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ON THE CORRECTNESS OF ORPHAN ELIMINATION ALGORITHMS

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Abstract

In a distributed system, node crashes and network delays can result in *orphaned* computations: computations that are still running but whose results are no longer needed. Several algorithms have been proposed to detect and eliminate such computations before they can see inconsistent states. In this paper we analyze two orphan elimination algorithms that have been proposed for nested transaction systems. We describe the algorithms formally, and present complete detailed proofs of correctness. Our proofs are remarkably simple, and show that the fundamental concepts underlying the two algorithms are quite similar. In addition, we show formally that the algorithms can be used in combination with any correct concurrency control technique, thus providing formal justification for the informal claims made by the algorithms' designers. Our results are a significant advance over earlier work in the area, in which it was extremely difficult to state and prove comparable results.

1. Introduction

Nested transaction systems are being explored in a number of projects (e.g., see [6, 18, 15, 1]) as a means for organizing computations in a distributed system. Like ordinary transactions, nested transactions provide a simple means for coping with concurrency and failures. In addition, nested transactions extend the usual notion of transactions [2, 14] to permit concurrency within a single action and to provide a greater degree of fault-tolerance, by isolating a transaction from a failure of one of its descendants.

In a distributed system, however, various factors, including node crashes and network delays, can result in *orphaned* computations: computations that are still running but whose results are no longer needed. For example, in the Argus system [6], the node making a remote request may give up because a network partition or some other problem makes it impossible to communicate with the other node. This may leave a process running at the called node; this process is an orphan. The orphan runs as a descendant of

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the transaction that made the call. Since the caller gives up by aborting the transaction that made the call, the orphan cannot have any permanent effects on the state of the system.

As discussed in [7, 11], however, orphans are still undesirable, for two reasons. First, they waste resources: they use processor cycles, and may also hold locks, causing other computations to be delayed. Second, they may see inconsistent information. For example, a transaction might be reading data at two nodes, with some invariant relating the states of the data. If the transaction reads data at one of the nodes and then becomes an orphan, another transaction could change the data at both nodes before the orphan reads the data at the second node. This could happen, for example, because the first node learns that the transaction has aborted and releases its locks. While the inconsistencies seen by an orphan should not have any permanent effect on the internal state of the system, they can cause strange behavior if the orphan is interacting with the external world, and can also make programs difficult to debug.

Several algorithms have been proposed to prevent orphans from seeing inconsistent information. Early work in the area includes Nelson's thesis [13], which describes algorithms for detecting and eliminating orphans that arise because of crashes. Nelson's work did not assume an underlying transaction mechanism, so that it was difficult to assign a simple semantics to abandoned computations. Recent work [19, 7, 11] has studied orphans in the context of a nested transaction system, in which an abandoned computation can be *aborted*, preventing it from having any effect on the state of the system. The goal of the algorithms in [19, 7, 11] is to detect and eliminate orphans before they can see inconsistent information.

In this paper we give formal descriptions and correctness proofs for two orphan elimination algorithms in [7] and [11]. The algorithm in [7] is currently in use in the Argus system. Our analysis covers only orphans resulting from aborts of actions that leave running descendants; we are currently working on modelling crashes and describing the parts of the algorithms that handle orphans that result from crashes. Our proofs are completely rigorous, yet quite simple. In addition, both the presentations and the proofs follow the intuitions which the designers use in describing the algorithms.

Our proofs clarify the fundamental concepts underlying the algorithms. We define a single general correctness condition for algorithms that eliminate orphans that result from aborts, and prove that both algorithms ensure this condition. While the algorithms seem quite different, our proofs show that the underlying ideas are quite similar.

The designers of the algorithms have claimed that the algorithms work in combination with any concurrency control protocol that ensures serializability of committed transactions. Our correctness condition relates the behavior of a system containing an orphan elimination algorithm to a system with no orphan elimination: the system with orphan elimination must "simulate" the system without orphan

elimination, in the sense that each transaction in the system with orphan elimination must see a view of the system it could see in an execution of the other system in which it was not an orphan. (By a view of the system, we mean the results of operations invoked by the transaction.) Thus, if the concurrency control protocol ensures that non-orphans see consistent views, our correctness condition implies that the orphan elimination algorithm will guarantee that all transactions see consistent views. This provides formal justification for the informal claims made by the algorithms' designers.

The formalism used in this paper is based on that in [9]. In [9], Lynch and Merritt develop a model for nested transaction systems including aborts, and use the model to show that an exclusive locking variation of Moss's algorithm [12] ensures correctness for non-orphans. In this paper we use the model to describe the orphan elimination algorithms, to state correctness properties, and to prove them correct.

Earlier work on verifying the Argus algorithm was done by Goree [4], who used a simple trace-based model for nested transaction systems [8]. While Goree was able to state and prove similar properties of the algorithm, the correctness properties were difficult to state and the proofs were extremely complex. In contrast, the correctness property described below is simple and intuitive, and our proofs are correspondingly simple. This provides strong evidence that the basic model from [9] is both simple and powerful enough for modelling and analyzing nested transaction systems.

The remainder of the paper is organized as follows. We begin in Section 2 with a brief description of *I/O automata*, which serve as the formal foundation for our work. Then, in Section 3, we review the relevant material from [9]. The material in these two sections is largely abstracted from [9], except for Section 3.5; the reader who is familiar with [9] is encouraged to skim these sections quickly.

In Section 4, we present some basic definitions and results that underlie the results to be presented in the rest of the paper. In the following sections, we present a series of different systems. The first, called a *filtered system*, abstracts the fundamental property ensured by both orphan elimination algorithms; we prove that a filtered system simulates the corresponding system without orphan elimination in the appropriate way. We also show that filtered systems ensure correctness for all transactions when combined with any concurrency control protocol that ensures correctness for non-orphans.

The second system, called an *Argus system*, provides a rigorous and detailed model for the Argus orphan elimination algorithm. We show that Argus systems simulate filtered systems. The third system, called a *strictly filtered system*, is a simple restriction of filtered systems that serves as an intermediate step in the proof of the algorithm from [11]. The fourth system, called a *clock system*, models the algorithm from [11]. We show that strictly filtered systems simulate filtered systems, and that clock systems simulated strictly filtered systems. The simulation results compose in a simple way, showing that both algorithms are correct, and that, like filtered systems, both algorithms can be used with any

concurrency control protocol that ensures correctness for non-orphans.

After presenting the descriptions and proofs of the algorithms, we conclude in Section 9 with a summary of our results and some suggestions for further work.

2. Basic Model

We use the I/O automaton model [10], a simple model for concurrent systems, as the formal foundation for our work. This model consists of (possibly infinite-state) nondeterministic automata that have operation names associated with their state transitions. Communication among automata is described by identifying their operations. In this paper, we only prove properties of finite behavior, so we only require a simple special case of the general model. In this section, we give a concise review of the relevant definitions.

2.1. I/O Automata

An I/O automaton \mathcal{A} has components $states(\mathcal{A})$, $start(\mathcal{A})$, $out(\mathcal{A})$, $in(\mathcal{A})$, and $steps(\mathcal{A})$. Here, $states(\mathcal{A})$ is a set of states, of which a subset $start(\mathcal{A})$ is designated as the set of start states. The next two components are disjoint sets: $out(\mathcal{A})$ is the set of *output operations*, and $in(\mathcal{A})$ is the set of *input operations*. The union of these two sets is the set of *operations* of the automaton. Finally, $steps(\mathcal{A})$ is the transition relation of \mathcal{A} , which is a set of triples of the form (s', π, s) , where s' and s are states, and π is an operation. This triple means that in state s' , the automaton can atomically do operation π and change to state s . An element of the transition relation is called a *step* of \mathcal{A} . If (s', π, s) is a step of \mathcal{A} , we say that π is *enabled* in s' .

The output operations are intended to model the actions that are triggered by the automaton itself, while the input operations model the actions that are triggered by the environment of the automaton. We require the following condition, which says that an I/O automaton must be prepared to receive any input operation at any time.

Input Condition: For each input operation π and each state s' , there exist a state s and a step (s', π, s) .

An *execution* of \mathcal{A} is a finite alternating sequence $s_0, \pi_1, s_1, \pi_2, \dots$ of states and operations of \mathcal{A} , ending with a state. Furthermore, s_0 is in $start(\mathcal{A})$, and each triple (s', π, s) which occurs as a consecutive subsequence is a step of \mathcal{A} . From any execution, we can extract the *schedule*, which is the subsequence of the execution consisting of operations only. Because transitions to different states may have the same operation, different executions may have the same schedule.

If S is any set of schedules (or property of schedules), then A is said to *preserve* S provided that the following holds. If $\alpha = \alpha'\pi$ is any schedule of A , where π is an output operation, and α' is in S , then α is in S . That is, the automaton is not the first to violate the property described by S .

2.2. Composition of Automata

We describe systems as consisting of interacting components, each of which is an I/O automaton. It is convenient and natural to view systems as I/O automata, also. Thus, we define a composition operation for I/O automata, to yield a new I/O automaton.

A set of I/O automata may be composed to create a *system* S , if the sets of output operations for the automata are disjoint. (Thus, every output operation in S will be triggered by exactly one component.) The system S is itself an I/O automaton. A state of the composed automaton is a tuple of states, one for each component, and the start states are tuples consisting of start states of the components. The set of *operations* of S , $ops(S)$, is exactly the union of the sets of operations of the component automata. The set of *output operations* of S , $out(S)$, is likewise the union of the sets of output operations of the component automata. Finally, the set of *input operations* of S , $in(S)$, is $ops(S) - out(S)$, the set of operations of S that are not output operations of S . The output operations of a system are intended to be exactly those that are triggered by components of the system, while the input operations of a system are those that are triggered by the system's environment.

