replay attacks, so it can be implemented easily without additional, time-synchronized mechanisms.

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**Chin-Chen Chang** received the B.S. degree in applied mathematics and the M.S. degree in computer and decision sciences from National Tsing Hua University, Hsinchu, Taiwan, in 1977 and 1979, respectively. He received the Ph.D. degree in computer engineering from National Chiao Tung University, Hsinchu, Taiwan, in 1982. During the years 1980-1983, Dr. Chang was on the faculty of the Department of Computer Engineering, National Chiao Tung University. From 1983 to 1989, he was on the faculty of the Institute of Applied Mathematics, National Chung Hsing University, Taichung, Taiwan. From 1989 to 2002 he was a full professor of the Department of Computer Science and Information Engineering, National Chung Cheng University, Chiayi, Taiwan. From 2002 to 2005, he was a chair professor at the same University. Since February 2005, he has been a chair professor at Feng Chia University, Taichung, Taiwan. His current research interests include database design, computer cryptography, image compression, and data structures. Dr. Chang is a fellow of IEEE.

**Chia-Yin Lee** received his B.S. and M.S. degrees in computer science and information engineering from Tunghai University, Taichung, Taiwan, in 2001 and 2004, respectively. He received the Ph.D. degree in computer science and information engineering from National Chung Cheng University, Chiayi, Taiwan, in 2010. Since August 2011, Dr. Lee has been a postdoctoral research fellow at Information & Communication Technology Laboratories, National Chiao Tung University, Hsinchu, Taiwan. His research interests include information security and image processing.