The triple (s', π, s) is in the transition relation of S if and only if for each component automaton A , one of the following two conditions holds. Either π is an operation of A , and the projection of the step onto A is a step of A , or else π is not an operation of A , and the states corresponding to A in the two tuples s' and s are identical. Thus, each operation of the composed automaton is an operation of a subset of the component automata. During an operation π of S , each of the components which has operation π carries out the operation, while the remainder stay in the same state. Again, the operation π is an output operation of the composition if it is the output operation of a component — otherwise, π is an input operation of the composition.

An *execution* of a system is defined to be an execution of the automaton composed of the individual automata of the system. If α is a sequence of operations of a system S with component A , then we denote by $\alpha|A$ the subsequence of α containing all the operations of A . Clearly, if α is a schedule of S , $\alpha|A$ is a schedule of A .

The following lemma from [9] expresses formally the idea that an operation is under the control of the component of which it is an output.

Lemma 1: Let α' be a schedule of a system S , and let $\alpha = \alpha'\pi$, where π is an output operation of component A . If $\alpha|A$ is a schedule of A , then α is a schedule of S .

3. Generic Systems

In this section, we define "generic systems", which consist of transactions, generic objects, and a generic controller. They are a generalization of the "weak concurrent systems" of [9]. Transactions and generic objects describe user programs and data, respectively. The generic controller controls communication between the other components, and thereby defines the allowable orders in which the transactions may take steps. All three types of system components are modelled as I/O automata.

We begin by defining a structure which describes the nesting of transactions. Namely, a *system type* is a four-tuple $(\mathcal{T}, \text{parent}, \mathcal{O}, \mathcal{V})$, where \mathcal{T} , the set of transaction names, is organized into a tree by the mapping $\text{parent}: \mathcal{T} \rightarrow \mathcal{T}$, with T_0 as the root. In referring to this tree, we use traditional terminology, such as child, leaf, least common ancestor (lca), ancestor and descendant. (A transaction is its own ancestor and descendant.) The leaves of this tree are called *accesses*. The set \mathcal{O} denotes the set of objects; formally, \mathcal{O} is a partition of the set of accesses, where each element of the partition contains the accesses to a particular object. The set \mathcal{V} is a set of *values*, to be used as return values of transactions. The tree structure can be thought of as a predefined naming scheme for all possible transactions that might ever be invoked. In any particular execution, however, only some of these transactions will actually take steps. We imagine that the tree structure is known in advance by all components of a system. The tree will, in general, be an infinite structure.

The classical transactions of concurrency control theory (without nesting) appear in our model as the children of a "mythical" transaction, T_0 , the root of the transaction tree. It is very convenient to introduce the new root transaction to model the environment in which the rest of the transaction system runs. Transaction T_0 has operations that describe the invocation and return of the classical transactions. It is natural to reason about T_0 in much the same way as about all of the other transactions.

The internal nodes of the tree model transactions whose function is to create and manage subtransactions, but not to access data directly. The only transactions which actually access data are the leaves of the transaction tree, and thus they are distinguished as "accesses". The partition \mathcal{O} simply identifies those transactions which access the same object.

A generic system of a given system type is the composition of a set of I/O automata. This set contains a transaction for each *internal* (i.e. non-leaf, non-access) node of the transaction tree, a generic object for each element of \mathcal{O} and a generic controller. These automata are described below. (If X is a generic object associated with an element χ of the partition \mathcal{O} , and T is an access in χ , we write $T \in \text{accesses}(X)$ and say that " T is an access to X ".)

For the rest of this paper, we fix a particular system type $(\mathcal{T}, \text{parent}, \mathcal{O}, \mathcal{V})$.

3.1. Transactions

Transactions are modelled as I/O automata. In modelling transactions, we consider it very important not to constrain them unnecessarily; thus, we do not want to require that they be expressible as programs in any particular high-level programming language. Modelling the transactions as I/O automata allows us to state exactly the properties that are needed, without introducing unnecessary restrictions or complicated semantics.

A non-access transaction T is modelled as an I/O automaton, with the following operations:

Input operations:

CREATE(T)
 COMMIT(T',v), for $T' \in \text{children}(T)$ and $v \in V$
 ABORT(T'), for $T' \in \text{children}(T)$

Output operations:

REQUEST_CREATE(T'), for $T' \in \text{children}(T)$
 REQUEST_COMMIT(T,v), for $v \in V$

The CREATE input operation "wakes up" the transaction. The REQUEST_CREATE output operation is a request by T to create a particular child transaction.⁵ The COMMIT input operation reports to T the successful completion of one of its children, and returns a value recording the results of that child's execution. The ABORT input operation reports to T the unsuccessful completion of one of its children, without returning any other information. We call COMMIT(T',v), for any v , and ABORT(T') *return* operations for transaction T' . The REQUEST_COMMIT operation is an announcement by T that it has finished its work, and includes a value recording the results of that work.

It is convenient to use two separate operations, REQUEST_CREATE and CREATE, to describe what takes place when a subtransaction is activated. The REQUEST_CREATE is an operation of the transaction's parent, while the actual CREATE takes place at the subtransaction itself. In actual distributed systems such as Argus [8], this separation does occur, and the distinction will be important in our results and proofs. Similar remarks hold for the REQUEST_COMMIT and COMMIT operations.

We leave the executions of particular transaction automata largely unspecified; the choice of which children to create, and what value to return, will depend on the particular implementation. However, it is convenient to assume that schedules of transaction automata obey certain syntactic constraints. Thus, transaction automata are required to preserve well-formedness, as defined below.

⁵Note that there is no provision for T to pass information to its child in this request. In a programming language, T might be permitted to pass parameter values to a subtransaction. Although this may be a convenient descriptive aid, it is not necessary to include in it the underlying formal model. Instead, we consider transactions that have different input parameters to be different transactions.

We recursively define *well-formedness* for sequences of operations of transaction T. Namely, the empty schedule is well-formed. Also, if $\alpha = \alpha'\pi$ is a sequence of operations of T, where π is a single operation, then α is well-formed provided that α' is well-formed, and the following hold:

- If π is CREATE(T), then
 - (i) there is no CREATE(T) in α' .
- If π is COMMIT(T',v) or ABORT(T') for a child T' of T, then
 - (i) REQUEST_CREATE(T') appears in α' and
 - (ii) there is no return operation for T' in α' .
- If π is REQUEST_CREATE(T') for a child T' of T, then
 - (i) there is no REQUEST_CREATE(T') in α'
 - (ii) there is no REQUEST_COMMIT(T) in α' and
 - (iii) CREATE(T) appears in α' .
- If π is a REQUEST_COMMIT for T, then
 - (i) there is no REQUEST_COMMIT for T in α' and
 - (ii) CREATE(T) appears in α' .

These restrictions are very basic; they simply say that a transaction does not get created more than once, does not receive repeated notification of the fates of its children, does not receive conflicting information about the fates of its children, and does not receive information about the fate of any child whose creation it has not requested; also, a transaction does not perform any output operations before it has been created or after it has requested to commit, and does not request the creation of the same child more than once. Except for these minimal conditions, there are no restrictions on allowable transaction behavior. For example, the model allows a transaction to request to commit without discovering the fate of all subtransactions whose creation it has requested. Also, a transaction can request creation of new subtransactions at any time, without regard to its state of knowledge about subtransactions whose creation it has previously requested. Particular programming languages may choose to impose additional restrictions on transaction behavior. (An example is Argus, which suspends activity in transactions until subtransactions complete.) However, our results do not require such restrictions.

3.2. Generic Objects

Generic objects are similar to the abstract objects of Argus and other "object-oriented" systems. A generic object provides a set of "operations" (not to be confused with the operations of an I/O automaton) through which transactions can observe and change the object's state. For uniformity and ease of exposition, we model the "operations" as subtransactions, here called *access transactions*. Accesses can be invoked by concurrent transactions, and transactions can abort; thus, generic objects must provide synchronization and recovery sufficient to ensure serializability of the transactions using them. For example, the particular objects studied in [9], which use an exclusive locking variation of Moss's algorithm [12] for synchronization combined with version stacks for recovery, have been shown to

be correct for non-orphan transactions [9]. In section 3.5, we will discuss in more detail the various possible notions of correctness and what properties are ensured by the locking objects studied in [9].

In this section, we define the aspects of generic objects that are relevant to our analysis of orphan algorithms. It turns out that the details of how synchronization and recovery are implemented by a generic object are largely irrelevant. Indeed, this is one of the important contributions of this paper: we are able to state correctness conditions for and verify orphan elimination algorithms in a way that is completely independent of the concurrency control and recovery method used.

A generic object X is modelled as an I/O automaton, with the following operations:

Input Operations:

CREATE(T), T an access to X
 INFORM_COMMIT_AT(X)OF(T)
 INFORM_ABORT_AT(X)OF(T)

Output Operations:

REQUEST_COMMIT(T,v), T an access to X

The CREATE input operation starts an access transaction at the object. Similarly, the REQUEST_COMMIT output indicates that an access transaction has finished its work, and includes a value recording the results. The INFORM_COMMIT and INFORM_ABORT input operations tell X that some transaction (not necessarily an access to X) has committed or aborted, respectively.

As for transaction automata, we leave the executions of particular generic objects largely unspecified. However, we do assume, as for transactions, that schedules of generic objects obey certain syntactic constraints. Thus, generic objects are required to preserve well-formedness, defined recursively as follows: First, the empty schedule is well-formed. Second, if $\alpha = \alpha'\pi$ is a sequence of operations of X , then α is well-formed provided that α' is well-formed and the following hold:

- If π is CREATE(T), then
 - (i) there is no CREATE(T) in α' .
- If π is a REQUEST_COMMIT for T, then
 - (i) there is no REQUEST_COMMIT for T in α' , and
 - (ii) CREATE(T) occurs in α' .
- If π is INFORM_COMMIT_AT(X)OF(T), then
 - (i) there is no INFORM_ABORT_AT(X)OF(T) in α' , and
 - (ii) if T is an access to X, then a REQUEST_COMMIT for T occurs in α' .
- If π is INFORM_ABORT_AT(X)OF(T), then
 - (i) there is no INFORM_COMMIT_AT(X)OF(T) in α' .

These restrictions are again quite basic. They state that a given access is created at most once, and

requests to commit at most once, and then only if it has been created. In addition, an object should not be given conflicting information about the fate of a transaction, i.e., it should not be told both that a transaction committed and that it aborted. Finally, an object X should be told that an access to X has committed only if the access actually requested to commit.

3.3. Generic Controller

The third kind of component in a generic system is the generic controller. The generic controller is also modelled as an automaton. The transactions and generic objects have been specified to be any I/O automata whose operations and behavior satisfy simple syntactic restrictions. A generic controller, however, is a fully specified automaton, particular to each system type. (Recall that we have assumed that the system type is fixed; we describe the generic controller for the fixed system type.)

The generic controller has seven operations:

Input Operations:

REQUEST_CREATE(T),
REQUEST_COMMIT(T,v).

Output Operations:

CREATE(T),
COMMIT(T,v),
ABORT(T),
INFORM_COMMIT_AT(X)OF(T),
INFORM_ABORT_AT(X)OF(T).

The REQUEST_CREATE and REQUEST_COMMIT inputs are intended to be identified with the corresponding outputs of transaction and object automata, and correspondingly for the output operations.

Each state s of the generic controller consists of five sets: $create_requested(s)$, $created(s)$, $commit_requested(s)$, $committed(s)$, and $aborted(s)$. The set $commit_requested(s)$ is a set of (transaction,value) pairs, and the others are sets of transactions. The initial state of the generic controller is denoted by s_0 . All of the components of s_0 are empty except for $create_requested$, which is $\{T_0\}$. For a state s , we define $returned(s) = committed(s) \cup aborted(s)$.

The transition relation for the generic controller consists of exactly those triples (s',π,s) satisfying the pre- and postconditions below, where π is the indicated operation. For brevity, we include in the postconditions only those conditions on the state s which may change with the operation. If a component of s is not mentioned in the postcondition the component is taken to be the same in s as in s' .

- REQUEST_CREATE(T)

Postcondition:

$create_requested(s) = create_requested(s') \cup \{T\}$

- REQUEST_COMMIT(T,v)
Postcondition:
 $\text{commit_requested}(s) = \text{commit_requested}(s') \cup \{(T,v)\}$
- CREATE(T)
Precondition:
 $T \in \text{create_requested}(s') - \text{created}(s')$
Postcondition:
 $\text{created}(s) = \text{created}(s') \cup \{T\}$
- COMMIT(T,v)
Precondition:
 $(T,v) \in \text{commit_requested}(s')$
 $T \notin \text{returned}(s')$
 $\text{children}(T) \cap \text{create_requested}(s') \subseteq \text{returned}(s')$
Postcondition:
 $\text{committed}(s) = \text{committed}(s') \cup \{T\}$
- ABORT(T)
Precondition:
 $T \in \text{create-requested}(s') - \text{returned}(s')$
Postcondition:
 $\text{aborted}(s) = \text{aborted}(s') \cup \{T\}$
- INFORM_COMMIT_AT(X)OF(T):
Precondition:
 $T \in \text{committed}(s')$
- INFORM_ABORT_AT(X)OF(T):
Precondition:
 $T \in \text{aborted}(s')$

The controller assumes that its input operations, REQUEST_CREATE and REQUEST_COMMIT, can occur at any time, and simply records them in the appropriate components of the state. Once the creation of a transaction has been requested, the controller can create it by producing a CREATE operation. The precondition of CREATE indicates that a given transaction will be created at most once; the postcondition of CREATE records the fact that the creation has occurred. Similarly, the postconditions for COMMIT and ABORT record that the operation has occurred. INFORM_COMMIT and INFORM_ABORT operations can be generated at any time after the corresponding COMMIT and ABORT operations have occurred.

The precondition for the COMMIT operation ensures that a transaction only commits if it has requested to do so, and has not already returned (committed or aborted). In addition, the actual COMMIT operation must be delayed until all children requested by the committing transaction have returned. Recall from the well-formedness conditions described earlier that a transaction, once created, can request to commit at any time. However, once it has done so, it cannot request that any more children be

created.

The precondition for the ABORT operation ensures that a transaction will be aborted only if a REQUEST_CREATE has occurred for it and it has not already returned. There are no other constraints on when a transaction can be aborted, however. For example, a transaction can be aborted while some of its descendants are still running.

The generic controller presented here is a slight generalization of the "weak concurrent controller" in [9]. However, the results in [9] and their proofs are essentially unaffected by the generalization.)

The following lemma states some simple invariants relating schedules of the generic controller to the states that result from applying them to the initial state.

Lemma 2: Let α be a schedule of the generic controller, and let s be a state which can result from applying α to the initial state s_0 . Then the following conditions are true.

1. T is in $\text{create_requested}(s)$ exactly if α contains a REQUEST_CREATE(T) operation.
2. T is in $\text{created}(s)$ exactly if α contains a CREATE(T) operation.
3. (T,v) is in $\text{commit_requested}(s)$ exactly if α contains a REQUEST_COMMIT(T,v) operation.
4. T is in $\text{committed}(s)$ exactly if α contains a COMMIT operation for T .
5. T is in $\text{aborted}(s)$ exactly if α contains an ABORT(T) operation.
6. $\text{aborted}(s) \cap \text{committed}(s) = \emptyset$

Proof: Straightforward. \square

3.4. Generic Systems

The composition of transactions with generic objects and the generic controller is called a *generic system* (of the given system type). The non-access transactions and generic objects are called the *system primitives*. The schedules of a generic system are called *generic schedules*.

Define the *generic operations* to be those operations that occur in the generic system. REQUEST_CREATE, REQUEST_COMMITS, CREATES, COMMITS, ABORTS, INFORM_COMMITS and INFORM_ABORTS. For any generic operation π , we define $\text{location}(\pi)$ to be the primitive at which π occurs.

A sequence of generic operations is called *well-formed* provided that its projection on each generic primitive (transaction and generic object) is well-formed.

Lemma 3: Every generic schedule is well-formed.

Proof: By induction on the length of schedules. The basis, when the length of α is 0, is trivial. Suppose that $\alpha\pi$ is a generic schedule, where π is a single operation, and assume that α is well-formed. It suffices to show that $\alpha\pi|P$ is well-formed for all generic primitives P . Let P be any fixed generic primitive. If π is not an operation of P , the result is immediate, so assume that π is an operation of P . We consider cases.

1. π is an output of P

Since generic primitives preserve well-formedness, the result is immediate.

2. π is CREATE(T)

The generic controller preconditions and Lemma 2 imply that no CREATE(T) appears in α .

3. π is COMMIT(T, v)

Then π is an input to the transaction parent(T). The generic controller preconditions and Lemma 2 imply that REQUEST_COMMIT(T, v) occurs in α . The well-formedness of α implies that CREATE(T) occurs in α . The generic controller preconditions and Lemma 2 imply that REQUEST_CREATE(T) occurs in α . Also, the generic controller preconditions and Lemma 2 ensure that α does not contain a return operation for T .

4. π is ABORT(T)

Then π is an input to the transaction parent(T). The generic controller preconditions and Lemma 2 imply that REQUEST_CREATE(T) occurs in α , and also imply that no return operation for T occurs in α .

5. π is INFORM_COMMIT_AT(X)OF(T)

By the generic controller preconditions and Lemma 2, there is no INFORM_ABORT_AT(X)OF(T) in α , and there is a COMMIT operation for T in α . Again by the generic controller preconditions and Lemma 2, a REQUEST_COMMIT for T occurs in α . If T is an access to X , this operation occurs at X .

6. π is INFORM_ABORT_AT(X)OF(T)

By the generic controller preconditions and Lemma 2, there is no INFORM_COMMIT_AT(X)OF(T) in α .

□

3.5. Correctness

In much of the database literature on transactions, serializability is taken as the definition of correctness. To deal with nested transactions, and to handle aborts, the usual notion of serializability must be generalized. This is done in [9] as follows.

The idea is that a generic system is correct if every schedule of the generic system "looks like" a serial schedule to each transaction. The permissible serial schedules are defined by another kind of system, called a "serial system". Serial systems are similar to generic systems in that they are composed of transactions, a serial controller, and objects. The transactions are identical to those in generic systems. The serial controller, however, differs from the generic controller in two respects. First, the serial

controller permits only one child of a transaction to run at a time. Thus, sibling transactions execute sequentially at every level in the transaction tree. Second, the serial controller aborts a transaction only if it has not yet been created, and creates a transaction only if it has not been aborted. In other words, aborted transactions never take any steps in a serial schedule.

Objects in a serial system are simpler than generic objects. Since the serial controller guarantees that siblings execute sequentially, and that aborted transactions never take any steps, serial objects do not have to deal with concurrency or with failures. The serial objects serve as a specification of how objects should behave in the absence of concurrency and failures. (The serial objects in [9] serve the same purpose as the "serial specifications" in [20].)

Serial schedules capture the notion that an aborted transaction has no effect, and that siblings execute sequentially. Thus, they serve as the basis against which correctness is defined for more complicated systems, such as generic systems.

Many possible notions of correctness can be defined. We consider two here. The first is quite simple: it requires that every schedule look like a serial schedule to every transaction. More precisely, if α is a generic schedule and T is a non-access transaction, we say that α is *serially correct at T* if there exists a serial schedule β such that $\beta|T = \alpha|T$. In other words, T sees the same thing in α that it could see in some serial schedule. We say that α is *serially correct* if it is serially correct for all non-access transactions.⁶ We also say that a system is serially correct if every schedule of the system is serially correct.

Requiring every transaction to see a serial view is a strong requirement. Without orphan elimination, in fact, most systems do not meet this requirement. Instead, they provide a slightly weaker notion of correctness, namely that non-orphan transactions see serial views. More precisely, if α is a sequence of generic operations and T is a transaction, we say that T is an *orphan* in α if $\text{ABORT}(T')$ occurs in α for some ancestor T' of T . Systems without orphan elimination ensure that each schedule is serially correct for all non-orphan transactions; orphan transactions, however, can see arbitrary views.

As mentioned above, one example of a generic object is the combination of a "resilient object" and corresponding "lock manager", as defined in [9]. The resilient object handles recovery processing, in particular, the processing of information about the fate (commit or abort) of each transaction. The lock manager implements an exclusive locking protocol based on that of Moss [12]. The combination can be encapsulated in a "black box" called a generic object, which handles both concurrency control and

⁶As discussed in [9], this definition of correctness allows different transactions in α to "see" different serial schedules. However, correctness applies to the root transaction as well, so the root must see the same results from the top-level transactions in a generic schedule that it could see in some serial schedule.

recovery.⁷ In this paper, we call the combination of a resilient object and a lock manager a *locking object*. We call a generic system built using locking objects a *locking system*. (Such a system is called a "weak concurrent system" in [9].) We call schedules of a locking system *locking schedules*.

One of the main results proved in [9] is that locking schedules are serially correct for non-orphan transaction primitives:

Theorem 4: Let α be a locking schedule and let T be a non-access transaction that is not an orphan in α . Then α is serially correct at T .

To ensure that every transaction sees a serial view, the orphan elimination algorithms described in the remainder of this paper rely on the generic objects to ensure that non-orphans see serial views. However, as we will describe in more detail later, it is not necessary to use a particular kind of generic object, such as the locking objects from [9]. Instead, we will show that the orphan elimination algorithms work with any objects that ensure serial correctness for non-orphans. In other words, the orphan elimination algorithms and the concurrency control algorithms are essentially independent. We prove a result of the following sort for each orphan elimination algorithm: if α is a schedule of the system with orphan elimination and T is a transaction, then there exists a generic schedule β such that $\beta|T = \alpha|T$ and T is not an orphan in β . In other words, the orphan elimination algorithms prevent transactions from "knowing" that they are orphans — everything a transaction sees is consistent with what it could see in some execution in which it is not an orphan. This result can be combined, for example, with a result such as Theorem 4 to show that all transactions obtain serial views in a system with orphan elimination and locking objects. We will make these ideas more precise later in the paper.

This modularity has important advantages in building systems. Objects can be constructed to ensure serial correctness for non-orphans, without worrying about orphans at all. For example, it is shown in [3] that objects that use read-write locking (as opposed to exclusive locking as used in the locking objects of [9]) ensure serial correctness for non-orphans. We are also currently working on generalizing the results in [20] to nested transaction systems. This will permit us to show that many other kinds of objects ensure serial correctness, including objects that use timestamps for concurrency control [16], and objects that use more general approaches to locking [5, 17, 20]. The results in this paper indicate that the orphan elimination algorithms analyzed here can be combined with any of these objects.

⁷The only difference is that the CREATE input operation has another name in [9].

4. Information Flow

The orphan elimination algorithms analyzed in this paper use quite different techniques to detect and eliminate orphans. However, the fundamental underlying structure is quite similar. In this section we define a notion of a "dependency relation" that models the information flow among operations. These definitions allow us to analyze both orphan elimination algorithms in a simple and straightforward manner.

For a sequence α of generic operations, define the relation *directly-affects*(α) to be the relation containing the pairs (ϕ, π) of operation instances⁸ such that ϕ occurs before π in α , and at least one of the following holds:

- $\text{location}(\phi) = \text{location}(\pi)$, and π is an output operation
- $\phi = \text{REQUEST_CREATE}(T)$ and $\pi = \text{CREATE}(T)$
- $\phi = \text{REQUEST_COMMIT}(T, v)$ and $\pi = \text{COMMIT}(T)$
- ϕ is a return operation for a child of T and $\pi = \text{COMMIT}(T)$
- $\phi = \text{REQUEST_CREATE}(T)$ and $\pi = \text{ABORT}(T)$
- $\phi = \text{COMMIT}(T)$ and $\pi = \text{INFORM_COMMIT_AT}(X)\text{OF}(T)$
- $\phi = \text{ABORT}(T)$ and $\pi = \text{INFORM_ABORT_AT}(X)\text{OF}(T)$

Define the relation *affects*(α) to be the transitive closure of *directly-affects*(α). If the pair (ϕ, π) is in the relation *directly-affects*(α), we say that ϕ *directly-affects* π in α . Similarly, if (ϕ, π) is in the relation *affects*(α), we say that ϕ *affects* π in α .

The idea is that ϕ directly-affects π if they both occur at the same primitive (and π is an output, since inputs can always occur), or if they involve different primitives but the preconditions for the controller require ϕ to occur before π can occur. This notion of one operation affecting another is "safe," in the sense that ϕ affects π if there is any way that the precondition for π could require ϕ to have occurred. If the operations involve different primitives, the preconditions for π do require ϕ to occur if ϕ directly-affects π . If the operations occur at the same primitive, however, it might be ϕ happens to occur before π , yet that the particular primitive does not require ϕ to occur before π . In the absence of more information about the particular primitives used in a system, however, it is difficult to say more about the ways in which one operation can affect another. Fortunately, the orphan elimination algorithms

⁸Formally, an *operation instance* is a pair (i, π) , where i is a positive integer and π is an operation. An operation instance (i, π) is said to *occur* in α if the i -th element of α is π . To avoid introducing excessive and confusing notation, we will not be overly formal in distinguishing operations from operation instances. For example, we will write that an operation instance is `CREATE(T)` meaning formally that its second component is `CREATE(T)`.

described later in this paper are essentially independent of the particular primitives used in a system, and do not rely on more information about the particular primitives in the system.

The following lemmas follow directly from the definitions:

Lemma 5: Let α be a sequence of generic operations. If ϕ affects π in α , then there exists a $\psi \neq \pi$ such that ψ directly-affects π in α , and either $\psi = \phi$ or ϕ affects ψ in α .

Lemma 6: Let α be a sequence of generic operations. If ϕ affects π in α , α' is a prefix of α , and ϕ and π both occur in α' , then ϕ affects π in α' .

If α is a sequence of generic operations and β is a subsequence of α , we say that β is closed in α if, whenever β contains an operation instance π in α , it also contains any ϕ that affects π in α . The following lemma is immediate from the definitions:

Lemma 7: Let α be a sequence of generic operations, and let β be a closed subsequence of α . If β' is a prefix of β , then β' is closed in α .

The following lemma states that $\text{affects}(\alpha)$ contains all dependencies that are relevant to the execution of a generic system.

Lemma 8: If α is a generic schedule, then any closed subsequence of α is also a generic schedule.

Proof: Fix α . We proceed by induction on the length of subsequences β of α , to show that, if β is closed in α , then β is a generic schedule. The basis, when the length of β is 0, is trivial. For the inductive step, assume that β is a closed subsequence of α of length at least 1. Then let $\beta = \beta'\pi$, where π is a single operation. Let α' be the prefix of α preceding π . By Lemma 7, β' is closed in α . Thus, the inductive hypothesis implies that β' is a generic schedule. We consider cases.

1. π is an output operation of a primitive P

Since β is closed in α , it follows from the definition of $\text{affects}(\alpha)$ that β contains all operations of P that precede π in α . Thus, $\beta|P$ is a prefix of $\alpha|P$, and since $\alpha|P$ is a schedule of P, it must be that $\beta|P$ is also a schedule of P. Then β is a generic schedule, by Lemma 1.

2. $\pi = \text{CREATE}(T)$

Then Lemma 2 and the controller preconditions imply that $\text{REQUEST_CREATE}(T)$ occurs in α' , and no $\text{CREATE}(T)$ occurs in α' . Since β is closed in α , $\text{REQUEST_CREATE}(T)$ also occurs in β' . Since no $\text{CREATE}(T)$ occurs in β' , Lemma 2 implies that π is enabled in the (unique) generic controller state resulting from β' . Thus, β is a schedule of the generic controller, so Lemma 1 implies that β is a generic schedule.

3. $\pi = \text{COMMIT}(T,v)$

Then Lemma 2 and the controller preconditions imply that α' contains $\text{REQUEST_COMMIT}(T,v)$ and contains no return operations for T. In addition, α' contains a return operation for each child T' of T for which $\text{REQUEST_CREATE}(T')$ appears in α' . Since β is closed in α , β contains these operations (by the definition of directly-affects); thus, so does β' . Since no return operations for T occur in β' , Lemma 2 implies that π is enabled after β' , so β is a generic schedule.

4. $\pi = \text{ABORT}(T)$

Then α' contains $\text{REQUEST_CREATE}(T)$ and contains no return operations for T . Since β is closed in α , β' also contains $\text{REQUEST_CREATE}(T)$. Since no return operations for T occur in β' , π is enabled after β' , so β is a generic schedule.

5. $\pi = \text{INFORM_COMMIT_AT}(X)\text{OF}(T)$

Then α' contains a COMMIT operation for T . Since β is closed in α , so does β' . Thus, π is enabled after β' , so β is a generic schedule.

6. $\pi = \text{INFORM_ABORT_AT}(X)\text{OF}(T)$

Then α' contains an ABORT operation for T . Since β is closed in α , so does β' . Thus, π is enabled after β' , so β is a generic schedule.

□

This lemma shows that the relation $\text{affects}(\alpha)$ captures all ways in which one operation can depend on another. If π is not affected by ϕ in some schedule α , then π cannot "know" that ϕ occurred, since π could also have occurred in a different schedule in which ϕ did not occur.

The intuitive idea behind the orphan elimination algorithms is that they ensure that an operation of a transaction T is never affected by the abort of an ancestor. Once we have shown this, Lemma 8 allows us to show that every transaction gets a view it could get in an schedule in which it is not an orphan: we simply take the subsequence of the schedule containing all operations of T and all operations that affect them. The resulting sequence is a generic schedule, by Lemma 8, and does not contain an abort for an ancestor of T , by construction.

5. Filtered Systems

One way of ensuring that operations of a transaction T are never affected by the abort of an ancestor of T is to add preconditions to the generic controller to permit operations of T to occur only if they would not be affected in this way. It turns out, however, that this approach checks for orphans much more frequently than necessary. In this section we define another kind of system, called a "filtered system", that checks for orphans only when access transactions commit. We then show that this is sufficient to ensure that transactions are never affected by the aborts of ancestors.

Filtered systems consist of transactions, generic objects, and a "filtered controller". The filtered controller is obtained by slightly modifying a generic controller; it "filters" commits of access transactions so that any non-access transaction, orphan or not, sees a view it could see as a non-orphan in the generic system.

5.1. The Filtered Controller

The filtered controller is the same as the generic controller, except that it permits an access to commit only if it is not affected by the abort of an ancestor.

The filtered controller has the same seven operations as the generic controller. Each state s of the filtered controller consists of six components. The first five are the same as for the generic controller (i.e., $\text{create_requested}(s)$, $\text{created}(s)$, $\text{commit_requested}(s)$, $\text{committed}(s)$, and $\text{aborted}(s)$). The sixth, $\text{history}(s)$, is a sequence of generic operations. The initial state of the filtered controller is denoted by s_0 . As in the generic controller, all sets are empty in s_0 except for create_requested , which is $\{T_0\}$. $\text{History}(s_0)$ is the empty sequence. As before, we define $\text{returned}(s) = \text{committed}(s) \cup \text{aborted}(s)$.

The transition relations for all operations except $\text{COMMIT}(T,v)$, where T is an access, are defined as for the generic controller, except that each operation π has an additional postcondition of the form $\text{history}(s) = \text{history}(s')\pi$. In other words, the history component of the state simply records the sequence of operations that have occurred. The transition relation for the $\text{COMMIT}(T,v)$ operation, where T is an access, is defined as follows.

- $\text{COMMIT}(T,v)$, T an access

Precondition:

$(T,v) \in \text{commit_requested}(s')$
 $T \notin \text{returned}(s')$
 if T' is an ancestor of T ,
 then $\text{ABORT}(T')$ does not affect $\text{COMMIT}(T,v)$ in $\text{history}(s')\text{COMMIT}(T,v)$

Postcondition:

$\text{committed}(s) = \text{committed}(s') \cup \{T\}$
 $\text{history}(s) = \text{history}(s')\text{COMMIT}(T,v)$

Thus, at the point where an access is about to commit to its parent, an explicit test is performed to verify that the new COMMIT operation is not affected (in our formal sense) by the abort of any ancestor of the access.

5.2. Filtered Systems

A *filtered system* is the composition of transactions, generic objects and the filtered controller. Schedules of a filtered system are called *filtered schedules*.

Lemma 9: Every filtered schedule is a generic schedule.

Proof: First we note that if α is both a filtered schedule and a generic schedule, if s_F is the (uniquely defined) state of the filtered controller after α and s_G is the (uniquely defined) state of the generic schedule after α , then s_G is the same as s_F except for the omission of the history component. This is easily seen by induction on the length of α .

Now we show the result by induction on the length of filtered schedules. The basis, length 0, is trivial. Let $\alpha = \alpha'\pi$ be a filtered schedule of length at least 1, where π is a single operation. If π is an output of a transaction or generic object P, then $\alpha|P$ is a schedule of P, and so the inductive hypothesis and Lemma 1 imply that α is a generic schedule. So assume that π is an output of the filtered controller. Let s_F be the state of the filtered controller after α' , and let s_G be the state of the generic controller after α' . By the inductive hypothesis and the claim above, s_G is the same as s_F except for the deletion of the history component. Since π is enabled in s_F for the filtered controller, it is also enabled in s_G for the generic controller. Thus, α is a schedule of the generic controller, and hence, by Lemma 1, is a generic schedule. \square

As described above, the filtered controller performs an explicit test to ensure that the commit of an access is not affected by the abort of any ancestor. The following key lemma shows that this test actually guarantees more: that a similar property holds for all operations occurring at non-access transactions.

Lemma 10: Let α be a filtered schedule, and let T be a non-access transaction. Let π be an operation in α , such that $\text{location}(\pi) = T$. Then there is no $\text{ABORT}(T')$ operation that affects π in α , for any ancestor T' of T.

Proof: First note that Lemmas 9 and 3 imply that α is well-formed; we will use this fact in the proof of the lemma. The proof is by induction on the length of α . If α is empty, the result clearly holds. Suppose $\alpha = \alpha'\pi$, and that the lemma holds for α' . Obviously, $\text{affects}(\alpha) \subseteq \text{affects}(\alpha') \cup \{(\phi, \pi) \mid \phi \text{ is an operation in } \alpha'\}$. Thus, it suffices to show that the single operation π is not affected, in α , by the abort of an ancestor. So assume the contrary, that $\phi = \text{ABORT}(T')$ affects π in α , for some ancestor T' of T.

By Lemma 5, there exists a $\psi \neq \pi$ such that ψ directly-affects π in α , and either $\psi = \phi$ or ϕ affects ψ in α . Since $\psi \neq \pi$, ϕ and ψ must occur in α' . Thus, by Lemma 6, if $\phi \neq \psi$, ϕ affects ψ in α' .

Notice that $\text{location}(\phi) = \text{parent}(T')$; since T' is an ancestor of T, $\text{parent}(T') \neq T$. Thus, $\text{location}(\phi) \neq T$.

We consider cases.

1. π is an output operation of T.
Then by the definition of directly-affects(α), $\text{location}(\psi) = T$. Since $\text{location}(\phi) \neq T$, $\phi \neq \psi$. Thus, ϕ affects ψ in α' . But this contradicts the inductive hypothesis.
2. π is $\text{CREATE}(T)$.
Then by the definition of directly-affects(α), $\psi = \text{REQUEST_CREATE}(T)$. Thus, $\phi \neq \psi$, so ϕ affects ψ in α' . Since $\text{REQUEST_CREATE}(T)$ is an operation of $\text{parent}(T)$, the inductive hypothesis implies that T' is not an ancestor of $\text{parent}(T)$. The only possibility is that $T' = T$, which implies that $\text{ABORT}(T)$ precedes $\text{REQUEST_CREATE}(T)$ in α . But this implies that $\alpha|T$ is not well-formed, a contradiction.
3. π is $\text{COMMIT}(T'', v)$, where T'' is a child of T and T'' is an access.
Then the precondition for $\text{COMMIT}(T'', v)$ in the filtered controller is violated, a contradiction.

4. π is $\text{COMMIT}(T'',v)$, where T'' is a child of T and T'' is a non-access transaction. Then T' is an ancestor of T'' , and by the definition of $\text{directly-affects}(\alpha)$, ψ is either $\text{REQUEST_COMMIT}(T'',v)$ or a return operation for a child of T'' . Thus, $\phi \neq \psi$, so ϕ affects ψ in α' . But this contradicts the inductive hypothesis.
5. π is $\text{ABORT}(T'')$, where T'' is a child of T . Then by the definition of $\text{directly-affects}(\alpha)$, $\psi = \text{REQUEST_CREATE}(T'')$. Thus, $\phi \neq \psi$, so ϕ affects ψ in α' . Again, this contradicts the inductive hypothesis.

□

5.3. Simulation of Generic Systems by Filtered Systems

The following theorem is the key result of the paper. It shows that filtered systems ensure that every transaction gets a view it could get when it is not an orphan. In other words, an orphan cannot discover that it is an orphan, since the view it sees is consistent with it not being an orphan. This is the basic correctness property for the orphan elimination algorithms.

Theorem 11: Let α be a filtered schedule and let T be a non-access transaction. Then there exists a generic schedule β such that T is not an orphan in β and $\beta|T = \alpha|T$.

Proof: Let β be the subsequence of α containing all operations π such that $\text{location}(\pi) = T$, and all other operations ϕ that affect, in α , some operation whose location is T . By Lemma 8, β is a generic schedule. It suffices to show that there is no ancestor T' of T for which $\text{ABORT}(T')$ occurs in β . Suppose not; i.e., there exists an ancestor T' of T for which $\text{ABORT}(T')$ occurs in β . Then by the construction of β , α contains an operation π of T such that $\text{ABORT}(T')$ affects π in α . By Lemma 10, this is impossible. □

As discussed earlier, we can combine Theorem 11 with Theorem 4 to obtain an important corollary. Define a *filtered locking system* to be a filtered system whose generic objects are locking objects; its schedules are called *filtered locking schedules*.

Corollary 12: Any filtered locking system is serially correct.

Proof: Let α be a filtered locking schedule and let T be a non-access transaction. Theorem 11 yields a locking schedule γ such that T is not an orphan in γ and $\gamma|T = \alpha|T$. Theorem 4 then yields a serial schedule β with $\beta|T = \gamma|T$; this is equal to $\alpha|T$, as needed. □

A similar corollary can be obtained for any generic system whose transactions and objects ensure serial correctness for non-orphans. Namely, let S be a generic system whose schedules are serially correct non-orphan non-access transactions. Define $\text{filter}(S)$ to be the system obtained from S by replacing the generic controller in S with the filtered controller. Then Theorem 11 implies that $\text{filter}(S)$ is serially correct.

At first it might seem somewhat surprising that it is enough to prevent the commits of orphaned accesses to ensure serial correctness for all orphans. It is not necessary to filter operations of other transactions because of the restricted communication patterns among the primitives in a system. The execution of a transaction primitive T can be affected by an ancestor only through the $\text{CREATE}(T)$

operation, or through communication via shared objects. As long as T does not access any objects that "know" that its ancestor has aborted, T cannot observe a state that depends on the abort. In effect, by preventing the commits of orphaned accesses, we isolate orphaned transactions from the objects, ensuring that an orphaned transaction never sees that it is an orphan.

6. Argus Systems

In this section we analyze the orphan elimination algorithm used in the Argus system [6, 7]. We describe the algorithm by defining an *Argus controller* that describes in formal terms the algorithm discussed in [7]. We then define Argus systems, which are composed of transactions, generic objects, and an Argus controller, and show that Argus systems "simulate" filtered systems. In other words, a schedule of an Argus system looks like a schedule of a filtered system to each non-access transaction; since filtered systems are serially correct, so are Argus systems.

6.1. The Argus Controller

The filtered controller uses global knowledge of the entire history of operations to filter the commits of access transactions. This kind of global knowledge is not practical in a distributed system. Thus, the Argus algorithm makes use of local knowledge about the aborts that have occurred. To ensure that the commit of an access is not affected by the abort of an ancestor, the Argus algorithm keeps track of the aborts "known" by each operation that occurs, and propagates this knowledge from an operation to any later operations that it affects.

The Argus controller has the same seven operations as the generic controller. Each state s of the Argus controller consists of six components. The first five are the same as for the generic controller (i.e., $create_requested(s)$, $created(s)$, $commit_requested(s)$, $committed(s)$, and $aborted(s)$). The sixth, $done(s)$, is a mapping from operations⁹ to sets of transactions. As before, the initial state is denoted by s_0 , and all sets are initially empty in s_0 except for $create_requested$, which is $\{T_0\}$. $Done(s_0)$ maps each operation to the empty set. As before, we define $returned(s) = committed(s) \cup aborted(s)$.

The transition relations for the operations of the Argus controller are defined as follows. (Note: The postcondition for each operation π specifies the value of $done(s)(\pi)$, but not of $done(s)(\phi)$ for any other operation ϕ ; our intent is that $done(s)(\phi) = done(s')(\phi)$.)

- REQUEST_CREATE(T)
Postcondition:
 $create_requested(s) = create_requested(s') \cup \{T\}$

⁹Note that the domain of $done(s)$ is the set of operations, not the set of operation instances. We could have used the set of instances instead, obtaining a slightly modified algorithm and proof. Using the set of operations, however, seems to result in a simpler and cleaner description of the algorithm.

for all π such that $\text{location}(\pi) = \text{parent}(T)$,
 $\text{done}(s')(\pi) \subseteq \text{done}(s)(\text{REQUEST_CREATE}(T))$

- **REQUEST_COMMIT(T,v)**
 Postcondition:
 $\text{commit_requested}(s) = \text{commit_requested}(s') \cup \{(T,v)\}$
 for all π such that $\text{location}(\pi) = \text{location}(\text{REQUEST_COMMIT}(T,v))$,
 $\text{done}(s')(\pi) \subseteq \text{done}(s)(\text{REQUEST_COMMIT}(T,v))$
- **CREATE(T)**
 Precondition:
 $T \in \text{create_requested}(s') - \text{created}(s')$
 Postcondition:
 $\text{created}(s) = \text{created}(s') \cup \{T\}$
 $\text{done}(s')(\text{REQUEST_CREATE}(T)) \subseteq \text{done}(s)$
- **COMMIT(T,v), T a non-access**
 Precondition:
 $(T,v) \in \text{commit_requested}(s')$
 $T \notin \text{returned}(s')$
 $\text{children}(T) \cap \text{create_requested}(s') \subseteq \text{returned}(s')$
 Postcondition:
 $\text{committed}(s) = \text{committed}(s') \cup \{T\}$
 for all π such that $\pi = \text{REQUEST_COMMIT}(T,v)$ or π is the return of a child of T
 $\text{done}(s')(\pi) \subseteq \text{done}(s)(\text{COMMIT}(T,v))$
- **COMMIT(T,v), T an access**
 Precondition:
 $(T,v) \in \text{commit_requested}(s')$
 $T \notin \text{returned}(s')$
 there is no ancestor of T in $\text{done}(s')(\text{REQUEST_COMMIT}(T,v))$
 Postcondition:
 $\text{committed}(s) = \text{committed}(s') \cup \{T\}$
 $\text{done}(s')(\text{REQUEST_COMMIT}(T,v)) \subseteq \text{done}(s)(\text{COMMIT}(T,v))$
- **ABORT(T)**
 Precondition:
 $T \in \text{create_requested}(s') - \text{returned}(s')$
 Postcondition:
 $\text{aborted}(s) = \text{aborted}(s') \cup \{T\}$
 $\text{done}(s')(\text{REQUEST_CREATE}(T)) \cup \{T\} \subseteq \text{done}(s)(\text{ABORT}(T))$
- **INFORM_COMMIT_AT(X)OF(T):**
 Precondition:
 $T \in \text{committed}(s')$
 Postcondition:
 for all v, $\text{done}(s')(\text{COMMIT}(T,v)) \subseteq \text{done}(s)(\text{INFORM_COMMIT_AT}(X)\text{OF}(T))$
- **INFORM_ABORT_AT(X)OF(T):**
 Precondition:
 $T \in \text{aborted}(s')$
 Postcondition:

$$\text{done}(s')(\text{ABORT}(T)) \subseteq \text{done}(s)(\text{INFORM_ABORT_AT}(X)\text{OF}(T))$$

There are two differences between the Argus controller and the generic controller. First, the postconditions for each operation π in the Argus controller require $\text{done}(s)(\pi)$ to include $\text{done}(s')(\phi)$ for each ϕ that directly-affects π .¹⁰ In addition, the postcondition for $\text{ABORT}(T)$ requires T to be in $\text{done}(s)(\text{ABORT}(T))$. As Lemma 14 below shows, these constraints are enough to ensure that $\text{done}(s)(\pi)$ contains T whenever $\text{ABORT}(T)$ affects an instance of π .

Second, the precondition for the commit of an access permits the commit to occur only if the access does not "know about" the abort of an ancestor, i.e., no ancestor is in $\text{done}(s')(\text{REQUEST_COMMIT}(T,v))$. As Lemma 15 below shows, this is enough to ensure that every Argus schedule is a filtered schedule.

$\text{Done}(s)$ models the distributed information maintained by the Argus algorithm to keep track of actions that abort. However, rather than modelling nodes directly and keeping the information on a per-node basis as is done in the actual algorithm, we maintain the information for each operation, propagating it whenever one operation directly-affects another. The rules in the postconditions above for propagating done from one operation to another follow directly the rules used by the actual Argus algorithm.

Notice that the controller postconditions require a minimum amount of information to be propagated at each step, i.e., the postcondition for an operation π requires certain entries to appear in $\text{done}(s)(\pi)$. The postconditions are stated to be quite non-deterministic, so that an implementation could propagate more than the minimum required, perhaps by keeping track of done at a coarser granularity. In fact, the implementation of the Argus algorithm in the current Argus prototype maintains done on a per-node basis, so that much more information is propagated than is required by the formal description of the algorithm above. In describing the algorithm, we have tried to focus on the behavior necessary for correctness, and to avoid constraining an implementation any more than necessary.

Notice also that the controller does not put any limit on what goes into done. For example, as described above it is permissible for $\text{done}(s)(\pi)$ to contain a transaction that has not aborted. It would be easy to add a requirement that $\text{done}(s)(\pi) \subseteq \text{aborted}(s)$, but this is not necessary to prove that the algorithm eliminates all orphans. To prove other properties, such as that the algorithm only detects and eliminates real orphans, we would need to add additional requirements such as the one just mentioned. We will not attempt to state or prove such properties in this paper; the property just described is a special case of more general liveness properties, which are the subject of current research.

¹⁰The postcondition for the INFORM_COMMIT operation may be a little confusing. Since the value returned in the COMMIT operation is not part of the INFORM_COMMIT , the postcondition requires $\text{done}(s')(\text{COMMIT}(T,v))$ to be included for all $v \in V$. For a given T , however, only one $\text{COMMIT}(T,v)$ will occur, so $\text{done}(s')(\text{COMMIT}(T,v))$ will be empty for all but one v .

6.2. Argus Systems

An *Argus system* is the composition of transactions, generic objects, and the Argus controller. Schedules of the Argus system are called *Argus schedules*.

Lemma 13: Every Argus schedule is a generic schedule.

Proof: The proof is similar to that of Lemma 9. \square

The following lemma states the basic invariant about the information in $\text{done}(s)$:

Lemma 14: Let α be an Argus schedule, let s be a state of the Argus controller after α , and let ψ be an operation instance in α . If $\psi = \text{ABORT}(T)$ or there exists a $\phi = \text{ABORT}(T)$ such that ϕ affects ψ in α , then $T \in \text{done}(s)(\psi)$.

Proof: The proof proceeds by induction on the length of α . If α is of length 0, there is nothing to prove. So suppose $\alpha = \alpha'\pi$, where π is a single operation. Let s' be a state of the Argus controller after α' such that (s', π, s) is an element of the transition relation for the Argus controller.

There are two cases: either ψ appears in α' , or ψ and π are the same operation instance. First, suppose ψ appears in α' . If π and ψ are instances of different operations, the result follows immediately from the inductive hypothesis and the fact that $\text{done}(s)(\rho) = \text{done}(s')(\rho)$ for any $\rho \neq \pi$. Otherwise, π and ψ must be different instances of the same operation. By Lemmas 13 and 3, α is a generic schedule and is well-formed. The well-formedness conditions described earlier and the definition of the generic controller imply that the only operations that can occur more than once in a generic schedule are of the form $\text{INFORM_COMMIT_AT}(X)\text{OF}(T')$ or $\text{INFORM_ABORT_AT}(X)\text{OF}(T')$ for some X and T' . We consider these two cases:

1. If ψ and π are both of the form $\text{INFORM_COMMIT_AT}(X)\text{OF}(T')$ (for the same X and T'), then by Lemma 5 and the definition of $\text{directly-affects}(\alpha)$, there must be a $\text{COMMIT}(T', v)$ in α' such that ϕ affects $\text{COMMIT}(T', v)$ in α' . Then the inductive hypothesis implies that $T \in \text{done}(s')(\text{COMMIT}(T', v))$. The postcondition for π implies that $T \in \text{done}(s)(\pi)$, which is equal to $\text{done}(s)(\psi)$.
2. If ψ and π are both of the form $\text{INFORM_ABORT_AT}(X)\text{OF}(T')$ (for the same X and T'), then by Lemma 5 and the definition of $\text{directly-affects}(\alpha)$, either $T = T'$ or there is an $\text{ABORT}(T')$ in α' such that ϕ affects $\text{ABORT}(T')$ in α' . In either case, the inductive hypothesis implies that $T \in \text{done}(s')(\text{ABORT}(T'))$. The postcondition for π implies that $T \in \text{done}(s)(\pi)$, which is equal to $\text{done}(s)(\psi)$.

Second, π and ψ can be the same operation instance. We consider cases:

1. π is an output of a primitive P .
Then $\pi \neq \text{ABORT}(T)$, so assume $\phi = \text{ABORT}(T)$ affects π in α . There are two possibilities, depending on whether or not $P = \text{parent}(T)$. If $P = \text{parent}(T)$, then $P = \text{location}(\phi)$. The inductive hypothesis implies that $T \in \text{done}(s')(\phi)$. Then the postconditions for the REQUEST_CREATE and REQUEST_COMMIT operations imply that $T \in \text{done}(s)(\pi)$. If $P \neq \text{parent}(T)$, then by Lemma 5 and the definition of $\text{directly-affects}(\alpha)$, ϕ affects some operation ρ in α' , where $\text{location}(\rho) = P$. The inductive hypothesis implies that $T \in \text{done}(s')(\rho)$, and the postconditions imply that $T \in \text{done}(s)(\pi)$.
2. $\pi = \text{CREATE}(T')$.

Then $\pi \neq \text{ABORT}(T)$, so assume $\phi = \text{ABORT}(T)$ affects π in α . By Lemma 5 and the definition of $\text{directly-affects}(\alpha)$, ϕ affects $\text{REQUEST_CREATE}(T')$ in α' . The inductive hypothesis implies that $T \in \text{done}(s')(\text{REQUEST_CREATE}(T'))$, and the postcondition of the CREATE operation implies that $T' \in \text{done}(s)(\pi)$.

3. $\pi = \text{COMMIT}(T',v)$.

Then $\pi \neq \text{ABORT}(T)$, so assume $\phi = \text{ABORT}(T)$ affects π in α . By Lemma 5 and the definition of $\text{directly-affects}(\alpha)$, either T is a child of T' , or ϕ affects some operation ρ in α' , where ρ is either $\text{REQUEST_COMMIT}(T',v)$ or a return operation for a child of T' . If T is a child of T' , ϕ is a return operation for a child of T' , and the inductive hypothesis implies that $T \in \text{done}(s')(\phi)$. Furthermore, since T' has a child, T' is not an access, and the postcondition for π implies that $T \in \text{done}(s)(\pi)$. If T is not a child of T' , the inductive hypothesis implies that $T \in \text{done}(s')(\rho)$ and the postconditions of the COMMIT operation imply that $T \in \text{done}(s)(\pi)$.

4. $\pi = \text{ABORT}(T')$

If $T = T'$, the postcondition for π implies that $T \in \text{done}(s)(\pi)$. Otherwise, assume that $\phi = \text{ABORT}(T)$ affects π in α . Then by Lemma 5 and the definition of $\text{directly-affects}(\alpha)$, ϕ affects $\text{REQUEST_CREATE}(T')$ in α' . Then the inductive hypothesis implies that $T \in \text{done}(s')(\text{REQUEST_CREATE}(T'))$, and the postcondition of the ABORT operation implies that $T \in \text{done}(s)(\pi)$.

□

6.3. Simulation of Generic Systems by Argus Systems

Lemma 14 shows that the Argus controller propagates enough information about aborts so that every operation π "knows about" (in $\text{done}(s)(\pi)$) every abort that affects it. The following lemma shows that the information in $\text{done}(s)$, combined with the precondition on commits of accesses, is enough to ensure that Argus systems simulate filtered systems.

Lemma 15: Every Argus schedule is a filtered schedule.

Proof: The proof is by induction on the lengths of Argus schedules. The basis, length 0, is trivial. For the inductive step, let α be an Argus schedule of the form $\alpha'\pi$, where π is a single operation. Let s_A be a state of the Argus controller after α' , and let s_F be the state of the filtered controller after α' . (Notice that the state of the filtered controller is uniquely defined by α' , while the state of the Argus controller is not.) The only case that is not immediate is where $\pi = \text{COMMIT}(T,v)$ and T is an access. So assume that this is the case.

We must show that π is enabled in s_F . This amounts to showing that if T' is an ancestor of T , then $\text{ABORT}(T')$ does not affect π in α . Suppose the contrary: that $\phi = \text{ABORT}(T')$, for some ancestor T' of T , and that ϕ affects π in α . Since T has no children, ϕ affects $\psi = \text{REQUEST_COMMIT}(T,v)$ in α' . By Lemma 14, $T' \in \text{done}(s_A)(\psi)$. But this violates the precondition for π in the Argus controller. □

The following theorem shows that Argus systems, like filtered systems, ensure that every non-access transaction gets a view it could get in an execution in which it is not an orphan.

Theorem 16: Let α be an Argus schedule and let T be a non-access transaction. Then there exists a generic schedule β such that T is not an orphan in β and $\beta|T = \alpha|T$.

Proof: Immediate by Lemma 15 and Theorem 11. \square

As for the filtered controller, if we define an *Argus locking system* to be an Argus system with locking objects, and *Argus locking schedules* to be schedules of Argus locking systems, then we obtain the following corollary.

Corollary 17: Any Argus locking system is serially correct.

Proof: Let α be an Argus locking schedule and let T be a non-access transaction. Theorem 16 yields a locking schedule γ such that T is not an orphan in γ and $\gamma|T = \alpha|T$. Theorem 4 then yields the required serial schedule β . \square

Similarly, we can use the Argus controller with any collection of objects that ensures serial correctness for non-orphans, and obtain serial correctness for all non-access transactions.

7. Strictly Filtered Systems

As it turns out, the orphan elimination algorithm described in [11] ensures a stronger property than does the Argus algorithm. In this section we define a "strictly filtered controller", which allows an access to commit only if no ancestor has aborted. (Compare this to the filtered controller, which allows an access to commit if an ancestor has aborted as long as the access is not affected by the abort.) We then define strictly filtered systems, which are composed of transactions, generic objects, and the strictly filtered controller, and show that strictly filtered systems simulate filtered systems. In the next section we will describe formally the algorithm from [11] and show that it simulates strictly filtered systems.

7.1. Strictly Filtered Controller

The strictly filtered controller is similar to the generic controller: it has the same operations, and the same states. The transition relations associated with the operations are also identical to those for the generic controller, except for the COMMIT operation for accesses, which is defined as follows:

- COMMIT(T, v), T an access

Precondition:

$$\begin{aligned} (T, v) &\in \text{commit_requested}(s') \\ T &\notin \text{returned}(s') \\ \text{ancestors}(T) \cap \text{aborted}(s') &= \emptyset \end{aligned}$$

Postcondition:

$$\text{committed}(s) = \text{committed}(s') \cup \{T\}$$

The COMMIT operation for an access has an additional precondition, which permits the transaction to commit only if none of its ancestors has already aborted.

7.2. Strictly Filtered Systems

A *strictly filtered system* is the composition of transactions, generic objects and the strictly filtered controller. Schedules of the strictly filtered system are *strictly filtered schedules*.

Lemma 18: Every strictly filtered schedule is a generic schedule.

Proof: Immediate. \square

7.3. Simulation of Generic Systems by Strictly Filtered Systems

Lemma 19: Every strictly filtered schedule is a filtered schedule.

Proof: By induction on the length of strictly filtered schedules. The basis, when the length of the schedule is 0, is easy. For the inductive step, let $\alpha = \alpha'\pi$ be a strictly filtered schedule, with π a single operation. Let s_S be the state of the strictly filtered controller after α' , and let s_F be the state of the filtered controller after α' . The only difference between s_S and s_F is that s_F includes α' as its history component.

The only interesting case is where π is a COMMIT(T, v), for T an access, so assume this is so. Since π is enabled in s_S , $\text{ancestors}(T) \cap \text{aborted}(s_S) = \emptyset$, so that there is no ABORT(T') in α' , for T' an ancestor of T . Then no such ABORT(T') can affect π in α , so π is enabled in s_F . \square

Like filtered systems and Argus systems, strictly filtered systems prevent orphans from discovering that they are orphans:

Theorem 20: Let α be a strictly filtered schedule and let T be a non-access transaction. Then there exists a generic schedule β such that T is not an orphan in β and $\beta|T = \alpha|T$.

Proof: Immediate by Lemma 19 and Theorem 11. \square

As before, we can define a *strictly filtered locking system* to be a strictly filtered system with locking objects, and *strictly filtered locking schedules* to be schedules of strictly filtered locking systems. We then obtain the following corollary.

Corollary 21: Any strictly filtered locking system is serially correct.

Proof: Let α be a strictly filtered locking schedule and let T be a non-access transaction. Theorem 20 yields a locking schedule γ such that T is not an orphan in γ and $\gamma|T = \alpha|T$. Theorem 4 then yields the required serial schedule β . \square

As before, we can use the strictly filtered controller with any collection of objects that ensures serial correctness for non-orphans, and obtain serial correctness for all non-access transactions.

8. Clock Systems

In this section we describe formally the orphan elimination algorithm from [11]. (More precisely, two algorithms are described in [11], an "eager" algorithm based on physical clocks, and a "lazy" algorithm based on logical clocks. Here we describe the eager algorithm. The lazy algorithm can be described and analyzed in a manner similar to that used for the Argus algorithm.) We do this by defining a "clock controller," which uses a global clock to ensure that transactions do not abort until all their descendant accesses have stopped running. We then define clock systems, which are composed of transactions

generic objects, and the clock controller. Finally, we show that clock systems simulate strictly filtered systems, and thus generic systems as well.

8.1. The Clock Controller

The clock controller maintains a quiesce time for each access transaction and a release time for every transaction. An access transaction is allowed to commit only if its quiesce time has not passed. Release times are chosen so that once a transaction's release time is reached, all its descendant accesses have quiesced. A transaction is allowed to abort only if its release time has passed. This ensures that, after a transaction aborts, none of its descendant accesses will commit.

If quiesce and release times are fixed in advance, some transactions may be forced to abort unnecessarily as their quiesce times expire. It is possible to obtain extra flexibility by providing operations in the clock controller for adjusting quiesce and release times.

The clock controller has ten operations:

Input Operations:

REQUEST_CREATE(T),
REQUEST_COMMIT(T,v).

Output Operations:

CREATE(T),
COMMIT(T,v)
ABORT(T)
INFORM_COMMIT_AT(X)OF(T)
INFORM_ABORT_AT(X)OF(T)
TICK
ADJUST_QUIESCE(T)
ADJUST_RELEASE(T)

These are the same as for the generic controller, with the addition of three new output operations: TICK, ADJUST_QUIESCE and ADJUST_RELEASE. These output operations are to be thought of as "internal" to the clock controller, in that they will not be used as inputs to any other components of the clock system. The TICK operation advances the clock, while the two ADJUST operations adjust quiesce and release times. By adjusting the quiesce time for a transaction to be later than its current value, we can extend the time during which a transaction is allowed to run. Similarly, by adjusting the release time for a transaction to be earlier than its current value, we can allow a transaction to abort without waiting as long as would otherwise be necessary.

The state of the clock controller consists of eight components. The first five are as in the generic controller, and are initialized in the same way. The other three are clock(s), quiesce(s), and release(s). A.

before, we denote the initial state of the controller by s_0 . $\text{Clock}(s)$ is a real number, initialized arbitrarily. $\text{Quiesce}(s)$ is a total mapping from access transactions to real numbers, and $\text{release}(s)$ is a total mapping from all transactions to real numbers. The initial values of quiesce and release are arbitrary, subject to the following condition: for all transactions T and T' , where T' is an ancestor of T , $\text{quiesce}(s_0)(T) \leq \text{release}(s_0)(T')$. We define $\text{returned}(s)$ as usual.

The transition relations associated with the clock controller operations are as for the generic controller, except for $\text{COMMIT}(T,v)$ for access transactions T , $\text{ABORT}(T)$, TICK , $\text{ADJUST_QUIESCE}(T)$ and $\text{ADJUST_RELEASE}(T)$. These are defined below.

- $\text{COMMIT}(T,v)$, where T is an access
 Precondition:
 $(T,v) \in \text{commit_requested}(s')$
 $T \notin \text{returned}(s')$
 $\text{clock}(s') < \text{quiesce}(T)(s')$
 Postcondition:
 $\text{committed}(s) = \text{committed}(s') \cup \{T\}$
- $\text{ABORT}(T)$
 Precondition:
 $T \in \text{create_requested}(s') - \text{returned}(s')$
 $\text{release}(s')(T) \leq \text{clock}(s')$
 Postcondition:
 $\text{aborted}(s) = \text{aborted}(s') \cup \{T\}$
- TICK
 Postcondition:
 $\text{clock}(s') < \text{clock}(s)$
- $\text{ADJUST_RELEASE}(T)$
 Precondition:
 if $T \in \text{aborted}(s')$, then $r \leq \text{clock}(s')$
 $\text{quiesce}(s')(T') \leq r$ for all $T' \in \text{descendants}(T)$
 Postcondition:
 $\text{release}(s)(T) = r$
- $\text{ADJUST_QUIESCE}(T)$
 Precondition:
 $q \leq \text{release}(s')(T')$ for all $T' \in \text{ancestors}(T)$
 Postcondition:
 $\text{quiesce}(s)(T) = q$

8.2. Clock Systems

A *clock system* is the composition of transactions, generic objects, and the clock controller. Operations of a clock system are called *clock operations*. Schedules of a clock system are called *clock schedules*. If α is any sequence of clock operations, define $\text{generic}(\alpha)$ to be the subsequence of α containing exactly the generic operations in α .

Lemma 22: If α is a clock schedule, then $\text{generic}(\alpha)$ is a generic schedule.

Proof: Straightforward by induction. \square

Lemma 23: Let α be a clock schedule, and let s be the state of the clock controller after α .
 (a) If $T \in \text{aborted}(s)$, then $\text{release}(s)(T) \leq \text{clock}(s)$. (b) For all access transactions T and all ancestors T' of T , $\text{quiesce}(s)(T) \leq \text{release}(s)(T')$.

Proof: Straightforward by induction. \square

8.3. Clock Systems Simulate Generic Systems

The following lemma shows that clock systems simulate strictly filtered systems.

Lemma 24: If α is a clock schedule, then $\text{generic}(\alpha)$ is a strictly filtered schedule.

Proof: The proof is by induction on the length of α . The basis, when the length of α is 0, is easy. For the inductive step, let $\alpha = \alpha'\pi$, where π is a single operation. Let s_C be a state of the clock controller after α , and s_S the state of the strictly filtered controller after $\text{generic}(\alpha')$. The only interesting case is where $\pi = \text{COMMIT}(T, v)$ for T an access, so suppose this is so.

Since π is enabled in s_C , we know that $\text{clock}(s_C) < \text{quiesce}(s_C)(T)$. Let T' be an ancestor of T . If $T' \in \text{aborted}(s_S)$, then $T' \in \text{aborted}(s_C)$. Then Lemma 23 implies that $\text{release}(s_C)(T') \leq \text{clock}(s_C)$. Lemma 23 also implies that $\text{quiesce}(s_C)(T) \leq \text{release}(s_C)(T')$. Thus, $\text{quiesce}(s_C)(T) \leq \text{clock}(s_C)$, a contradiction. It follows that no ancestor of T is in $\text{aborted}(s_S)$, so that π is enabled in s_S . \square

Clock systems also prevent orphans from discovering that they are orphans:

Theorem 25: Let α be a clock schedule and T a non-access transaction. Then there exists a generic schedule β such that T is not an orphan in β and $\beta|T = \alpha|T$.

Proof: Lemma 24 and Theorem 20 imply the existence of a generic schedule β such that T is not an orphan in β in $\beta|T = \text{generic}(\alpha)|T$. But $\text{generic}(\alpha)|T = \beta|T$, so the result follows. \square

We define a *clock locking system* to be a clock system with locking objects, and *clock locking schedules* to be schedules of clock locking systems. The following corollary is immediate.

Corollary 26: Any clock locking system is serially correct.

Proof: By Theorems 25 and 4. \square

9. Conclusions

We have defined correctness properties for orphan elimination algorithms, and have presented precise descriptions and proofs for two algorithms from [7] and [11]. Our proofs are quite simple, and show that the systems exhibit a substantial degree of modularity: the orphan elimination algorithms can be used in combination with any concurrency control protocol that ensures correctness for non-orphans. The simplicity of our proofs is a direct result of this modularity, and is in sharp contrast to earlier work [4] in which the orphan elimination algorithm and the concurrency control protocol were not cleanly separated.

In this paper we have analyzed only orphans that result from aborts of transactions. We are currently

studying orphans that result from crashes. The algorithms for detecting and eliminating such orphans described in [7, 11] are quite interesting, but also more complicated than the algorithms for handling aborts. We would like to find a similar separation of concerns for the crash-orphan algorithms, showing, for example, that the crash-orphan algorithms are independent of the concurrency control protocol and the abort-orphan algorithm used in the system. Whether this will be possible is still open.

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